

Surname	Centre Number	Candidate Number
First name(s)		2



**GCE A LEVEL**

1305U60-1



S24-1305U60-1

**WEDNESDAY, 12 JUNE 2024 – AFTERNOON**

**FURTHER MATHEMATICS – A2 unit 6**  
**FURTHER MECHANICS B**

1 hour 45 minutes

For Examiner's use only		
Question	Maximum Mark	Mark Awarded
1	11	
2	16	
3	13	
4	13	
5	13	
6	14	
<b>Total</b>	<b>80</b>	

**ADDITIONAL MATERIALS**

In addition to this examination paper, you will need:

- a Formula Booklet;
- a calculator.

**INSTRUCTIONS TO CANDIDATES**

Use black ink or black ball-point pen. Do not use gel pen or correction fluid.

You may use a pencil for graphs and diagrams only.

Write your name, centre number and candidate number in the spaces at the top of this page.

Answer **all** questions.

Take  $g$  as  $9.8 \text{ ms}^{-2}$ .

Write your answers in the spaces provided in this booklet. If you run out of space, use the additional page(s) at the back of the booklet, taking care to number the question(s) correctly.

**INFORMATION FOR CANDIDATES**

The maximum mark for this paper is 80.

The number of marks is given in brackets at the end of each question or part-question.

Sufficient working must be shown to demonstrate the **mathematical** method employed.

Answers without working may not gain full credit.

Unless the degree of accuracy is stated in the question, answers should be rounded appropriately.

You are reminded of the necessity for good English and orderly presentation in your answers.

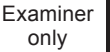


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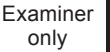


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- (b) Calculate the coefficient of restitution between  $A$  and  $B$ .

[3]

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- (c) Find the angle through which the direction of motion of  $B$  is deflected as a result of the collision. Give your answer correct to the nearest degree.

[3]

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- (d) After the collision, sphere  $B$  continues to move with velocity  $(-4\mathbf{i} - 5\mathbf{j})\text{ms}^{-1}$  until it collides with another sphere  $C$ , which exerts an impulse of  $(-20\mathbf{i} + 18\mathbf{j})\text{Ns}$  on  $B$ .

Find the velocity of  $B$  after the collision with  $C$ .

[2]

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- (a) Show that  $v$  satisfies the differential equation

[3]



At time  $t = 0$ , the object passes a point A with a speed of  $\sqrt{g}$  ms<sup>-1</sup>. The object then hits the ground with a speed of 8 ms<sup>-1</sup>.

(b) Calculate the time taken for the object to hit the ground. [6]

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- [7]





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- The diagram shows a shaded region bounded by two circular arcs. A vertical dashed line segment connects point A at the top to point C at the bottom. The right-hand boundary is a circular arc starting from point C and ending at point B. A vertical double-headed arrow between points C and B is labeled  $2a$ .





- (b) Suppose that the lamina is suspended in equilibrium by means of two vertical wires attached at  $A$  and  $B$  so that  $AB$  is horizontal. Find the fraction of the lamina's weight that is supported by the wire attached at  $B$ . [3]

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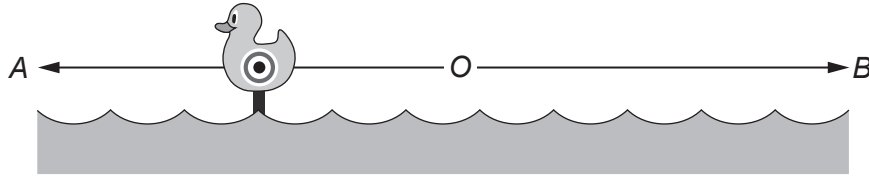


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4. The diagram below shows part of a game at a funfair that consists of a target moving along a straight horizontal line  $AB$ . The centre of the target may be modelled as a particle moving with Simple Harmonic Motion about centre  $O$ , where  $O$  is the midpoint of  $AB$ .



When the target is at a distance of 84 cm from O, its speed is  $52 \text{ cms}^{-1}$  and the magnitude of its acceleration is  $1344 \text{ cms}^{-2}$ .

- (a) Show that the period of the motion is  $\frac{\pi}{2}$  s. [3]



[5]



- [illegible]



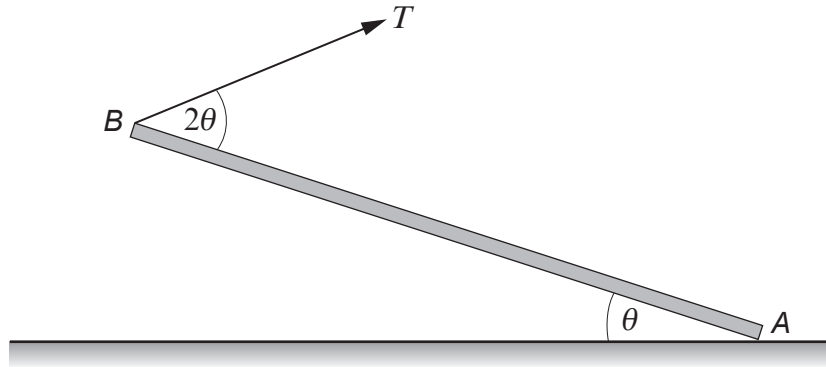


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5. The diagram below shows a uniform rod  $AB$  of weight  $WN$  and length  $2l$ , with its lower end  $A$  resting on a rough horizontal floor. A light cable is attached to the other end  $B$ . The rod is in equilibrium when it is inclined at an angle of  $\theta$  to the floor, where  $0^\circ < \theta \leq 45^\circ$ . The tension in the cable is  $TN$  acting at an angle of  $2\theta$  to the rod, as shown in the diagram.



- (a) (i) Show that  $T = \frac{W}{4} \operatorname{cosec} \theta$ . [4]
- (ii) Hence determine the normal reaction of the floor on the rod at  $A$ , giving your answer in terms of  $W$ . [4]







- $$y = \frac{a}{b} \sqrt{b^2 - x^2},$$

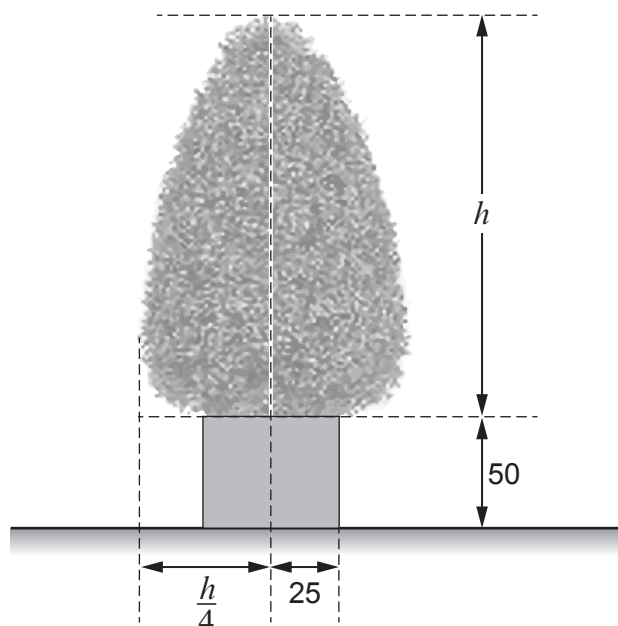
A Cartesian coordinate system with x and y axes. The origin is labeled  $O$ . The y-axis has a point  $a$  and the x-axis has a point  $b$ . A shaded region  $R$  is shown in the first quadrant, bounded by the y-axis from  $0$  to  $a$ , the x-axis from  $0$  to  $b$ , and a concave-down curve connecting  $(0, a)$  and  $(b, 0)$ .

The volume of  $S$  is  $\frac{2}{3}\pi a^2b$ .

- (a) Use integration to show that the distance of the centre of mass of  $S$  from the  $y$ -axis is  $\frac{3b}{8}$ .



The diagram below shows a small tree growing in a pot. The uniform solid  $S$  described on the previous page may be used to model the part of the tree above the pot. This part of the tree has height  $h$  cm and base radius  $\frac{h}{4}$  cm. The pot, including its contents, may be modelled as a solid cylinder of height 50 cm and radius 25 cm.



You may assume that the density of the pot, including its contents, is equal to 20 times the density of the part of the tree above the pot.





- (c) Identify one possible limitation of the model used that could affect your answer to part (b).

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