

Surname	Centre Number	Candidate Number
First name(s)		2



GCE A LEVEL

1305U40-1



S24-1305U40-1

MONDAY, 3 JUNE 2024 – AFTERNOON

FURTHER MATHEMATICS – A2 unit 4
FURTHER PURE MATHEMATICS B

2 hours 30 minutes

ADDITIONAL MATERIALS

In addition to this examination paper, you will need:

- a Formula Booklet;
- a calculator.

INSTRUCTIONS TO CANDIDATES

Use black ink or black ball-point pen. Do not use gel pen or correction fluid.

You may use a pencil for graphs and diagrams only.

Write your name, centre number and candidate number in the spaces at the top of this page.

Answer **all** questions.

Write your answers in the spaces provided in this booklet. If you run out of space, use the additional page(s) at the back of the booklet, taking care to number the question(s) correctly.

INFORMATION FOR CANDIDATES

The maximum mark for this paper is 120.

The number of marks is given in brackets at the end of each question or part-question.

Sufficient working must be shown to demonstrate the **mathematical** method employed.

Answers without working may not gain full credit.

Unless the degree of accuracy is stated in the question, answers should be rounded appropriately.

You are reminded of the necessity for good English and orderly presentation in your answers.

For Examiner's use only		
Question	Maximum Mark	Mark Awarded
1	11	
2	13	
3	9	
4	21	
5	14	
6	8	
7	12	
8	11	
9	9	
10	12	
Total	120	

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- This image shows a full page of a worksheet designed for handwriting practice. It features approximately 20 horizontal dashed lines spaced evenly across the page, providing a guide for letter height and placement. The background is plain white, and there are no other markings or text present.



2. The function f is defined by $f(x) = \cosh\left(\frac{x}{2}\right)$.

- (a) State the Maclaurin series expansion for $\cosh\left(\frac{x}{2}\right)$ up to and including the term in x^4 . [2]

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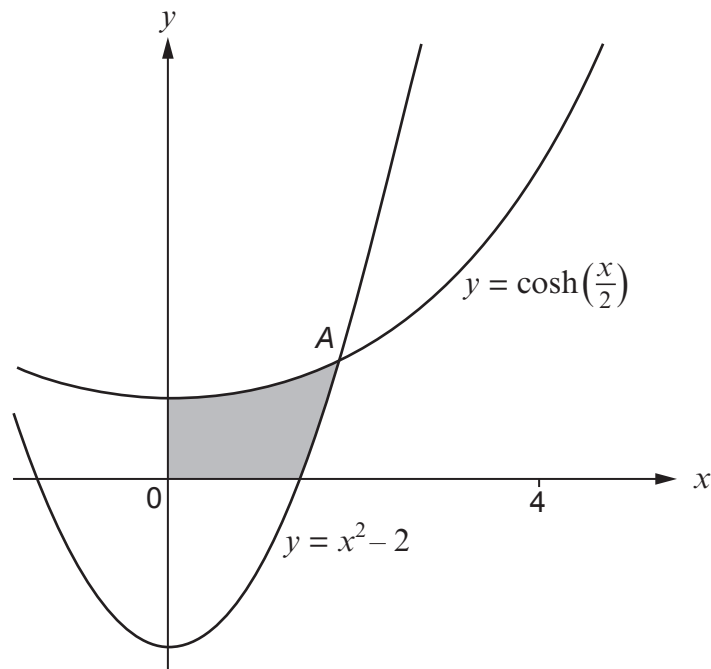
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Another function g is defined by $g(x) = x^2 - 2$. The diagram below shows parts of the graphs of $y = f(x)$ and $y = g(x)$.



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- [6]



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$$\cos x \frac{dy}{dx} + y \sin x = 4 \cos^3 x \sin x + 5$$

[9]







$$r = 3 - 4 \cos^2 \theta, \quad \text{where } \frac{\pi}{6} \leq \theta \leq \frac{5\pi}{6}.$$




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[8]

(a) $\int \frac{3-x}{x(x^2+1)} dx$



(b) $\int \frac{\sinh 2x}{\sqrt{\cosh^4 x - 9 \cosh^2 x}} dx$

[6]



6. The matrix \mathbf{M} is defined by

$$\mathbf{M} = \begin{pmatrix} 12 & 30 & 8 \\ 18 & 25 & 20 \\ 19 & 50 & 16 \end{pmatrix}.$$

- (a) Given that $\det \mathbf{M} = -1040$, give a geometrical interpretation of the solution to the following equation. [2]

$$\begin{pmatrix} 12 & 30 & 8 \\ 18 & 25 & 20 \\ 19 & 50 & 16 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 2668 \\ 3402 \\ 4581 \end{pmatrix}$$

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- (b) Three hotels A, B, C each have different types of room available to book: single, double and family rooms. For each type of room, the price per night is the same in each of the three hotels.

The table below gives, for each hotel, details of the number of each type of room and the total revenue per night when the hotel is full.

Hotel	Types of room			Total revenue
	Single	Double	Family	
A	12	30	8	£2,668
B	18	25	20	£3,402
C	19	50	16	£4,581



[6]



- (i) Find the mean value of $y = \frac{1}{\sqrt{16-6x-x^2}}$ between $x = -3$ and $x = 1$. [4]

[illegible]



(b) Evaluate the improper integral

$$\int_1^{\infty} \frac{-8e^{-2x}}{4e^{-2x} - 5} dx,$$

giving your answer correct to three decimal places.

[3]

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[6]

[illegible]

$$\sin 6\theta + 2\cos^2\theta = 3\cos 2\theta - \sin 2\theta + 1.$$

[9]





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$$\frac{dy}{dt} = 6x + 8y + 15e^{3t}$$

$$\frac{dy}{dt} = 6x + 8y + 15e^{3t}$$

[5]



[7]



[illegible]

[illegible]

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