

ch # 10
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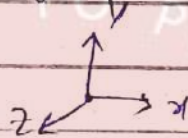
Thermodynamics

Degree of freedom:

No of independent ways on which particle can move.

* Translatory degree of freedom:

* Three ways motion



* Rotational degree of freedom:

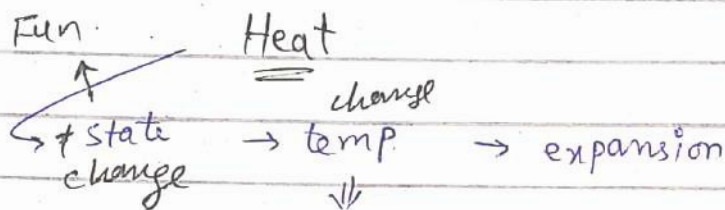
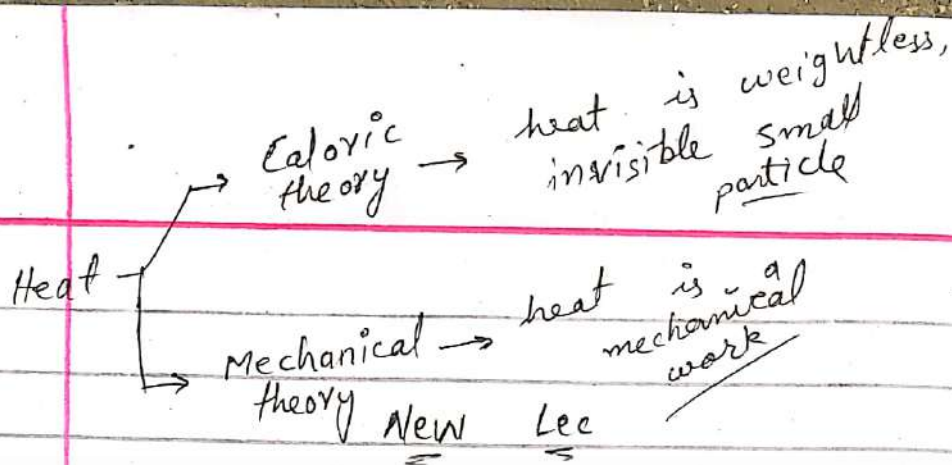
* Two ways motion

clockwise Anti-clockwise









* So heat is the form of energy.
 OR * The total K.E of a molecule of a system is called heat

* Heat produces motion.

$$H \propto W$$

$$H = JW$$

mechanical equivalent of heat

$$J = \frac{H}{W}$$

1st Law of Thermodynamics



It gives the mathematical relation b/w heat, U & Work

$$\Delta Q = \Delta U + \Delta W$$

$$\Delta Q = \Delta U + P\Delta V$$

Small ← change small

Inferences from 1st Law of T.D:

- * 1st time related heat energy with other form of energy.
- * It is law of conservation of ^(heat) energy.
- * "U" is state function.

* The definition of heat as energy in transit. ↓

Thermal (heat) energy can be converted into mechanical work.

* For a cyclic process
 $\Delta U = 0$ ($U_i = U_f$)

Limitation:

* It does not indicate the direction of heat. ↓

1st Law does not indicate why the heat can't flow a cold body to hot body

* It does not tell anything about the condition under which heat can be transformed into work. ↓

Feasibility of process/spontaneity

* 1st Law of T.D. does not indicate as to why all work convert into heat & all heat cannot to work $\Downarrow$ 100% efficient engine

* All natural spontaneous process are irreversible.

Application

a) Isothermal process:

$$T = \text{constant} \Rightarrow \Delta T = 0$$

$$U = \text{constant} \Rightarrow \Delta U = 0$$

$Q, P, V \rightarrow \text{variable}$

* conducting wall / Diathermic wall

* According to 1st Law of T.D

Isothermal expansion
 $\Downarrow$

$$\boxed{\Delta Q = \Delta W}$$

Isothermal Compression
 $\Downarrow$

$$\boxed{-\Delta Q = -\Delta W}$$

* equation of Isothermal process

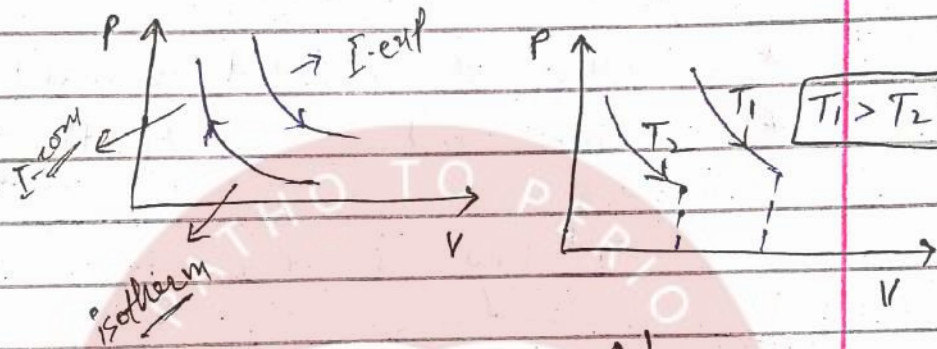
$$\boxed{P_1 V_1 = P_2 V_2}$$

Boyle's Law

* W. done in Isothermal process:

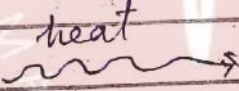
$$W = nRT \frac{\log V_2}{\log V_1} \Rightarrow (W \propto T)$$

④ Graph of Isothermal process:

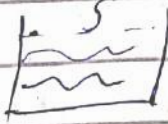


examples:

a): Latent heat of fusion

heat  ice (melting)
 $T = \text{constant}$

b): Latent heat of ~~ev~~ vaporization:

 (Boiling)
($T = \text{constant}$)

New Lec

(d) Adiabatic Process:

* $\Delta Q = 0 \Rightarrow$ No heat enter nor lost $\Rightarrow$ heat content are kept constant.

* $P, V, T \rightarrow$ Variable

* quick process (Rapid change)

* non-conducting wall (adiabatic wall)

1st Law of T.D

A. expansion
($\Delta Q = 0$)

$$\Delta W = \Delta U$$



* work is done at cost of Internal energy

* System used its own

I.E for work.

$$I.E = \downarrow$$

$$T = \downarrow$$

* cooling

A. compression

$$\Delta W = \Delta U$$



* work done is converted into I.E.

$I.E \uparrow$
 $T \uparrow$
* heating is produced

* Equation of Adiabatic process

$$PV^\gamma = \text{const}$$

$$P_1 V_1^\gamma = P_2 V_2^\gamma$$



poisson's equation

$$\rho \propto \frac{1}{V^\gamma}$$

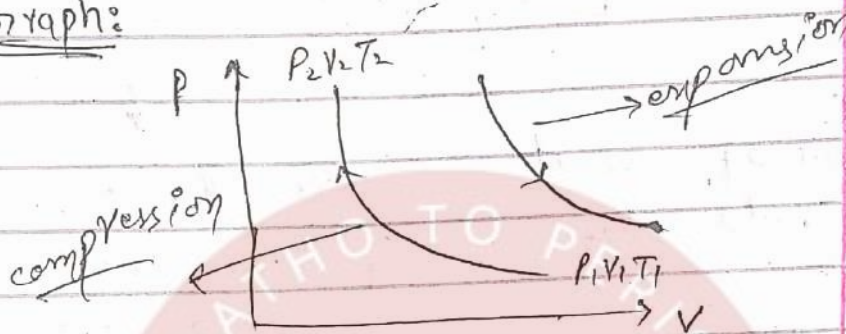
$$\gamma = \frac{C_p}{C_v}$$

* W. done in A. process:

$$W = nR(T_1 - T_2)$$

$$W \propto T_1 - T_2$$

Graph:



* Graph of A. process is called Adiabats. Adiabats is hyperbola in shape.

* Adiabats is steeper than isotherm

MCQs:

The ratio of slope of adiabatic to isothermal graph is.

- a) $1:\gamma$ b) $\gamma:1$ c) $\sqrt{\gamma}:1$ d) $1:\sqrt{\gamma}$

Q.9

* isothermal process slope = P/V
 * Adiabatic process slope = P/V^γ

Q.10

* Rapid escape of air from a burst tyre.

* The rapid expansion & compression of air through which sound waves is passing

* ~~so~~ clouds formation in atmosphere

② Isochoric process or Isometric process

* Volume = Constant

* $Q, P, T, =$ variable

$$\boxed{\Delta Q = \Delta U + \Delta W} \quad \uparrow 0$$

Conversion of heat energy into I.E of system

$P \uparrow$
 $T \uparrow$
 $U \uparrow$

$$\Rightarrow \boxed{\Delta Q = \Delta U}$$

Removal of heat $\Rightarrow$ equivalent decrease in the I.E

$P \downarrow$
 $T \downarrow$
 $U \downarrow$

$$\Rightarrow \boxed{\Delta Q = \Delta U}$$

* Its indicator is temp

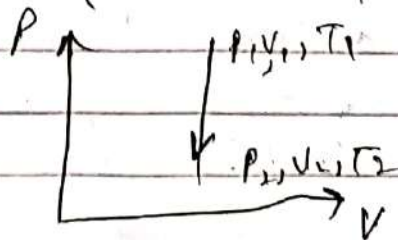
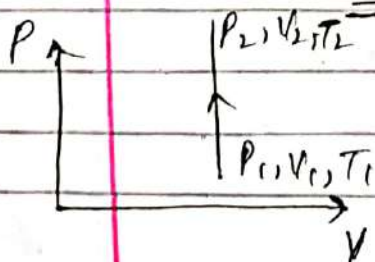
* $\boxed{P \propto T}$ $\frac{P}{T} = \text{constant}$

$$\boxed{\frac{P_1}{T_1} = \frac{P_2}{T_2}}$$

e.g.

pressure cooker is the example of isochoric process

Graph of isochoric process



④ Isobaric Process:

- * $P = \text{constant}$
- * $V, T, \Delta Q = \text{variable}$
- * In isobaric process, heat is divided into two parts. Some energy is used in W done $\therefore$ rest of the heat energy is changed of temperature.

$$\Delta Q = \Delta U + \Delta W$$

$$(\Delta Q = \Delta U + P\Delta V)$$

constant

equation:

$$V \propto T$$

$$\boxed{\frac{V_1}{V_2} = \frac{T_1}{T_2}}$$

W done:



$$W = P(V_2 - V_1)$$

⑤ Isolated process:

$$\Delta Q = 0$$

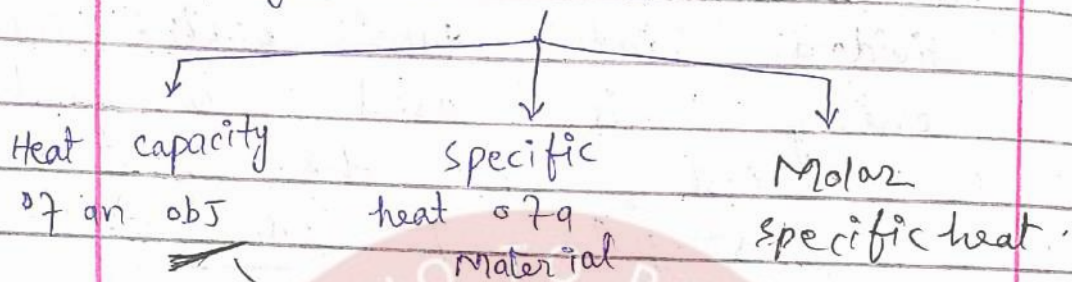
$$\Delta W = 0$$

$$\Delta U = 0$$

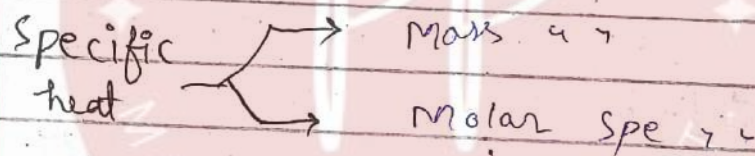
New Lec

Heat Capacity

Amount of heat required to raise the temp of substance by 1°C or 1°F .



heat required to raise the temper by 1°C .



a) Mass specific heat:

$$\Delta Q \propto m$$

$$\Delta Q \propto \Delta T$$

$$\Delta Q \propto m \Delta T \quad \Delta Q = C m \Delta T$$

$$C = \frac{\Delta Q}{\Delta T m} \quad \text{or} \quad C = \frac{S}{m} \quad \therefore S = \frac{\Delta Q}{\Delta T}$$

b) Molar specific heat:

$$\Delta Q \propto n$$

$$\Delta Q \propto \Delta T$$

$$\Delta Q \propto n \Delta T$$

$$\Delta Q = C n \Delta T$$

$$C = \frac{\Delta Q}{n \Delta T}$$

$$C = \frac{S}{n}$$

isobaric

Molar Specific heat Capacity

isochoric

Molar specific heat at const pressure

Molar specific heat at const volume

$$C_p = \frac{\Delta Q_p}{n \Delta T}$$

$$C_v = \frac{\Delta Q_v}{n \Delta T} = \frac{\Delta U}{n \Delta T}$$

$$C_p = \frac{W + \Delta U}{n \Delta T}$$

$$Q_p > Q_v \quad \text{or} \quad C_p > C_v$$

$$Q_p = W + \Delta U$$

$$Q_p = W + Q_v \Rightarrow W = Q_p - Q_v$$

$$C_p - C_v = R$$

$$\gamma = \frac{C_p}{C_v} \quad \left(\gamma = \frac{1 + \frac{2}{f}}{1} \right)$$

③ Isothermal process: ④ Adiabatic process

$$T = \text{const}$$

$$\Delta T = 0$$

$$C = \frac{\Delta Q}{n \times 0}$$

$$C = \infty$$

$$Q = \text{const}$$

$$\Delta Q = 0$$

$$C = \frac{\Delta Q}{n \Delta T}$$

$$C = \frac{0}{n \Delta T}$$

$$C = 0$$

Gas	C_p	f	C_v	γ
* Monatomic	$\frac{5}{2}R$	3	$\frac{3}{2}R$	$\frac{5}{3} = 1.67$
* Diatomic	$\frac{7}{2}R$	5	$\frac{5}{2}R$	$\frac{7}{5} = 1.4$
* polyatomic	$\frac{9}{2}R$	6 or 7	$\frac{7}{2}R$	$\frac{9}{7} = 1.29$

Mayer's Relation

$$C_p = \frac{\gamma R}{\gamma - 1}$$

Mols: $\frac{R}{C_p} = \frac{\gamma - 1}{\gamma}$ $\frac{C_p}{\gamma} = \frac{R}{\gamma - 1}$

Mols: $\frac{R}{C_v} = \frac{\gamma - 1}{\gamma}$ $\frac{R}{C_p} = \left(\frac{\gamma - 1}{\gamma} \right)$

Note:

① $C_p - C_v = R$

$\gamma = \frac{C_p}{C_v} \Rightarrow C_v = \frac{C_p}{\gamma}$

$\gamma(C_p - C_v) = R$

$C_v(\gamma - 1) = R$ imp

$$C_v = \frac{R}{\gamma - 1}$$

$C_p - C_v = R$

$C_p - \frac{C_p}{\gamma} = R$

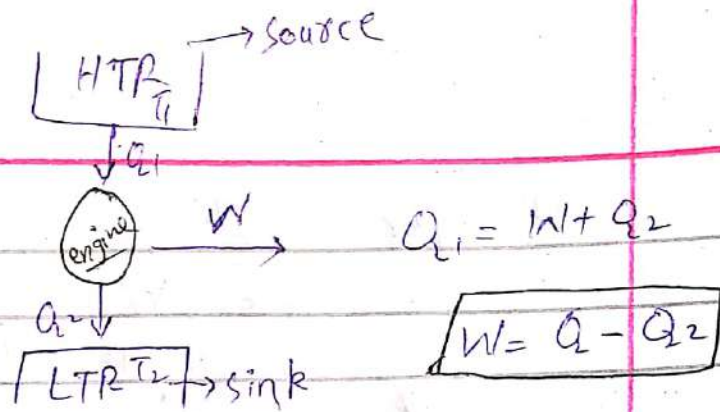
$C_p \left(1 - \frac{1}{\gamma} \right) = R$

imp

$$C_p = \frac{\gamma R}{\gamma - 1}$$

Heat engine

Convert heat energy
to mechanical energy



$$\eta = \frac{\text{output}}{\text{input}} \times 100\% \quad \eta = \frac{W}{Q_1} \times 100$$

$$\eta = \frac{Q_1 - Q_2}{Q_1} \times 100$$

$$\eta = \frac{Q_1}{Q_1} - \frac{Q_2}{Q_1} \times 100$$

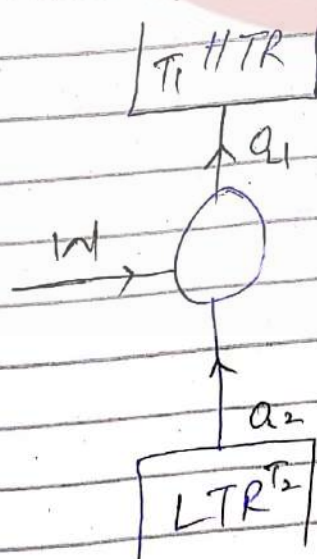
if $\boxed{Q_2 \uparrow}$
 $\boxed{\eta \downarrow}$

$$\boxed{\eta = 1 - \frac{Q_2}{Q_1} \times 100}$$

if $\boxed{Q_1 \uparrow}$
 $\boxed{\eta \uparrow}$

if $Q_2 = 0$ then $\eta = 1 \text{ or } 100\%$
 $\Downarrow$
 no sink

④ Refrigerator / Reverse heat engine / Heat pump



(*) For Cooling:
Room = LTR

Surround = HTR

~~heating~~

$$\eta = \frac{\text{output}}{\text{input}}$$

$$\eta = \frac{Q_2}{W}$$

$$\eta = \frac{Q_2}{Q_1 - Q_2}$$

$$\eta = \frac{Q_2}{T_1 - T_2}$$

(*) For heating

Room = HTR

Surround = LTR

$$\eta = \frac{Q_1}{W}$$

$$\eta = \frac{Q_1}{Q_1 - Q_2}$$

$$\eta = \frac{T_1}{T_1 - T_2}$$

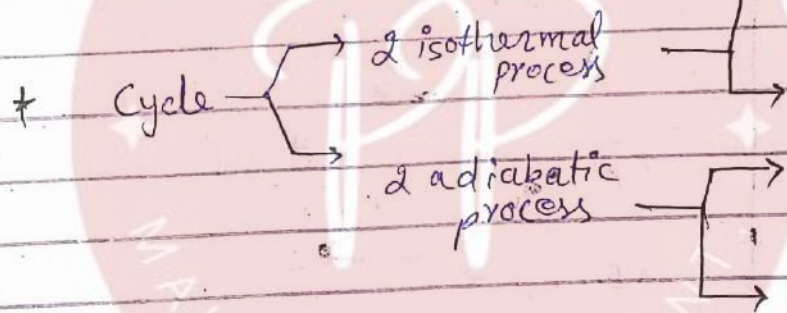
Carnot Engine

- * Ideal engine
- * can't be constructed practically
- * Most efficient heat engine
- * Sadi Carnot
- * η - depend upon tempera of

Source
(HTR)

Sink
(LTR)
- * independant of Nature of working substances.

* W. substances = ideal gas



$$\eta = 1 - \frac{T_2}{T_1} \quad \text{or} \quad \eta = \left(1 - \frac{T_2}{T_1}\right) \times 100\%$$

$$\text{or} \quad \eta = \left(1 - \frac{Q_2}{Q_1}\right) \times 100\%$$

$$\eta = \frac{T_1 - T_2}{T_1} \quad \eta = \frac{\Delta T}{T_1}$$

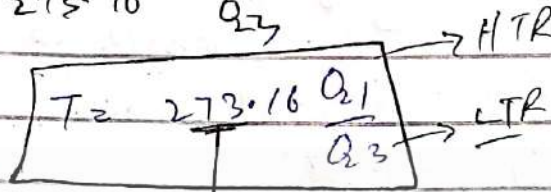
* $\frac{Q_1}{Q_2} = \frac{T_1}{T_2}$ → Carnot theorem

MCQs: if $T_2 = 0$

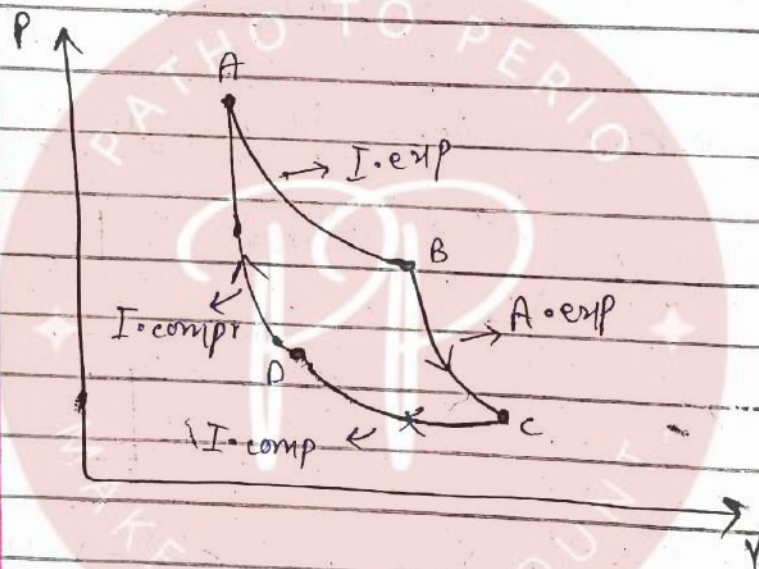
then $\eta = 100\%$

isotherm
 Adiabatic expansion
 adiabatic compression
 adi compression

if $\frac{T_1}{273.16} = \frac{Q_1}{Q_2}$



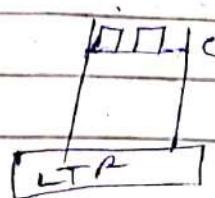
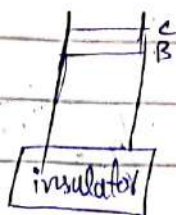
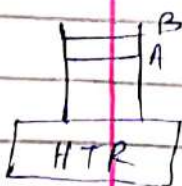
Triple point of water = 0°C
 at which three states of H_2O exist.



Carnot theorem

No engine can be more efficient than Carnot engine.

All C.O engine working b/w same temp have same η irrespective of w. substances



MCCS

(isother)

(*) During Carnot cycle, heat is given to the system, its temperature must _____.

- a) $\uparrow$ b) $\downarrow$ (c) Same d) None

(*) During Carnot cycle, heat is given out from the system, its temperature must _____.

- a) $\uparrow$ b) $\downarrow$ (c) Same d) None

$T_{\text{change}} \leftarrow \text{(adiabatic)} \downarrow$

(*) During Carnot heat, no heat is provided or taken out of the system, then temp of system must be _____.

- a) $\uparrow$ b) $\downarrow$ (c) may rise or fall d) None

Entropy

Statistical entropy $\rightarrow$ always $\uparrow$

The measure of randomness (disorder) is called statistical entropy.

$$S = k \ln w$$

$k = \text{Boltzmann const}$

$w = \text{probability of order/disorder}$

Thermal entropy

The unavailability of useful thermal energy is called Thermal entropy.

$$\Delta S = \frac{\Delta Q}{\Delta t}$$

$S \rightarrow$ is a state variable (II Law T.D)
* J/K



$$w = 1$$

$$S = k \ln 1 \Rightarrow$$

$$S = k(0)$$

$$\boxed{S=0}$$



$$\neq w \neq 1$$

$$\neq S \neq 1$$

Entropy

For a System

At body level

At engine

a) For a process as $\Delta Q = 0$
So $\Delta Q = 0$
 $S = \text{const}$
 $\boxed{\Delta S = 0}$

b) For all reversible process
 $\Delta S = 0$

c) For all irreversible process
 $\Delta S \neq 0$
 $\Delta S \neq +ve$ $S = \uparrow$

d) ΔS for universe is always +ve.

$\Delta S \geq 0$ $\begin{cases} \Delta S = 0 \text{ (Reversible)} \\ \Delta S > 0 \text{ (Irreversible)} \end{cases}$

① At body level:

a) Hot body Reject heat

$$\star S \downarrow \star \Delta S = -ve \star \Delta S_1 = -\frac{Q}{T_1}$$

b) At cold body (LTR):

$$\star S \uparrow \star \Delta S = +ve \star \Delta S = +\frac{Q}{T_2}$$

New Lec

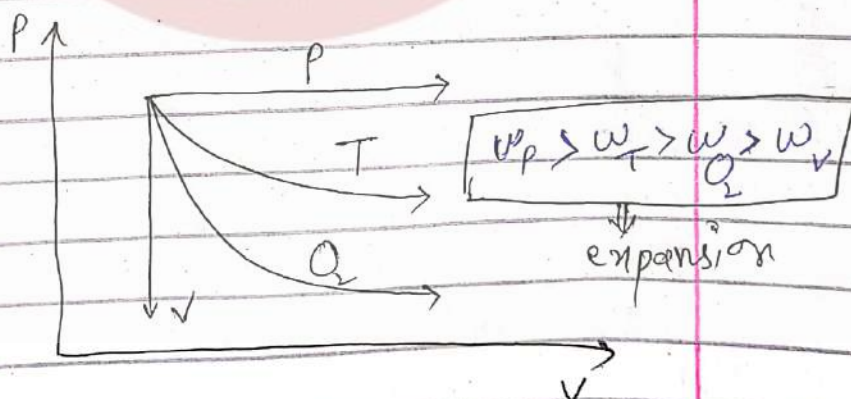
② At engine level:

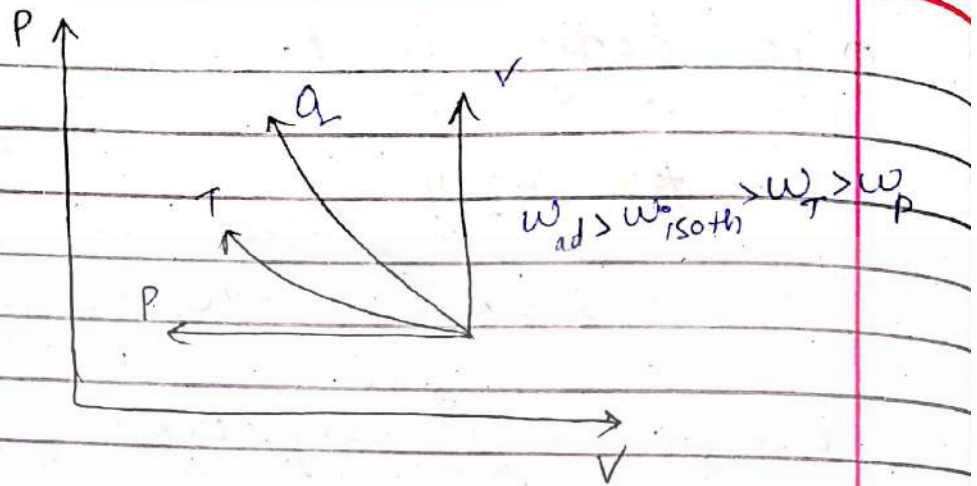
$$\Delta S = +ve, S \uparrow$$

$$\Delta S = \Delta S_2 + \Delta S_1$$

$$\Delta S = \frac{Q}{T_2} - \frac{Q}{T_1}$$

$$\Delta S = +ve (T_1 > T_2)$$





Zeroth Law:

gives definition of
Temperature

