

PART-A

1. Choose the correct homophone for Ascent.

- A) Accent
- B) Assent
- C) Axent
- D) Axant

2. Which of the following is an Indian Grammarian?

- A) Bhash
- B) Bharata
- C) Panini
- D) Prakasam

3. Find the correct expression.

- A) Between you and I
- B) Between you and me
- C) Between you and my
- D) Between you and mine

4. Pair with harp from the following.

- A) on
- B) at
- C) upon
- D) in

5. Who is the Indian Nobel Laureate for Literature?

- A) Jatin Kumar Naik
- B) Hargobind Khurana
- C) Rabindranath Tagore
- D) Mother Teresa

6. Who among the following wrote The Jungle Book?

- A) Mark Twaine
- B) R.K. Narayan
- C) Rudyard Kipling
- D) Rabindranath Tagore

7. Fill appropriate preposition in the blank:

The bread is made _____ wheat flour.

- A) of
- B) from
- C) in

D) on

8. Find the appropriate homonym for Altar.

- A) Alter
- B) Altor
- C) Altur
- D) Altair

9. A Simile is a

- A) Contrast
- B) Parallel
- C) Combination
- D) Comparison

10. Find the correct idiom.

- A) Better safe than sad
- B) Better safe than serious
- C) Better safe than sorry
- D) Better safe than regretful

11. A can do a piece of work in 80 days. He works at it for 10 days and then B alone finishes the remaining work in 42 days. In how much time will A and B working together, finish the work?

- A) 40 days
- B) 35 days
- C) 50 days
- D) 30 days

12. Choose the missing term out of the given alternatives Y, W, U, S, Q, ?, ?

- A) M, L
- B) J, R
- C) L, M
- D) O, M

13. In a certain language, PEN is written as QDM, then how BOOK will be written in that code?

- A) CMJN
- B) CNNJ
- C) CNLS
- D) NMJP

14. After deducting a commission of 5%, a T.V. set costs Rs.9595. Its marked price is

- A) Rs.10,000
- B) Rs.10,075
- C) Rs.10,100
- D) Rs.10,500

15. At what rate percent per annum will a sum of money double in 16 years?

- A) 6.25% p.a.
- B) 6.00% p.a.
- C) 6.75% p.a.
- D) 6.50% p.a.

16. In an exam two papers maths and chemistry, 60% of the students pass in maths and 70% pass in chemistry. What is minimum percentage of students who could have failed in both the subjects?

- A) 0%
- B) 30%
- C) 40%
- D) None of these

17. B, the son of A was married to C, whose sister D was married to E, the brother of B. How is D related to A?

- A) Sister
- B) Daughter-in-law
- C) Sister-in-law
- D) Cousin

18. Statements:

- I. The farmers have decided against selling their Kharif crops to the Government agencies.
- II. The Government has reduced the procurement price of Kharif crops starting from the last month to the next six months.

- A) Statement I is the cause and statement II is its effect
- B) Statement II is the cause and statement I is its effect
- C) Both the statements I and II are independent causes
- D) Both the statements I and II are effects of independent causes

19. Indiscreet is related to imprudent in the same way as Indisposed is related to

- A) Concerned
- B) Crucial
- C) Clear
- D) Reluctant

20. Rangaswamy Cup is associated with

- A) Archery
- B) Cricket
- C) Football
- D) Hockey

21. Who is the father of Geometry?

- A) Aristotle
- B) Euclid

- C) Pythagoras
- D) Kepler

22. Shivaji's war strategy used against the Mughals was

- A) Alert Army
- B) Political Supremacy
- C) Large Army
- D) Guerilla Warfare

23. Marginal utility, a consumer derives from a good, is

- A) Change in his total utility as a result of adding one unit to his stock of a good
- B) Utility derived from a particular good
- C) Change in utility derived as a result of a change in the price of a good
- D) Change in his total utility when he buys extra units of a good

24: Joint Military Exercise Nomadic Elephant 2017 is being held between India and

- A) Vietnam
- B) Mongolia
- C) Sri Lanka
- D) Thailand

25. $1014 \times 986 = ?$

- A) 998804
- B) 998814
- C) 998904
- D) 999804

PART-B

26. The solution of the differential equation $\frac{dy}{dx} = \frac{1-x}{y}$ represents a family of

- A) circle with centre at (1,0)
- B) circle with centre at (0, 0)
- C) circle with centre at (-1,0)
- D) straight line with slope -1

27. Suppose $\alpha = \lim_{(x,y) \rightarrow (0,0)} \frac{\sin(x^2+y^2)}{x^2+y^2}$; $\beta = \lim_{(x,y) \rightarrow (0,0)} \frac{x^2-y^2}{x^2+y^2}$ then which of the following statements is true?

- A) α exists but β does not exist
- B) α does not exist but β exists
- C) α, β do not exist
- D) both α, β exist

28. The set $U = \left\{x \in \mathbb{R} : \sin x = \frac{1}{2}\right\}$ is

- A) open
- B) closed
- C) both open and closed
- D) neither open nor closed

29. Let $\{a_n\}$ and $\{b_n\}$ be sequences of real numbers defined as $a_1 = 1$ and for $n \geq 1$, $a_{n+1} = a_n + (-1)^n 2^{-n}$, $b_n = \frac{2a_{n+1} - a_n}{a_n}$. Then

- A) $\{a_n\}$ converges to zero and $\{b_n\}$ is a Cauchy sequence
- B) $\{a_n\}$ converges to a non-zero number and $\{b_n\}$ is a Cauchy sequence
- C) $\{a_n\}$ converges to zero and $\{b_n\}$ is not a convergent sequence
- D) $\{a_n\}$ converges to a non-zero number and $\{b_n\}$ is not a convergent sequence

30. The matrix equation $AX = B$ has a unique non-zero solution if

- A) A is singular
- B) A is non-singular
- C) A is non-singular and B is not a null matrix
- D) A is non-singular and B is a null matrix

31. The sequence $\{(-1)^n\}_{n=1}^{\infty}$ is

- A) bounded and convergent
- B) convergent and unbounded
- C) bounded and divergent
- D) divergent and unbounded

32. If sequences of real numbers $\{a_n\}_{n=1}^{\infty}$, $\{b_n\}_{n=1}^{\infty}$ and $\{c_n\}_{n=1}^{\infty}$ are such that, $b_n = a_{2n}$ and $c_n = a_{2n+1}$, then $\{a_n\}_{n=1}^{\infty}$ is convergent implies

- A) $\{b_n\}_{n=1}^{\infty}$ is convergent but $\{c_n\}_{n=1}^{\infty}$ need not be convergent
- B) $\{c_n\}_{n=1}^{\infty}$ is convergent but $\{b_n\}_{n=1}^{\infty}$ need not be convergent
- C) both $\{b_n\}_{n=1}^{\infty}$ and $\{c_n\}_{n=1}^{\infty}$ are convergent
- D) both $\{b_n\}_{n=1}^{\infty}$ and $\{c_n\}_{n=1}^{\infty}$ are divergent

33. Consider the statements

- a. The series $\sum \sin \frac{1}{n}$ is convergent
- b. The series $\frac{1.2}{3^2.4^2} + \frac{3.4}{5^2.6^2} + \frac{5.6}{7^2.8^2} + \dots$ is convergent.

Then

- A) both the statements (a) and (b) are true
- B) (a) is true and (b) is false
- C) (a) is false and (b) is true
- D) neither (a) nor (b) is true

34. The series $x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots$ is convergent for

A) all real values of x

B) $|x| < 1$ only

C) $|x| < 1$

D) $-1 < x < 1$

35. $\lim_{n \rightarrow \infty} (2^n + 3^n)$ is equal to

A) 2

B) 3

C) 5

D) 6

36. The value of $\iiint xyz dx dy dz$ over the domain bounded by $x = 0, y = 0, z = 0, x + y + z = 1$ is

A) $\frac{1}{360}$

B) 360

C) $\frac{1}{720}$

D) 720

37. The value of the integral $\int_{-1}^1 \frac{|x|}{x} dx$ is equal to

A) 2

B) 1

C) $\frac{1}{2}$

D) 0

38. The integral $\int_0^\pi x F(\sin x) dx$ is equal to

A) $\frac{\pi}{4} \int_0^\pi F(\sin x) dx$

B) $\frac{\pi}{2} \int_0^\pi F(\sin x) dx$

C) $\pi \int_0^\pi F(\sin x) dx$

D) $\int_0^\pi F(\sin x) dx$

39. If G is a group and H is a subgroup of index 2 in G , then which of the following is a correct statement?

A) H is a normal subgroup of G

B) H is not a normal subgroup of G

C) H is a subgroup of G

D) None of these

40. If $a, b \in G$, where G is a group of order m , then order of ab and ba are

A) equal to m

B) same

- C) unequal
D) not defined

41. Which amongst the following statements is not true?

- A) A sequence cannot converge to more than one limit,
B) Every convergent sequence is bounded
C) Every bounded sequence is convergent
D) Limit of a convergent sequence is unique

42. If $u_n = \sqrt{n+1} - \sqrt{n}$ and $v_n = \sqrt{n^4+1} - n^2$, then

- A) $\sum_{n=1}^{\infty} u_n$ converges but $\sum_{n=1}^{\infty} v_n$ diverges
B) $\sum_{n=1}^{\infty} u_n$ diverges but $\sum_{n=1}^{\infty} v_n$ converges
C) $\sum_{n=1}^{\infty} u_n$ and $\sum_{n=1}^{\infty} v_n$ both converges
D) $\sum_{n=1}^{\infty} u_n$ and $\sum_{n=1}^{\infty} v_n$ both diverges

43. The sequence $a_n = \frac{1}{n^2} + \frac{1}{(n+1)^2} + \dots + \frac{1}{(2n)^2}$

- A) converges to 0
B) converges to $\frac{1}{2}$
C) converges to $\frac{1}{4}$
D) does not converge

44. Let $a_n = \sin \frac{1}{n^2}$, $n = 1, 2, \dots$, then

- A) $\lim_{n \rightarrow \infty} a_n = 1$
B) $\sum_{n=1}^{\infty} a_n$ converges
C) $\limsup_{n \rightarrow \infty} a_n \neq \liminf_{n \rightarrow \infty} a_n$
D) $\sum_{n=1}^{\infty} a_n$ diverges

45. The derivative of a periodic function with period t is

- A) a constant function
B) a periodic function with period t
C) a non-periodic function
D) none of the above

46. Let A and B be any $n \times n$ real matrices, then which of the following statements is true?

- A) $\text{rank}(A + B) = \text{rank}(A) + \text{rank}(B)$
B) $\text{rank}(A + B) \leq \text{rank}(A) + \text{rank}(B)$
C) $\text{rank}(A + B) = \text{rank}(A) \cdot \text{rank}(B)$
D) $\text{rank}(A + B) \geq \text{rank}(A) + \text{rank}(B)$

47. If $E = \{e^{2x}, e^{3x}\}$, $x \in \mathbb{R}$ then the set E is

- A) linearly independent over \mathbb{R}

- B) linearly dependent over \mathbb{R}
 C) linearly independent over any interval (a, b) , only when 0 does not belong to (a, b)
 D) none of the above

48. Which one of the following statements is correct?

- A) There is no vector space of dimension 1
 B) Any three vectors of a vector space of dimension 3 are linearly independent
 C) There is one and only one basis of a vector space of finite dimension
 D) If a non-zero vector space V is generated by a finite set S , then V can be generated by a linearly independent subset of S

49. If $V_1 = (1, 2, 0, 3, 0)$, $V_2 = (1, 2, -1, -1, 0)$, $V_3 = (0, 0, 1, 4, 0)$, $V_4 = (2, 4, 1, 0, 1)$ and $V_5 = (0, 0, 0, 0, 1)$, then the dimension of the linear span of $\{V_1, V_2, V_3, V_4, V_5\}$ is

- A) 2
 B) 3
 C) 4
 D) 5

50. The dimension of the vector space $V = \{A = (a_{ij})_{m \times n} : a_{ij} \in \mathbb{C}, a_{ij} = -a_{ij}\}$ is

- A) n^2
 B) $n^2 - 1$
 C) $\frac{n^2 - n}{2}$
 D) $\frac{n^2}{2}$

51. Using Rolle's theorem, the equation $a_0x^n + a_1x^{n-1} + \dots + a_n = 0$ has at least one root between 0 and 1, if

- A) $\frac{a_0}{n} + \frac{a_1}{n-1} + \dots + a_{n-1} = 0$
 B) $\frac{a_0}{n-1} + \frac{a_1}{n-2} + \dots + a_{n-2} = 0$
 C) $\frac{a_0}{n+1} + \frac{a_1}{n} + \dots + a_n = 0$
 D) $na_0 + (n-1)a_1 + \dots + a_{n-1} = 0$

52. $\lim_{x \rightarrow 0} \frac{(1+x)^{\frac{1}{2}} - e + \frac{1}{2}ex}{x^2}$ is equal to

- A) $\frac{24}{11}e$
 B) $\frac{11}{24}e$
 C) $\frac{1}{11}e$
 D) $\frac{1}{24}e$

53. A monotonic function

- A) is always continuous

- B) is continuous only, if it satisfies intermediate value property
 C) can be nowhere continuous
 D) can be discontinuous at infinitely many points

54. The set of points where $f(x) = |\sin x|$ is not differentiable is

- A) empty
 B) $\{0\}$
 C) $\{k\pi; k \in \mathbb{Z}\}$
 D) $\{\frac{k\pi}{2}; k \in \mathbb{Z}\}$

55. Let $P_n(x)$ be a Taylor's polynomial of degree $n \geq 0$ for the function e^x about 0. Then, the error in this approximation is

- (A) $\frac{x^n}{n!} e^t$ for some $t, 0 < t < x$
 B) $\frac{x^n}{(n+1)!} e^t$ for some $t, 0 < t < x$
 C) $\frac{x^{n+1}}{n!} e^t$ for some $t, 0 < t < x$
 D) $\frac{x^{n+1}}{(n+1)!} e^t$ for some $t, 0 < t < x$

56. Consider the matrix $M = \begin{bmatrix} 0 & 1 & 2 & 0 \\ 1 & 0 & 1 & 0 \\ 2 & 1 & 0 & 2 \\ 0 & 0 & 2 & 0 \end{bmatrix}$ then

- A) M has no real eigen values
 B) All real eigen values of M are positive
 C) All real eigen values of M are negative
 D) M has both positive and negative real eigen values

57. If the nullity of the matrix $\begin{bmatrix} k & 1 & 2 \\ 1 & -1 & -2 \\ 1 & 1 & 4 \end{bmatrix}$ is 1, then the value of k is

- A) -1
 B) 0
 C) 1
 D) 2

58. Let $M = \begin{bmatrix} 4 & 2 & 1 & 3 \\ 6 & 3 & 4 & 7 \\ 2 & 1 & 0 & 1 \end{bmatrix}$ then the rank of M is

- A) 4
 B) 3
 C) 2
 D) 1

59. Following system of linear equations

$$x + 4y + 3z = 0$$

$$x + 3y + 4z = 0$$

$$x + 2y + 5z = 0 \text{ does have}$$

A) no solution

B) infinitely many solutions

C) more than one but finitely many solutions

D) exactly one solution

60. Let A be a 3×3 complex matrix, whose characteristic polynomial is given by

$$f(t) = t^3 + c_2 t^2 + c_1 t + c_0, \text{ then}$$

A) $\det(A) = c_2$

B) $\det(A) = c_0$

C) $\det(A) = -c_2$

D) $\det(A) = -c_0$

61. For the function $f: \mathbb{R}^2 \rightarrow \mathbb{R}$ defined by $f(x, y) = x^3 + y^3 - 3x - 12y + 20$, which of the following is true?

A) f has maximum at $(1, 2)$

B) f has minimum at $(-1, -2)$

C) f has maximum at $(1, 2)$ and minimum at $(-1, -2)$

D) The saddle points of f are $(-1, 2)$ and $(1, -2)$

62. $\int \sqrt{1 + 2 \tan x (\tan x + \sec x)} dx$ is equal to

A) $-\log(1 + \sin x) + c$

B) $\log(1 - \sin x) + c$

C) $-\log(1 - \sin x) + c$

D) $\log(1 + \sin x) + c$

63. The value of $\int_0^\infty \log\left(x + \frac{1}{x}\right) \frac{dx}{1+x^2}$ is

A) 0

B) ∞

C) $\log 2$

D) $\pi \log 2$

64. If $I_n = \int_0^{\pi/4} \tan^n x dx$ then

A) $I_n - I_{n-2} = \frac{1}{n-1}$

B) $I_n + I_{n+2} = \frac{1}{n-1}$

C) $I_n + I_{n-2} = \frac{1}{n}$

D) $I_n - I_{n-2} = \frac{1}{n-2}$

65. If $E = \{(x, y) \in \mathbb{R}^2 : 0 \leq x \leq 1, 0 \leq y \leq x\}$, then the value of $\iint_B (x + y) dx dy$ is equal to

- A) -1
- B) 0
- C) 1
- D) 1/2

66. If $f(x) = (x + |x|) |x|$, for all $x \in \mathbb{R}$, then which of the following is incorrect?

- A) f is continuous
- B) f is not differentiable for some x
- C) f' is continuous
- D) f' is differentiable

67. The Maclaurin's expansion of $\tan x$ in powers of x is valid in the interval

- A) $(-\infty, \infty)$
- B) $\left(-\frac{3\pi}{2}, \frac{3\pi}{2}\right)$
- C) $(-\pi, \pi)$
- D) $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$

68. Consider the function $f: \mathbb{R}^2 \rightarrow \mathbb{R}$ of two variables defined by

$$f(x, y) = \begin{cases} \frac{xy}{x^2 + y^2}, & x^2 + y^2 \neq 0 \\ 0, & x^2 + y^2 = 0 \end{cases}$$

Determine which one of the following facts about f is true.

- A) f is continuous at $(0, 0)$
- B) f has removable discontinuity at $(0, 0)$
- C) f is not differentiable at $(0, 0)$
- D) none of the above

69. If $f: \mathbb{R}^2 \rightarrow \mathbb{R}$ be defined by $f(x, y) = x^2 + y^2$ if x and y are rational
0 otherwise

then which of the following statements is true?

- A) f is not continuous at $(0, 0)$
- B) f is continuous at $(0, 0)$ but not differentiable at $(0, 0)$
- C) f is differentiable only at $(0, 0)$
- D) f is differentiable everywhere

70. Consider the function $f: \mathbb{R}^2 \rightarrow \mathbb{R}$ defined by $f(x, y) = x^y$. Determine which of the following is true for f .

- A) $f_x(a, 0) = 0$ for any constant a
- B) $f_y(e, 0) = 0$
- C) $f_{xy}(1, 0) = 0$
- D) $f_{yx}(1, 1) = 1$

71. The number of elements of order 5 in a symmetric group S_5 is

- A) 5
- B) 20
- C) 24
- D) 12

72. The set M of square matrices (of same order) with respect to matrix multiplication is

- A) group
- B) semi-group
- C) monoid
- D) rank

73. The number of generators in a cyclic group of order 10 are

- A) 1
- B) 2
- C) 3
- D) 4

74. The dimension of the vector space of all 3×3 real symmetric matrices is

- A) 3
- B) 4
- C) 6
- D) 9

75. If U is a 3×3 complex Hermitian matrix, which is unitary, then the distinct eigen values of U are

- A) $i, -i$
- B) $1 + i, 1 - i$
- C) $1, -1$
- D) $\frac{1+i}{2}, \frac{1-i}{2}$

76. If E is a connected subset of R with atleast two elements, then the number of elements in E is

- A) exactly two
- B) more than two but finite
- C) countably infinite
- D) uncountable

77. Define $f: R^2 \rightarrow R$ by $f(x, y) = 1$ if $xy = 0$
2 otherwise.

If $S = \{(x, y): f \text{ is continuous at the point } (x, y)\}$, then

- A) S is open
- B) $S = \varphi$

- C) S is connected
 D) S is closed

78. Let Q be the set of rational numbers and E be the set of all rationals p , such that $2 < p^2 < 3$, then E is

- A) closed and bounded in Q
 B) closed and unbounded in Q
 C) not compact in Q
 D) compact in Q

79. Consider the following subsets of \mathbb{R}

$$E = \left\{ \frac{n}{n+1} : n \in \mathbb{N} \right\}, F = \left\{ \frac{n}{x+1} : 0 \leq x \leq 1 \right\}, \text{ then}$$

- A) Both E and F are closed
 B) E is closed and F is not closed
 C) E is not closed and F is closed
 D) Neither E nor F is closed

80. If G is a cyclic group of order 8, then the order of the group of automorphisms of G is

- A) 2
 B) 4
 C) 6
 D) 8

81. $\int_0^{\pi/2} \frac{\sin^{3/2} x}{\sin^{3/2} x + \cos^{3/2} x} dx$ is equal to

- A) 0
 B) 1
 C) $\pi/4$
 D) $\pi/2$

82. The entire length of the curve whose equation is $x^{2/3} + y^{2/3} = r^{2/3}$ is equal to

- A) $\frac{3}{2}r$
 B) $2\sqrt{3}$
 C) $6r$
 D) none of these

83. The value of $\int_0^\infty \int_{1/y}^\infty x^4 e^{-x^3 y} dx dy$ is equal to

- A) $1/4$
 B) $1/3$
 C) $1/2$
 D) 1

84. Which of the following is not an integrating factor of the differential equation $dy - y dx = 0$?

- A) $\frac{1}{x^2}$

- B) $\frac{1}{x^2+y^2}$
 C) $\frac{1}{xy}$
 D) $\frac{x}{y}$

85. The orthogonal trajectory to the family of circles $x^2 + y^2 = 2cx$ (c arbitrary) is described by the differential equation

- A) $(x^2 + y^2)y' = 2xy$
 B) $(x^2 - y^2)y' = 2xy$
 C) $(y^2 - x^2)y' = xy$
 D) $(y^2 - x^2)y' = 2xy$

86. The maximum magnitude of the directional derivative for the surface $x^2 + xy + yz = 9$ at the point $(1, 2, 3)$ is along the direction

- A) $i + j + k$
 B) $2i + 2j + k$
 C) $i + 2j + 3k$
 D) $i - 2j + 3k$

87. If \vec{F} is such that $\nabla \times \vec{F} = 0$, then \vec{F} is called

- A) rotational
 B) irrotational
 C) solenoidal
 D) rotational and solenoidal

88. From the following, what is the value of $\int_C \vec{F} \cdot d\vec{r}$, where $\vec{F} = 2x^2y\hat{i} + 3xy\hat{j}$ and C is $y = 4x^2$ in the plane from $(0,0)$ to $(1, 4)$?

- A) $\frac{104}{9}$
 B) $\frac{104}{7}$
 C) $\frac{104}{3}$
 D) $\frac{104}{5}$

89. What from the following is the directional derivative of $\phi = 5x^2y - 5y^2z + 2.5z^2x$ at the point $(1, 1, 1)$ in the direction of the line $\frac{x-1}{2} = \frac{y-3}{-2} = z$?

- A) $\frac{11}{3}$
 B) $\frac{11}{2}$
 C) $11\frac{2}{3}$
 D) $\frac{2}{3}$

90. If x, y and z are positive real numbers, then the minimum value of $x^2 + 8y^2 + 27z^2$, where $\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 1$ is

- A) 108
- B) 216
- C) 405
- D) 1048

91. Which one of the following differential equations represent all circles with radius a ?

- A) $1 + \left(\frac{dy}{dx}\right)^2 + \sqrt{a^2 + x^2} \frac{d^2y}{dx^2} = 0$
- B) $1 + \left(\frac{dy}{dx}\right)^2 + \sqrt{a^2 + y^2} \frac{d^2y}{dx^2} = 0$
- C) $\left[1 + \left(\frac{dy}{dx}\right)^2\right]^3 + a^2 \left(\frac{d^2y}{dx^2}\right)^2 = 0$
- D) $\left[1 + \left(\frac{dy}{dx}\right)^2\right]^3 - a^2 \left(\frac{d^2y}{dx^2}\right)^2 = 0$

92. The solution $y(x)$ of the differential equation $(D^2 + 4D + 4)y = 0$ satisfying the conditions $y(0) = 4, y'(0) = 8$ is

- A) $4e^{2x}$
- B) $(16x + 4)e^{-2x}$
- C) $4e^{-2x} + 16x$
- D) $4e^{-2x} + 16x4e^{2x}$

93. An integrating factor for the differential equation $(\cos y \sin 2x)dx + (\cos^2 y - \cos^2 x)dy = 0$ is

- A) $\sec^2 y + \sec y \tan y$
- B) $\tan^2 y + \sec y \tan y$
- C) $\frac{1}{\sec^2 y + \sec y \tan y}$
- D) $\frac{1}{\tan^2 y + \sec y \tan y}$

94. If c is an arbitrary constant, then the general solution of the differential equation $\frac{dy}{dx} - \tan x \tan y = \cos x \sec y$ is

- A) $2 \sin y = (x + c - \sin x \cos x) \sec x$
- B) $\cos y = (x + c) \sin x$
- C) $\sec y = (x + c) \cos x$
- D) $\sin y = (x + c) \cos x$

95. The maximum value of $f(x, y, z) = xyz$ along all points lying on the intersection of the planes $x + y + z = 40$ and $z = x + y$ is

- A) 4000
- B) 3000
- C) 2000

D) 1000

96. The differential equation $\frac{dy}{dx} = k(a-y)(b-y)$ when solved with the condition $y(0) = 0$, fields the result

A) $\frac{b(a-y)}{a(b-y)} = e^{(a-b)kx}$

B) $\frac{b(a-x)}{a(b-x)} = e^{(a-b)ky}$

C) $\frac{a(b-y)}{b(a-y)} = e^{(a-b)kx}$

D) $xy = ke$

97. Solving by variation of parameter the differential equation $y'' - 2y' + y' = e^x \log_x$ the value of Wronskian W is

A) e^{2x}

B) 2

C) e^{-2x}

D) e

98. The differential equation $2y dx - (3y - 2x)dy = 0$

A) exact and homogeneous but not linear

B) homogeneous and linear but not exact

C) exact and linear but not homogeneous

D) exact, homogeneous and linear

99. The differential equation $(axy^3 + y \cos x)dx + (x^2y^2 + \beta \sin x) dy = 0$ is exact for the values of α and β such that

A) $\alpha = \frac{3}{2}, \beta = 1$

B) $\alpha = 1, \beta = \frac{3}{2}$

C) $\alpha = \frac{2}{3}, \beta = 1$

D) $\alpha = 1, \beta = \frac{2}{3}$

100. The particular solution of the equation $y' \sin x = y \log$ satisfying the initial condition $y(\pi/2) = e$, is

A) $e^{\tan(x/2)}$

B) $e^{\cot(x/2)}$

C) $\log \tan(x/2)$

D) $\log \cot(x/2)$

Answer Key				
Q.No./Ans	Q.No./Ans	Q.No./Ans	Q.No./Ans	Q.No./Ans
1 B	21 B	41 C	61 D	81 C
2 C	22 D	42 B	62 C	82 C
3 B	23 A	43 A	63 D	83 C
4 A	24 B	44 B	64 *	84 D
5 C	25 D	45 B	65 D	85 B
6 C	26 A	46 B	66 D	86 B
7 B	27 A	47 C	67 D	87 B
8 A	28 B	48 D	68 C	88 D
9 D	29 B	49 B	69 B	89 C
10 C	30 C	50 C	70 A or D	90 B
11 D	31 C	51 C	71 C	91 D
12 D	32 C	52 *	72 B or C	92 B
13 B	33 C	53 B	73 D	93 A
14 C	34 D	54 C	74 C	94 D
15 A	35 *	55 A	75 C	95 C
16 A	36 C	56 D	76 D	96 A
17 B	37 D	57 A	77 A	97 A
18 B	38 B	58 C	78 D	98 D
19 D	39 A	59 B	79 D	99 C
20 D	40 B	60 D	80 B	100 A

