

LINEAR SIMULTANEOUS EQUATIONS

Task 1 – Solve the simultaneous equations. Do not use trial and improvement.

1) $x + 5y = 23$
 $x + 3y = 15$

$$\begin{array}{r} x + 5y = 23 \\ -(x + 3y = 15) \\ \hline 2y = 8 \\ y = 4 \end{array}$$

$$\begin{array}{l} x + 5(4) = 23 \\ x + 20 = 23 \\ x = 3 \end{array}$$

$x = 3, y = 4$

2) $2x + 3y = 7$
 $2x + y = 5$

$$\begin{array}{r} 2x + 3y = 7 \\ -(2x + y = 5) \\ \hline 2y = 2 \\ y = 1 \end{array}$$

$$\begin{array}{l} 2x + 3(1) = 7 \\ 2x + 3 = 7 \\ 2x = 4 \\ x = 2 \end{array}$$

$x = 2, y = 1$

3) $5x + 3y = 23$
 $2x + 3y = 20$

$$\begin{array}{r} 5x + 3y = 23 \\ -(2x + 3y = 20) \\ \hline 3x = 3 \\ x = 1 \end{array}$$

$$\begin{array}{l} 5(1) + 3y = 23 \\ 5 + 3y = 23 \\ 3y = 18 \\ y = 6 \end{array}$$

$x = 1, y = 6$

4) $8x - y = 20$
 $7x + y = 10$

$$\begin{array}{r} 8x - y = 20 \\ +(7x + y = 10) \\ \hline 15x = 30 \\ x = 2 \end{array}$$

$$\begin{array}{l} 8(2) - y = 20 \\ 16 - y = 20 \\ -y = 4 \\ y = -4 \end{array}$$

$x = 2, y = -4$

5) $4x - 8y = 0$
 $4x + 10y = -9$

$$\begin{array}{r} 4x - 8y = 0 \\ -(4x + 10y = -9) \\ \hline -18y = 9 \\ y = -\frac{9}{18} = -\frac{1}{2} \end{array}$$

$$\begin{array}{l} 4x - 8\left(-\frac{1}{2}\right) = 0 \\ 4x + 4 = 0 \\ 4x = -4 \\ x = -1 \end{array}$$

$x = -1, y = -\frac{1}{2}$

Task 2 – Solve the simultaneous equations. Do not use trial and improvement.

6) $4x + 5y = 40$
 $2x + 2y = 18 \quad \times 2$

$$\begin{array}{r} 4x + 5y = 40 \\ -(4x + 4y = 36) \\ \hline y = 4 \end{array}$$

$$\begin{array}{l} 4x + 5(4) = 40 \\ 4x + 20 = 40 \\ 4x = 20 \\ x = 5 \end{array}$$

$x = 5, y = 4$

7) $6x - 7y = 22$
 $3x + 5y = 28 \quad \times 2$

$$\begin{array}{r} 6x - 7y = 22 \\ -(6x + 10y = 56) \\ \hline -17y = -34 \\ y = \frac{-34}{-17} = 2 \end{array}$$

$$\begin{array}{l} 6x - 7(2) = 22 \\ 6x - 14 = 22 \\ 6x = 36 \\ x = 6 \end{array}$$

$x = 6, y = 2$

8) $3x + 8y = 104 \quad \times 2$
 $2x - 6y = -44 \quad \times 3$

$$\begin{array}{r} 6x + 16y = 208 \\ -(6x - 18y = -132) \\ \hline 34y = 340 \\ y = 10 \end{array}$$

$$\begin{array}{l} 3x + 8(10) = 104 \\ 3x + 80 = 104 \\ 3x = 24 \\ x = 8 \end{array}$$

$x = 8, y = 10$

9) $5x - 3y = -3 \quad \times 2$
 $2x + 6y = 42$

$$\begin{array}{r} 10x - 6y = -6 \\ +(2x + 6y = 42) \\ \hline 12x = 36 \\ x = 3 \end{array}$$

$$\begin{array}{l} 5(3) - 3y = -3 \\ 15 - 3y = -3 \\ -3y = -18 \\ y = 6 \end{array}$$

$x = 3, y = 6$

10) $-5x - 9y = -26 \quad \times 3$
 $3x + 10y = 34 \quad \times 5$

$$\begin{array}{r} -15x - 27y = -78 \\ +(15x + 50y = 170) \\ \hline 23y = 92 \\ y = 4 \end{array}$$

$$\begin{array}{l} -5x - 9(4) = -26 \\ -5x - 36 = -26 \\ -5x = 10 \\ x = -2 \end{array}$$

$x = -2, y = 4$

11) $7x + 3y = -63 \quad \times 3$
 $8x + 9y = -111$

$$\begin{array}{r} 21x + 9y = -189 \\ -(8x + 9y = -111) \\ \hline 13x = -78 \\ x = -6 \end{array}$$

$$\begin{array}{l} 7(-6) + 3y = -63 \\ -42 + 3y = -63 \\ 3y = -21 \\ y = -7 \end{array}$$

$x = -6, y = -7$

$$\begin{aligned} 12) \quad 9x - 2y &= 13 & \times 4 \\ 6x + 8y &= 4 \end{aligned}$$

$$\begin{aligned} 36x - 8y &= 52 \\ + (6x + 8y &= 4) \\ \hline 42x &= 56 \\ x &= \frac{56}{42} = \frac{4}{3} \end{aligned}$$

$$9\left(\frac{4}{3}\right) - 2y = 13$$

$$12 - 2y = 13$$

$$-2y = 1$$

$$y = -\frac{1}{2}$$

$$x = \frac{4}{3}, y = -\frac{1}{2}$$

Task 3

- 13) At the cinema, 2 adult tickets and 1 child ticket cost £25. 1 adult ticket and 3 child tickets cost £27.

Work out the price of one adult ticket.

Work out the price of one child ticket.

Do not use trial and improvement.

$$\begin{aligned} \text{Adult ticket} &= x \\ \text{Child ticket} &= y \end{aligned}$$

$$\begin{aligned} 2x + y &= 25 & \times 3 \\ x + 3y &= 27 \end{aligned}$$

$$\begin{aligned} 6x + 3y &= 75 \\ - (x + 3y &= 27) \\ \hline 5x &= 48 \\ x &= 9.60 \end{aligned}$$

$$2(9.60) + y = 25$$

$$19.20 + y = 25$$

$$y = 5.80$$

One adult ticket costs £9.60

One child ticket costs £5.80

- 14) In a café, 2 sandwiches and 3 drinks cost £17.75. 3 sandwiches and 2 drinks cost £21. Work out the cost of one sandwich. Work out the cost of one drink. Do not use trial and improvement.

$$\begin{aligned} \text{Sandwich} &= x \\ \text{Drink} &= y \end{aligned}$$

$$\begin{aligned} 2x + 3y &= 17.75 & \times 3 \\ 3x + 2y &= 21 & \times 2 \end{aligned}$$

$$\begin{aligned} 6x + 9y &= 53.25 \\ - (6x + 4y &= 42) \\ \hline 5y &= 11.25 \\ y &= 2.25 \end{aligned}$$

$$2x + 3(2.25) = 17.75$$

$$2x + 6.75 = 17.75$$

$$2x = 11$$

$$x = 5.50$$

One sandwich costs £5.50

One drink costs £2.25

Challenge

- 15) Solve the simultaneous equations

$$\begin{aligned} 3x + 4y - 18 &= 0 \\ y &= 2x + 8 \end{aligned}$$

$$\begin{aligned} 3x + 4y &= 18 \\ 2x - y &= -8 & \times 4 \end{aligned}$$

$$\begin{aligned} 3x + 4y &= 18 \\ + (8x - 4y &= -32) \\ \hline 11x &= -14 \\ x &= -\frac{14}{11} \end{aligned}$$

$$3\left(-\frac{14}{11}\right) + 4y = 18$$

$$-\frac{42}{11} + 4y = 18$$

$$4y = \frac{240}{11}$$

$$y = \frac{60}{11}$$

$$x = -\frac{14}{11}, y = \frac{60}{11}$$

16) Solve the simultaneous equations

$$2x = 8 - 7y$$

$$\frac{y}{2} + 10 - x = 2$$

$$2x + 7y = 8$$

$$-x + \frac{y}{2} = -8 \quad \times 2$$

$$\begin{array}{r} 2x + 7y = 8 \\ +(-2x + y = -16) \\ \hline 8y = -8 \\ y = -1 \end{array}$$

$$2x + 7(-1) = 8$$

$$2x - 7 = 8$$

$$2x = 15$$

$$x = \frac{15}{2}$$

$$x = \frac{15}{2}, \quad y = -1$$

17) Solve the simultaneous equations

$$x + y + z = 4.5$$

$$2x + 2y = 4$$

$$2z = x$$

$$x = 2z$$

Substitute into first two equations:

$$2z + y + z = 4.5$$

$$y + 3z = 4.5 \quad \times 2$$

$$2(2z) + 2y = 4$$

$$2y + 4z = 4$$

$$\begin{array}{r} 2y + 6z = 9 \\ -(2y + 4z = 4) \\ \hline 2z = 5 \\ z = 2.5 \end{array}$$

$$2(2.5) = x$$

$$x = 5$$

$$5 + y + 2.5 = 4.5$$

$$y + 7.5 = 4.5$$

$$y = -3$$

$$x = 5, y = -3, z = 2.5$$

18) A basket contains apples and oranges. The total number of fruits is 50. There are 12 more apples than oranges. Work out the number of apples and oranges. Do not use trial and improvement.

$$\begin{array}{l} \text{Apples} = x \\ \text{Oranges} = y \end{array}$$

$$x + y = 50$$

$$x + x - 12 = 50$$

$$2x - 12 = 50$$

$$2x = 62$$

$$x = 31$$

$$31 + y = 50$$

$$y = 19$$

31 apples and 19 oranges