ALGEBRAIC BOUND CALCULATIONS

1) Given that

$$Y = c(d + e)$$

where,

c = 6.8 correct to 1 decimal place

d = 4 correct to 1 significant figure

e = 30 correct to the nearest 5

Work out the lower bound for the value of *Y*.

$$Y_{lower} = C_{lower}(d_{lower} + e_{lower})$$

= 6.75(3.5 + 27.5)
= **209.25**

2) Given that

$$N = \frac{g-h}{2}$$

where,

g = 5.6 correct to 2 significant figures

h = 0.4 correct to 1 decimal place

Work out the upper bound for the value of N.

$$N_{upper} = \frac{g_{upper} - h_{lower}}{2}$$
$$= \frac{5.65 - 0.35}{2}$$

= 2.65

3) Given that

$$X = k - 2l$$

where,

k = 20.34 correct to 2 decimal places

l = 3 correct to the nearest unit

Work out the lower bound for the value of *X*.

$$X_{lower} = k_{lower} - 2(l_{upper})$$

= 20.335 - 2(3.5)
= **13.335**

4) Given that

$$Z = \frac{2t-u}{v}$$

where,

t = 7.8 correct to 1 decimal place

u = 3.50 correct to 2 decimal places

v = 2 correct to one significant figure

Work out the upper bound for the value of Z. Give your answer to 2 decimal places.

$$Z_{upper} = \frac{2(t_{upper}) - u_{lower}}{v_{lower}}$$
$$= \frac{2(7.85) - 3.495}{1.5}$$
$$= 8.136 \dots$$
$$= 8.14 (2 dp)$$

5) Given that

$$C = x^2 + \frac{y}{z}$$

where,

x = 4.3 correct to 1 decimal place

y = 25.6 correct to 3 significant figures

z = 5 correct to the nearest unit

Work out the upper bound for the value of C.

$$C_{upper} = (x_{upper})^2 + \frac{y_{upper}}{z_{lower}}$$
$$= (4.35)^2 + \frac{25.65}{4.5}$$
$$= 24.6225$$

6) Given that
$$R = \frac{j}{m-n}$$

 $j = 42$ correct to 2 significant figures
 $m = 3.10$ correct to 2 decimal places
 $n = 0.4$ correct to 1 significant figure

Work out the lower bound for the value of R. Give your answer to 3 significant figures.

$$R_{lower} = rac{j_{lower}}{m_{upper} - n_{lower}}$$

$$= rac{41.5}{3.105 - 0.35}$$

$$= 15.0635 \dots$$

$$= 15.1 (3 sf)$$

7) Given that
$$T = a\left(b + \frac{c^3}{2}\right)$$

 $a = 5.4$ correct to 1 decimal place
 $b = 30$ correct to 2 significant figures
 $c = 1.45$ correct to 2 decimal places

Work out the upper bound of *T*. Give your answer to 2 decimal places.

$$T_{upper} = a_{upper} \left(b_{upper} + \frac{(c_{upper})^3}{2} \right)$$

$$= 5.45 \left(30.5 + \frac{1.455^3}{2} \right)$$

$$= 174.618 \dots$$

$$= 174.62 (2 dp)$$

8) Given that
$$D = a - \frac{b}{c}$$

 $a = 6.45$ correct to 2 decimal places
 $b = 1.9$ correct to 1 decimal place
 $c = 9$ correct to the nearest 5

Work out the upper bound of *D*. Give your answer to 2 decimal places.

$$D_{upper} = a_{upper} - \frac{b_{lower}}{c_{upper}}$$

$$= 6.455 - \frac{1.85}{11.5}$$

$$= 6.294 \dots$$

$$= 6.29 (2 dp)$$