

# RATIOS AS LINEAR FUNCTIONS

## Task 1

1) The ratio of blue to red counters is 2 : 3. What fraction of the counters are blue?

$$\text{Total parts} = 2 + 3 = 5$$

$$\frac{2}{5}$$

2) The ratio of red to orange sweets is 3 : 7. What fraction of the sweets are orange?

$$\text{Total parts} = 3 + 7 = 10$$

$$\frac{7}{10}$$

3) A paint mixes yellow and blue in the ratio 4 : 1. What fraction of the paint is yellow?

$$\text{Total parts} = 4 + 1 = 5$$

$$\frac{4}{5}$$

4) In a cinema the ratio of adults to children is 1 : 6. What fraction of the people are adults?

$$\text{Total parts} = 1 + 6 = 7$$

$$\frac{1}{7}$$

5) The ratio of right-handed to left-handed pupils in a class is 7 : 2. What percentage of the pupils are left-handed? Give your answer to the nearest percentage.

$$\text{Total parts} = 7 + 2 = 9$$

$$\frac{2}{9} = 22\%$$

6) A bag has red, green and yellow counters in the ratio 9 : 4 : 7. What percentage of the counters are green?

$$\text{Total parts} = 9 + 4 + 7 = 20$$

$$\frac{4}{20} = 20\%$$

7) At a school, pupils take Spanish, French and German in the ratio 5 : 9 : 4. What fraction of the pupils do not study Spanish?

$$\text{Total parts} = 5 + 9 + 4 = 18$$

$$\frac{13}{18}$$

8) A bag contains red and blue counters.  $\frac{3}{8}$  of the counters are red. Write the ratio of red to blue counters.

$$3 : 5$$

9) A drink is made with 30% syrup, and the rest is sparkling water. Write the ratio of syrup to sparkling water in the drink. Give your answer in simplest form.

$$30 : 70$$

$$3 : 7$$

10) The ratio A : B is 2 : 5. What fraction of the ratio represents A?

$$\text{Total parts} = 2 + 5 = 7$$

$$\frac{2}{7}$$

11) In a sale  $\frac{2}{3}$  of the items in a store are marked down. Write the ratio of the items marked down, to the items that are full priced.

$$2 : 1$$

12) In a jewellery store,  $\frac{4}{11}$  of the jewellery is silver and the rest of the jewellery is gold. Write the ratio of gold jewellery to silver jewellery.

$$7 : 4$$

13) At a concert the number of adults to children is in the ratio 5 : 2. The children are all either under 10 or over 10. The ratio of children under 10 to children over 10 is 3 : 4. What fraction of all the people at the concert are children under 10?

Fraction of children:

$$\frac{2}{7}$$

Fraction of children under 10:

$$\frac{2}{7} \times \frac{3}{7} = \frac{6}{49}$$

14) On a coach the ratio of teachers to students is 1 : 12. All the students study either science or history. The ratio of science students to history students is 5 : 7. What fraction of all the people on the coach are history students? Give your answer in simplest form.

Fraction of students:

$$\frac{12}{13}$$

Fraction of history students:

$$\frac{12}{13} \times \frac{7}{12} = \frac{84}{156} = \frac{7}{13}$$

15) In a park the ratio of adults to children is 4 : 1. The children are all either playing football or playing basketball. The ratio of football players to basketball players is 2 : 3. What percentage of all the people in the park are basketball players?

Fraction of children:

$$\frac{1}{5}$$

Fraction of children that play basketball:

$$\frac{1}{5} \times \frac{3}{5} = \frac{3}{25} = 12\%$$

16) In a university the ratio of national to international students is 7 : 3. 40% of the international students are studying engineering. What fraction of all the students in the university are international engineering students? Give your answer in simplest form.

Fraction of international students:

$$\frac{3}{10}$$

Fraction of international engineering students:

$$\frac{3}{10} \times \frac{4}{10} = \frac{12}{100} = \frac{3}{25}$$

## Task 2

17) Given that  $a : b = 2 : 3$  and  $b : c = 3 : 4$ , write the ratio  $a : b : c$ .

$$\begin{array}{l} a : b : c \\ 2 : 3 : 4 \end{array}$$

18) Given that  $p : q = 6 : 7$  and  $q : r = 5 : 9$ , write the ratio  $p : q : r$ .

$p : q$	$q : r$
$6 : 7$	$5 : 9$
$\times 5$	$\times 7$
$30 : 35$	$35 : 63$

$$\begin{array}{l} p : q : r \\ 30 : 35 : 63 \end{array}$$

19) Given that  $a : b = 3 : 5$  and  $b : c = 2 : 7$ , write the ratio  $a : b : c$ .

$a : b$	$b : c$
$3 : 5$	$2 : 7$
$\times 2$	$\times 5$
$6 : 10$	$10 : 35$
$a : b : c$	
$6 : 10 : 35$	

20) Given that  $x : y = 4 : 7$  and  $y : z = 3 : 8$ , write the ratio  $x : y : z$ .

$x : y$	$y : z$
$4 : 7$	$3 : 8$
$\times 3$	$\times 7$
$12 : 21$	$21 : 56$
$x : y : z$	
$12 : 21 : 56$	

21) Given that  $m : n = 1 : 6$  and  $m : p = 3 : 10$ , write the ratio  $n : p$ . Give your answer in simplest form.

$m : n$	$m : p$
$1 : 6$	$3 : 10$
$\times 3$	$\times 3$
$3 : 18$	
$n : p$	
$18 : 10$	
$9 : 5$	

22) The ratio of lions to tigers is 7 : 4.

The ratio of bears to lions is 5 : 2.

Find the ratio of tigers to bears.

$L : T$	$B : L$
$7 : 4$	$5 : 2$
$\times 2$	$\times 7$
$14 : 8$	$35 : 14$
$T : B$	
$8 : 35$	

23) Amir, Ben and Corey share £212. The ratio of Amir's share to Ben's share is 5 : 3. The ratio of Ben's share to Corey's share is 4 : 7. How much does Corey receive?

$A : B$	$B : C$
5 : 3	4 : 7
$\times 4$	$\times 3$
20 : 12	12 : 21

$$\begin{aligned} A : B : C \\ 20 : 12 : 21 \\ 20 + 12 + 21 = 53 \\ \text{£212} \div 53 = \text{£4} \end{aligned}$$

Corey receives:  
£4  $\times$  21 = £84

24) Given that  $m : p = 2 : 9$  and  $n : p = 5 : 6$ , write the ratio  $m : n : p$ .

$m : p$	$n : p$
2 : 9	5 : 6
$\times 2$	$\times 3$
4 : 18	15 : 18

$$\begin{aligned} m : n : p \\ 4 : 15 : 18 \end{aligned}$$

25) A survey is taken about vehicles in a car park. The results are expressed in the following ratios, as the numbers of:

$$\begin{aligned} \text{Cars} : \text{Motorbikes} &= 5 : 3 \\ \text{Cars} : \text{Vans} &= 10 : 1 \end{aligned}$$

If there were 187 vehicles recorded, how many vans were recorded?

$C : M$	$C : V$
5 : 3	10 : 1
$\times 2$	$\times 9$
10 : 6	

$$\begin{aligned} C : M : V \\ 10 : 6 : 1 \\ 10 + 6 + 1 = 17 \\ 187 \div 17 = 11 \end{aligned}$$

$$\begin{aligned} 10 : 6 : 1 \\ \times 11 \quad \times 11 \\ 110 : 66 : 11 \end{aligned}$$

11 vans were recorded.

### Task 3

26) In a fruit basket, there are apples, bananas and oranges. The ratio of apples to fruit that are not apples is 3 : 7. The ratio of bananas to fruit that are not bananas is 2 : 5. Work out the ratio of apples : bananas : oranges.

Make the total parts of the ratio the same  
(LCM is 70)

$a : n$	$b : n$
3 : 7	2 : 5
$\times 7$	$\times 10$
21 : 49	20 : 50

$$\begin{aligned} \text{Number of oranges:} \\ 70 - 21 - 20 = 29 \end{aligned}$$

$$\begin{aligned} a : b : o \\ 21 : 20 : 29 \end{aligned}$$

27) A customer feedback survey was given. Each review was positive, neutral or negative. The ratio of positive reviews to not positive reviews was 3 : 2. The ratio of negative reviews to not negative reviews was 2 : 7. Given there were fewer than 100 surveys given, work out the highest number of respondents that gave a negative review.

Make the total parts of the ratio the same  
(LCM is 45)

$P : O$	$N : O$
3 : 2	2 : 7
$\times 9$	$\times 5$
27 : 18	10 : 35

$$\begin{aligned} \text{Number of neutral reviews:} \\ 45 - 27 - 10 = 8 \end{aligned}$$

$$\begin{aligned} P : NU : N \\ 27 : 8 : 10 \\ 54 : 16 : 20 \text{ (90 parts)} \\ 20 \text{ respondents} \end{aligned}$$

28) The points A, B, C and D lie in order on a straight line, where

$$AB : BD = 4 : 7 \text{ and } AC : CD = 5 : 3.$$

Work out the ratio AB : BC : CD.

Make the total parts of the ratio the same  
(LCM is 88)

$AB : BD$	$AC : CD$
$4 : 7$	$5 : 3$
$\times 8$	$\times 11$
$32 : 56$	$55 : 33$

Length of BC:

$$88 - AB - CD$$

$$88 - 32 - 33 = 23$$

$AB : BC : CD$

$$32 : 23 : 33$$

29) The points A, B, C and D lie in order on a straight line, where

$$AB : BD = 2 : 9 \text{ and } AC : CD = 7 : 8.$$

Work out the ratio AB : BC : CD.

Make the total parts of the ratio the same  
(LCM is 165)

$AB : BD$	$AC : CD$
$2 : 9$	$7 : 8$
$\times 15$	$\times 11$
$30 : 135$	$77 : 88$

Length of BC:

$$165 - AB - CD$$

$$165 - 30 - 88 = 47$$

$AB : BC : CD$

$$30 : 47 : 88$$

#### Task 4

30) Given that,

$$A : B = 7 : 2 \text{ and } C : D = 3 : 8,$$

$$A + B = C + D,$$

Work out the ratio A : B : C : D.

Make total parts of the ratio the same  
(LCM is 99)

$A : B$	$C : D$
$7 : 2$	$3 : 8$
$\times 11$	$\times 9$
$77 : 22$	$27 : 72$

$$A : B : C : D \\ 77 : 22 : 27 : 72$$

31) A charity collects a bag of coins. The ratio of the number of 50p coins to the number of 20p coins is 3 : 2. The ratio of the number of 20p coins to the number of 10p coins is 5 : 4. If the total value of all the coins is £103.00, work out how many 50p coins there are.

Make the parts of the 20p coins the same:

$50p : 20p$	$20p : 10p$
$3 : 2$	$5 : 4$
$\times 5$	$\times 2$
$15 : 10$	$10 : 8$

$$50p : 20p : 10p$$

$$15 : 10 : 8$$

Work out the values of the ratio:

$$50p \text{ coins} \rightarrow 15 \text{ parts} \rightarrow 15 \times 50p = 750p$$

$$20p \text{ coins} \rightarrow 10 \text{ parts} \rightarrow 10 \times 20p = 200p$$

$$10p \text{ coins} \rightarrow 8 \text{ parts} \rightarrow 8 \times 10p = 80p$$

$$7.50 : 2 : 0.8$$

Share £103 in the ratio:

$$7.5 + 2 + 0.8 = 10.3$$

$$103 \div 10.3 = 10$$

Number of 50p coins:

$$15 \times 10 = 150$$

There are 150, 50p coins.