DIRECT AND INVERSE PROPORTIONS

4
CHAPTER

CONTENTS

➢ DIRECT VARIATION

Consider the following table which shows various numbers of books (each of same cost) denoted by x and the corresponding cost denoted by y.

x (No. of Books)	2	3	5	10	15
y (Cost in Rupees)	15	75	125	250	375

Here, we note that there is an increase in cost corresponding to the increase in the number of books. Hence, it is a case of direct variation.

In this case, if we compare the ratio of different number of books to the corresponding costs, then we have :

$$\frac{2}{50},\quad \frac{3}{75},\quad \frac{5}{125},\quad \frac{10}{250},\quad \frac{15}{375},$$

$$\downarrow\quad\downarrow\quad\downarrow\quad\downarrow\quad\downarrow$$

$$\text{or}\quad \frac{1}{25},\quad \frac{1}{25},\quad \frac{1}{25},\quad \frac{1}{25},\quad \frac{1}{25},$$

Thus is, each ratio reduces to $\frac{1}{25}$ which is constant. We may express is in a general form as:

$$\frac{x}{y} = k \text{ (constant)}$$

Thus, we conclude that,

When two quantities x and y vary such that the ratio $\frac{x}{y}$ remains constant and positive, then we say that x and y vary directly and the variation is called a Direct Variation.

In Mathematical language, it may be written as,

$$\frac{x}{y} = k$$

$$\text{or}\quad x = ky$$

Let us consider any two values of x, say x_1 and x_2 with their corresponding values of y as y_1 and y_2. We have

$$\text{and}\quad x_1 = ky_1$$

$$x_2 = ky_2$$

$$\therefore\quad \frac{x_1}{x_2} = \frac{ky_1}{ky_2}$$

or $\frac{x_1}{x_2} = \frac{y_1}{y_2}$, which helps us to find the value of any one of x_1, x_2, y_1 and y_2, when other three are known.

❖ EXAMPLES ❖

Ex.1 If the cost of 15 pens of the same value is ј 600, find the cost of -

(i) 20 pens

(ii) 3 pens.

Sol. Let us denote the required cost by x. Now, writing the like terms together, we have :

(i)

No. of Pens	Cost in rupees
15	600
20	x

Ratio of pens $= \frac{15}{20} = \frac{3}{4}$

Ratio of rupees $= \frac{600}{x}$

Since, more pens cost more money, so this is a case of direct variation.

Therefore, $\frac{3}{4} = \frac{600}{x}$

or $3 \times x = 600 \times 4$

or $x = \frac{600 \times 4}{3}$

or $x = 200 \times 4 = 800$

$\therefore$ The cost of 20 pens is ₹ 800.

(ii) Again, ratio of pens $= \frac{15}{3} = \frac{5}{1}$

ratio of rupees $= \frac{600}{x}$

$\therefore$ $\frac{5}{1} = \frac{600}{x}$

or $5 \times x = 600 \times 1$

or $x = \frac{600}{5} = 120$

$\therefore$ The cost of 3 pens is ₹ 120.

Ex.2 Reema types 540 words during half an hour. How many words would she type in 6 minutes ?

Sol. Suppose she types x words in 6 minutes. Then, the given information can be represented in the following tabular form :

Number of words	540	x
Time (in minutes)	30	6

Since in more time more words can be typed, it is case of direct variation.

$\therefore$ Ratio of number of words

= Ratio of number of minutes

$\Rightarrow \frac{540}{x} = \frac{30}{6} \Rightarrow x = \frac{6 \times 540}{30} \Rightarrow x = 108.$

Hence, she types 108 words in 6 minutes.

INVERSE VARIATION

Consider the following table showing various number of men and the corresponding number of days to complete the work.

x (No. of men)	40	20	10	8	5	1
y (No. of days)	1	2	4	5	8	40

Here, the number of men are denoted by x and the corresponding number of days by y.

In this case, when the number of men increases, the corresponding number of days decreases. But, by a careful observation, we find that the product of the corresponding number of men and days is always the same :

$40 \times 1 = 40$

$20 \times 2 = 40$

$10 \times 4 = 40$

$8 \times 5 = 40$

$5 \times 8 = 40$

$1 \times 40 = 40$

That is the product (40) is constant.

In general, it may be expressed as

$xy = k$(constant)

Let x_1 and x_2 be two values of x and their corresponding values of y be $y_1$and y_2.

Then, $x_1y_1 = k$ and $x_2y_2 = k$

$\therefore$ $\frac{x_1y_1}{x_2y_2} = \frac{k}{k} = 1$

or $x_1y_1 = x_2y_2$ or $\frac{x_1}{x_2} = \frac{y_2}{y_1}$

Hence, we conclude that, if two quantities x and y vary such that their product xy remains constant, then we say that x and y vary inversely and the variation is called inverse variation.

The relation $\frac{x_1}{x_2} = \frac{y_2}{y_1}$ is used to find the value of any one of x_1, x_2, y_1 and y_2, if the other three are known.

❖ EXAMPLES ❖

Ex.3 In a boarding house of 80 boys, there is food provisions for 30 days. If 20 more boys join the boarding house, how long will the provisions last ?

Sol. Obviously, more the boys the sooner would the provisions exhaust. It is, therefore, the case of inverse variation. The number of boys in the two situations are :

80 and (80 + 20), i.e., 100 respectively. If the provisions last for x days when the number of boys increased from 80 to 100, we can have the following table :

Number of Boys	Number of Days
80	30
100	x

Here, the ratio between the like terms are :

$$\frac{80}{100} \text{ and } \frac{30}{x}$$

Since, the problem is of inverse variation, we will invert the ratio and then equate them :

$$\frac{x}{30} = \frac{80}{100}$$

or $$\frac{x}{30} = \frac{4}{5}$$

or $$x = \frac{4 \times 30}{5} = \frac{4 \times 6}{1}$$

or $$x = 24$$

Therefore, the provisions will last for 24 days.

Ex.4 A jeep finishes a journey in 9 hours at a speed of 60 km per hour. by how much should its speed be increased so that it may take only 6 hours to finish the same journey ?

Sol. Let the desired speed of the jeep be

x km per hour, then we have :

Number of Hours	Speed of the Jeep (in km per hour)
9	60
6	x

Since, the greater the speed, the lesser the time taken. Therefore, the number of hours and speed vary inversely.

$$\therefore \quad \frac{9}{6} = \frac{x}{60}$$

or $$\frac{x}{60} = \frac{9}{6}$$

or $$x = \frac{9}{6} \times 60 = \frac{9 \times 10}{1} = 90$$

$\therefore$ Increase in speed = (90 – 60) km per hour

= 30 km per hour

Thus, the required increase in speed is 30 km per hour.

◈ Problems on Time and Distance

The speed of a moving body is the distance moved in unit time. It is usually represented either in km/h or m/s.

◈ Relation among Speed, Time and Distance

The relation among speed, distance and time is given by Distance covered = Speed × Time taken.

If any two of them are given, it is easy to determine the third one. The above relation can also be expressed in the following manners :

$$\text{Speed} = \frac{\text{Distance}}{\text{Time}}$$

or $$\text{Time} = \frac{\text{Distance}}{\text{Speed}}$$

We talk about speed, say 27 km/h, it means that we are actually talking about its average speed. By average speed of a vehicle, we mean that constant speed at which the vehicle would cover a distance of 27 km in an hour. Unless mentioned otherwise, by speed we shall mean an average speed.

❖ EXAMPLES ❖

Ex.5 A man takes 12 hours to travel 48 kilometres. How long will he take to travel 72 kilometres?

Sol. Since the man travels 48 km in 12 hours, therefore, one kilometre is travelled in $\frac{12}{48}$ hours.

$\therefore$ He travels 72 km in $\frac{12 \times 72}{48}$ hours

or in 18 hours.

Ex.6 A train of 320 metres length, is running at a speed of 72 km/h. How much time will it take to cross a pole ?

Sol. Speed of the train $= 72$ km/h

$= 72 \times 1000$ m/h

$= \frac{72000}{60 \times 60}$ m/s $= 20$ m/s

Length of the train $= 320$ m

Since the train of length 320 m has to cross the pole of negligible dimension, it has to cross the length of itself, i.e., 320 m.

Thus, distance to be covered = 320 m

Now, using the relation time $= \frac{\text{Distance}}{\text{Speed}}$, we get the required time for the train to cross a distance of 320 m $= \frac{320}{20}$ [$\because$ Speed of the train is 20 m/s (found above)]

Hence, the train takes 16 seconds to cross the pole.

➢ TIME AND WORK

We use the principles of direct and indirect variations to solve problems on 'time and work', such as :

"More men do more work and less men do less work" (Direct variation)

"More men take less time to do a work and less men take more time to do the same work."

(Indirect variation)

The problems on "time and work" are divided in two categories:

(i) To find the work done in a given period of time.

(ii) To find the time required to complete a given job.

◈ Working Rules

We shall use the unitary method by considering the following fundamental rules for solving problems regarding time and work:

(i) A complete job or work is taken to be one.

(ii) Time to complete a work

$$= \frac{\text{Total work to be done}}{\text{Part of the work done in one day}}.$$

❖ EXAMPLES ❖

Ex.7 Ratan takes 5 days to complete a certain job and shankar takes 8 days to do the same job. If both of them work together, how long will they take to complete the work ?

Sol. Since, Ratan takes 5 days to complete the given work

$\therefore$ Ratan finishes $\frac{1}{5}$ part in 1 day.

Similarly, Shankar takes 8 days to complete the work.

Therefore, Shankar finishes $\frac{1}{8}$ part in 1 day.

$\therefore$ In a day, they together will finish

$$= \frac{1}{5} + \frac{1}{8} = \frac{8+5}{40} = \frac{13}{40}$$

i.e., $\frac{13}{40}$ part of the work.

So, they both will take $\frac{40}{13}$ days $3\frac{1}{13}$ days to complete the work. Hence, the complete work will be finished by them together in $3\frac{1}{13}$ days.

Ex.8 Kshitij can do a piece of work in 20 days and Rohan can do the same work in 15 days. They work together for 5 days and then Rohan leaves. In how many days will Kshitij alone finish the remaining work ?

Sol. Since, Kshitij completes the work in 20 days

$\therefore$ Kshitij's 1 day work $= \frac{1}{20}$ part

Now, Rohan completes the work in 15 days.

Similarly, Rohan's 1 day work $= \frac{1}{15}$ part

$\therefore$ Their combined work for 1 day

$$= \frac{1}{20} + \frac{1}{15} = \frac{3+4}{60} = \frac{7}{60}$$

$\therefore$ Their combined work for 5 days

$$= 5 \times \frac{7}{60} = \frac{7}{12} \text{ part}$$

Remaining work = Complete work – Work done in 5 days

$$= 1-\frac{7}{12}$$

$$=\frac{12-7}{12}=\frac{5}{12}\text{ part}$$

Now, the remaining work is to be completed by Kshitij alone.

Kshitij can complete the whole work in 20 days.

So, he will complete $\frac{5}{12}$ work in

$\left(\frac{5}{12}\times 20\right)$ days, i.e., $\frac{25}{3}$ days or $8\frac{1}{3}$ days.

Ex.9 A and B can do a piece of work in 10 days; B and C in 15 days; C and A in 12 days. How long would A and B take separately to do the same work ?

Sol. A and B can complete the work in 10 days.

$\therefore$ (A and B)'s one day work = $\frac{1}{10}$ part

Similarly,

(B and C)'s one day work = $\frac{1}{15}$ part

(C and A)'s one day work = $\frac{1}{12}$ part

Adding up, we get

2(A and B and C)'s work in 1 day

$$=\left(\frac{1}{10}+\frac{1}{15}+\frac{1}{12}\right)\text{part}$$

$$=\frac{6+4+5}{60}=\frac{15}{60}=\frac{1}{4}\text{ part}$$

$\therefore$ (A and B and C) can do in 1 day

$$=\frac{1}{4}\times\frac{1}{2}=\frac{1}{8}\text{ part}$$

Now,

Part of work A can do in 1 day

= (1 day work of A and B and C) – (1 day work of B and C)

$$=\left(\frac{1}{8}\right)-\left(\frac{1}{15}\right)$$

$$=\frac{15-8}{120}=\frac{7}{120}\text{ part}$$

Hence, A can complete the work in $\left(1\times\frac{120}{7}\right)$ days, i.e., $\frac{120}{7}$ or $17\frac{1}{7}$ days.

Similarly,

Part of the work B can do in 1 day

= (1 day work of A and B and C) – (1 day work of A and C)

$$=\left(\frac{1}{8}\right)-\left(\frac{1}{12}\right)=\frac{3-2}{24}=\frac{1}{24}$$

Hence, B can complete the work in $\left(1\times\frac{24}{1}\right)$ days, i.e., 24 days.

Ex.10 A contractor undertakes to construct a road in 20 days and engages 12 workers. After 16 days, he finds that only $\frac{2}{3}$ part of the work has been done. How many more workers should he now engage in order to finish the job in time ?

Sol. From the question, it is clear that $\frac{2}{3}$ part of the work has been completed by 12 workers in 16 days.

$\therefore$ Remaining work = $1-\frac{2}{3}=\frac{1}{3}$

Remaining number of days = 20 – 16 = 4

Thus, $\frac{1}{3}$ part of the work is to be finished in 4 days.

$\therefore$ Number of workers required to complete $\frac{2}{3}$ part of work in 16 days = 12

Number of workers required to complete 1 work in 16 days

$$= 12\times\frac{3}{2}\times 16$$

Number of workers required to complete $\frac{1}{3}$ work in 1 day

$$= 12 \times \frac{3}{2} \times 16 \times \frac{1}{3}$$

Number of workers required to complete $\frac{1}{3}$ work in 4 days

$$= 12 \times \frac{3}{2} \times 16 \times \frac{1}{3} \times \frac{1}{4}$$

$\therefore$ Number of additional workers required

$$= 24 - 12 = 12$$

Hence, the contractor will have to engage 12 more workers to complete the work in time.

Ex.11 A garrison of 350 men had food for 25 days. However, after 5 days a reinforcement of 150 men join them. How long will the food last now?

Sol. As 350 men have already eaten the food for 5 days, so they will eat the remaining food in 20 days. Since 150 men have arrived, the number of men now becomes 500. Thus, it can be represented in a tabular form as,

Men	350	500
Number of days	20	x

Clearly, it is the case of inverse proportion.

Thus, ratio of men = inverse ratio of number of days.

or $\frac{350}{500} = \frac{x}{20}$ or $x = \frac{350 \times 20}{500} = 14$

$\therefore$ The food will last for 14 days.

Time and Work

The amount of work done by a person varies directly with the time taken by him or her.

If a man completes a work in 20 days, thus by unitary method we can say that he will complete $\frac{1}{20}$ th of the work in one day.

Rule 1. If A completes a work in n days, then the work done by A in one day = $\frac{1}{n}$ th part of the works.

Rule 2. If A completes $\frac{1}{n}$ th part of the work in one day, then A will take n days to complete the work.

Ex.12 Ashish takes 12 days to do a piece of work, while Arjun takes 15 days to do the work. Find the time taken by them if they work together.

Sol. Ashish takes 12 days to do piece of work.

$\therefore$ In one day he does $\frac{1}{12}$ th of the work.

Arjun takes 15 days to do a piece of work.

$\therefore$ In one day he does $\frac{1}{15}$ th of the work.

$\therefore$ Together they do $\left(\frac{1}{12} + \frac{1}{15}\right)$ th of the work in one day.

i.e. $\frac{1}{12} + \frac{1}{15} = \frac{5+4}{60} = \frac{9}{60} = \frac{3}{20}$

$\therefore$ In one day they will finish $\frac{3}{20}$ th of the work

$\therefore$ They take $\frac{20}{3} = 6\frac{2}{3}$ days to finish the work.

Ex.13 Two taps take 12 hours and 16 hours respectively to fill a tank. Find the time taken to fill the tank if they are open at the same time.

Sol. Time taken by first pipe = 12 hours

$\therefore$ In 1 hour it fills $\frac{1}{12}$ th of the tank.

Time taken by second pipe = 16 hours

$\therefore$ In 1 hour it fills $\frac{1}{16}$ th of the tank.

$\therefore$ Total work done in 1 hours

$$= \frac{1}{12} + \frac{1}{16} = \frac{4+3}{48} = \frac{7}{48}$$

$\therefore$ Time taken = $\frac{48}{7}$ hour

= 6 hours 51 minutes (approximately).

Ex.14 Mohinder ploughs a field in 6 days and Ram ploughs the same field in 12 days. How long both of them take to plough the same field working together ?

Sol. Mohinder ploughs in 6 days = 1 field

Mohinder ploughs in 1 day = $\frac{1}{6}$th field

Ram ploughs in 1 day = $\frac{1}{12}$th field

Both Ram and Mohinder ploughs in

1 day = $\left(\frac{1}{6}+\frac{1}{12}\right)$th field.

$= \frac{2+1}{12} = \frac{3}{12} = \frac{1}{4}$ field.

Now $\frac{1}{4}$th of the field is ploughed by them in 1 day.

$\therefore$ The complete field will be ploughed by them in $1 \times \frac{4}{1} = 4$ days.

Ex.15 12 men working 8 hours a day complete a work in 10 days. How long would 16 men working $7\frac{1}{2}$ hours a day take to complete the same work ?

Sol. Let the work completed in x days.

Men	Hours	Days
12	8	10
16	$\frac{15}{2}$	x

$$\left.\begin{array}{l}\text{More men less time}\\ \text{Less men more time}\\ \text{Thus, it is inverse variation}\end{array}\right] \left.\begin{array}{l}16:12\\ \frac{15}{2}:8\end{array}\right\} ::10:x$$

$$\therefore x = \frac{10\times12\times8\times2}{16\times15} = 8$$

$\therefore$ 16 men will complete the same work in 8 days.

Ex.16 2 men and 3 boys can harvest a field in 7 days. How long would 1 man and 2 boys take to harvest the same field ?

Sol. Given that 2 men and 3 boys harvest a field in 7 days. Thus, let us calculate the amount of field harvested by each one in one day.

2 men harvest 1 field in 7 days.

In one day 2 men will harvest $\frac{1}{7}$th of the field.

In one day 1 man will harvest $\frac{1}{2\times7}$th, i.e. $\frac{1}{14}$ th of the field.

Similarly, 1 boy will harvest $\frac{1}{3\times7}$th, i.e. $\frac{1}{21}$th of the field in one day.

Now, we have to find the time taken by 1 man and 2 boys to harvest the field. Adding the amounts of work completed by 1 man and 2 boys in one day, we get

$$\frac{1}{14} + \frac{2}{21} = \frac{3+4}{42} = \frac{7}{42} \text{ or } \frac{1}{6}$$

Thus, they will take 6 days to complete the harvesting.

➤ TIME, DISTANCE AND SPEED

We generally say that a body is covering so many kilometres every hour or so many metres in every second. We define speed of a body as the distance covered in unit time. Here, unit time can be one hour or one minute or one second and a body means an object.

Thus, speed is expressed in metres per second(m/s) or kilometres per second (km/s) or centimetres per second (cm/s). To find the speed of a moving object, we divide the distance covered by the time taken.

$$\therefore \text{Speed} = \frac{\text{Distance}}{\text{Time}} \text{ or Time} = \frac{\text{Distance}}{\text{Speed}}$$

or Distance = Speed × Time .

Ex.17 A man takes 2 hours to cover a distance when he walks at 3 kilometres per hour (kmph). Find the time taken if he walks at the rate of 4 kmph.

Sol. Speed = 3 km/h; Time = 2 hours

$\therefore$ Distance = 3 × 2 = 6 km

New speed = 4 km/h

Distance = 6 km

$$\therefore \quad \text{Time} = \frac{\text{Distance}}{\text{Speed}} = \frac{6}{4} = 1\frac{1}{2} \text{ hours}$$

Thus, the time taken by the man is $1\frac{1}{2}$ hours.

Ex.18 A train 375 m long takes 30 seconds to cross a pole. Find the speed of the train in kilometres per hour.

Sol. To cross a pole means the whole train should cross the pole.

$\therefore$ The distance travelled = 375 m

Time taken = 30 seconds

$\therefore$ Speed = $\frac{\text{Distance}}{\text{Time}} = \frac{375}{30}$ ms^{-1} = 12.5 ms^{-1}

In the above example, we have to convert metres per second into kilometres per hour.

Now, 1 hour = 60 × 60 seconds, 1 km = 1000 m

$\therefore \frac{km}{hr} = \frac{1000}{3600}\frac{m}{s}$ $\quad 1\frac{km}{hr} = \frac{5}{18}\frac{m}{s}$

or 1 m/s = $\frac{18}{5}$ km/hr

$\therefore$ 12 .5 $\frac{m}{s}$ = 12.5 × $\frac{18}{5}$ = 2.5 × 18 = 45 km/h.

Remember : To convert $\frac{m}{s}$ to $\frac{km}{hr}$ multiply by $\frac{18}{5}$.

To convert $\frac{km}{hr}$ to $\frac{m}{s}$, multiply by $\frac{5}{18}$.

Ex.19 A train 400 m long crosses a 800m long bridge. If it is travelling at 40 kmph, find the time taken to cross the bridge.

Sol. The distance travelled will be the whole length of the train and the whole length of bridge = 400 m + 800 m = 1200 m.

Speed = 40km/h = 40 × $\frac{5}{18}$ m/s = $\frac{100}{9}$ m/s

$\therefore$ Time = $\frac{\text{Distance}}{\text{Speed}} = \frac{1200}{100/9}$ sec = 108 sec

or 1 min 48 sec.

Ex.20 Two trains 132 m and 400 m in length are running on parallel tracks towards each other at 40 km/h and 55 km/h. Find the time taken to cross each other.

Sol. Since they are travelling towards each other, their relative speed will be (40 + 55) km/h = 95 km/h.

The distance travelled is the total length of the two trains,

i.e. 132 + 400 = 532 m.

$\therefore$ Time taken = $\frac{\text{Total distance}}{\text{Total Speed}} = \frac{532}{95\times\frac{5}{18}}$

$= \frac{532\times18}{95\times5}$ = 20.16 seconds.

Ex.21 Two trains of length 150 m and 180 m are running on parallel tracks in the same direction. Find the time taken to cross each other if their speeds are 35 km/h and 40 km/h.

Sol. Since they are moving in the same directing, the relative speed will be (40 – 35) km/h = 5 km/h.

The distance covered will be total length of the two trains = 150 + 180 = 330 m

Time taken = $\frac{\text{Distance}}{\text{Speed}}$

$= \frac{330}{5\times\frac{5}{18}} = \frac{330\times18}{5\times5}$

= 237.6 seconds = 3.96 minutes.

Ex.22 A train moving at 30 km per hour completes its journey in 14 hours. How much time will the train take for the same journey if it travelled at 60 km per hour ?

Sol. The given information can be shown in a tabular form as :

Speed (kmph)	30	60
Time (hours)	14	x

As the speed increases, the time decreases and the distance remains the same.

$\therefore$ 30 × 14 = 60 × x (refers to distance).

$\therefore$ x = $\frac{30\times14}{60}$ = 7 hours

Thus, the train will take 7 hours to complete the journey moving at 60 km/hr.

EXERCISE # 1

Q.1 A does a work in 10 days and B does the same work in 15 days. In how many days they together will do the same work ?

(A) 5 days (B) 6 days
(C) 8 days (D) 9 days

Q.2 A can finish a work in 18 days and B can do the same work in half the time taken by A. Then, working together, what part of the same work they can finish in a day ?

(A) $\frac{1}{6}$ (B) $\frac{2}{9}$
(C) $\frac{1}{9}$ (D) $\frac{2}{7}$

Q.3 A tyre has two punctures. The first puncture alone would have made the tyre flat in 9 minutes and the second alone would have done it in 6 minutes. If air leaks out at a constant rate, how long does it take both the punctures together to make if flat ?

(A) $1\frac{1}{2}$ minutes (B) $3\frac{1}{2}$ minutes
(C) $3\frac{3}{5}$ minutes (D) $4\frac{1}{4}$ minutes

Q.4 A family has enough rice for 8 members for 30 days. Find the number of days the rice will last if the members increased to 10.

Q.5 125 people finish a piece of work in 120 days. Find the number of people required to finish the same work in 100 days.

Q.6 Three taps take 6 hours, 8 hours and 12 hours respectively to fill a tank. How long will it take for all three taps together to fill the tank ?

Q.7 16 men can do a piece of work in 7 days. How long will it take 14 men to do the same work ?

Q.8 A restaurant has food stock to supply food for 900 people for 40 days. If only 600 people visited the restaurant, how long will the food last ?

Q.9 If apples are sold at ₹ 5 each, Sushma can buy 2 dozen apples with the money in her purse. How much will she buy if the cost is increased by ₹ 1 each ?

Q.10 8 horses consume a certain quantity of grains in 50 days. How long will the grains last if the number of horses is increased to 20 ?

Q.11 A school has enough food for 400 children for 12 days. How long will the food last for 80 more children ?

Q.12 Ramesh pours 10^5 granules of sand per second in a bottle and it takes him 320 days to fill it. How many days will it take to fill that bottle if he pours 10^6 granules per second ?

Q.13 Fill in the tables

(a)

x (number of men)	2	3	——	16	48
Y (time taken)	24	——	8	——	——

(b)

x (men)	8	2	18	9	——	——
y (days)	9	——	——	——	12	1

(c)

x (men)	12	——	28	——	6
y (time)	7	4	——	42	——

Q.14 A tank can be filled by two pipes A and B in 12 hours and 16 hours, respectively. While pipe C empties it in 8 hours, find the time taken to empty the tank if all three pipes are open (emptying implies negative).

Q.15 2 men working together take 6 days to finish a piece of work. If one of them takes 15 days if he works alone, find how long the second man will take to finish it, working alone ?

Q.16 A and B take 12 days to finish a piece of work. If B and C work together they take 15 days. While A and C together take 20 days. Find the time taken by each to work alone.

Q.17 A contractor hires 120 men to complete a job in 6 months. How many men should he hire if he has to complete the job in 4 months ?

Q.18 A and B together can write a manuscript in 20 days. If A takes 25 days when working along, find the time taken by B working alone.

Q.19 30 men can harvest a field in 14 days. Find the time taken by 20 men for the same job.

Q.20 Meeta. Veena and Kamlesh can sweep a playground in 4, 6 and 8 hours respectively. What portion of that ground can they sweep in one hour working together ?

Q.21 If 20 men working 12 hours a day can do binding of 2500 books in a day, how many books can 24 men bind in a day if each of them work 8 hours a day ?

Q.22 4 men and 7 boys can dig a tank in 15 days. How long would 2 men and 4 boys working together take to dig the tank.

Q.23 A can do a piece of work in 25 days, B can finish it in 20 days. They work together for 5 days and then A goes away. In how many days will B finish the remaining work ?

Q.24 6 men can complete the electric fitting of a building in 7 days. How many days will it take if 21 men do the job ?

Q.25 A cistern can be filled by one tap in 8 hours and by another in 4 hours. How long will it take to fill the cistern if both taps are opened together ?

ANSWER KEY

EXERCISE # 1

1. 6 days	**2.** $\frac{1}{6}$	**3.** $3\frac{3}{5}$ minutes	**4.** 24 days	**5.** 150 people
6. $\frac{8}{3}$ hours	**7.** 8 days	**8.** 60 days	**9.** 20 apples	**10.** 20 days
11. 10 days	**12.** 32 days	**13.** (a) 16, 6, 3, 1	(b) 36, 4, 8, 6, 72	(c) 21, 3, 2, 14
14. 48 hrs	**15.** 10 days	**16.** A = 30 days, B = 20 days, C = 60 days		**17.** 180 men
18. 100 days	**19.** 21 days	**20.** $\frac{13}{24}$ th portion	**21.** 2000 books	**22.** 52.5 days
23. 11 days	**24.** 2 days	**25.** $\frac{8}{3}$ hrs		

EXERCISE # 2

Q.1 If 12 boys earn ₹ 840 in 7 days, what will 15 boys earn in 6 days ?

Q.2 If 25 men earn ₹ 1000 in 10 days, how much will 15 men earn in 15 days ?

Q.3 Find the time taken by a train of length 200 m at 60 kmph to cross a lamp post.

Q.4 A car moving from city A to city B takes $8\frac{1}{2}$ hours. If the distance between the cities is 425 km, find the speed of the car.

Q.5 What is the distance covered by a car at 73 kmph in $5\frac{1}{2}$ hours ?

Q.6 Suresh cycles at 30 kmph to reach a destination 285 km away. What is the time taken by him ?

Q.7 Two cars start from the same point at speeds 60 km/h and 50 km/h. The slower car starts half an hour earlier. When will the other car catch up with the slower car ?

Q.8 Two trains start from the same station in the same direction but with a gap of one hour. The earlier train travels at 80 km/h while the second train travels at 95 km/h. When will the second train overtake the first ?

Q.9 How long will a train 600 m long take to cross a pole, if it travels at 45 kmph ?

Q.10 How long will a train 650 m long take to cross a bridge 350 m long, if it travels at a speed of 54 kmph ?

Q.11 A train 450 m long crosses a bridge in 72 seconds travelling at 60 kmph. Find the length of the bridge.

Q.12 A 300 m long train is travelling at 85 km/h. A man is running in the same direction at 5 km/h. How long will it take the train to cross the man ?

Q.13 A train 750 m long travelling at 45 km/h takes 72 seconds to cross another train travelling in the opposite direction at 52 km/h. Find the length of the second train.

Q.14 Two trains of length 220 m and 100 m are travelling on parallel lines in the same direction with speeds 46 km/h and 36 km/h. How long will it take the faster train to overtake the slower train? How long will it take if the trains were moving in the opposite directions ?

Q.15 A car takes 9 hours to cover a distance from X to Y travelling at 40 km per hour. Find the time taken if its speed is increased by 20 km per hour.

Q.16 A plane takes $1\frac{2}{3}$ hours to cover a distance flying at 340 km per hour. Find the time taken if the speed is increased to 850 km per hour.

ANSWER KEY

EXERCISE # 2

1. ₹ 900	**2.** ₹ 900	**3.** 12 sec	**4.** 50 km/h	**5.** 401.5 km
6. 9.5 h	**7.** $2\frac{1}{2}$ hr	**8.** $\frac{16}{3}$ hrs	**9.** 48 sec	**10.** 1 min 7 sec (approx)
11. 750 m	**12.** $\frac{27}{2}$ sec	**13.** 1190 m	**14.** 115.2 sec, 14.048 sec	
15. 6 hr	**16.** $\frac{2}{3}$ hr			