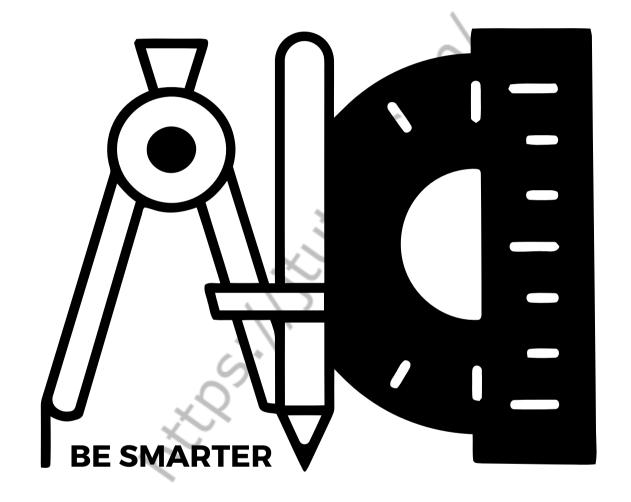
J-TUTES



YEAR 5 WORKBOOK

TERM 4 SYLLABUS

A) Write the point that is located at each ordered pair.

1) (2,4) _____ 2) (-2,5) _____

B) Write the ordered pair for each point.

7) Q(___,__)

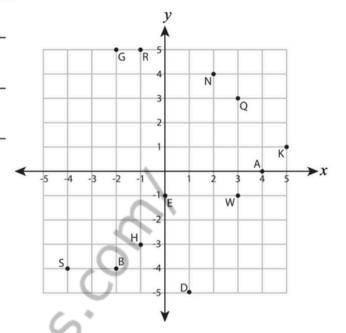
8) E(___, ___)

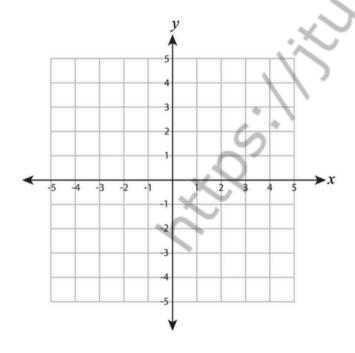
9) H(___,__)

10) R(____,___)

11) W(___,__)

12) A(___,__)





C) Plot each point on the coordinate grid.

13) U(-3,-3)

14) S(-4,5)

15) F(0,-4)

16) X(2,2)

17) T(1,-1)

18) K(5,-2)

D) Draw each shape on the coordinate grid.

19) Draw at (1,3)

20) Draw △ at (-5, -5)

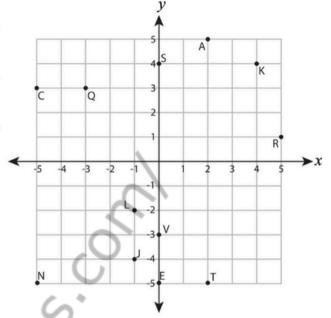
21) Draw 🖒 at (4, 1)

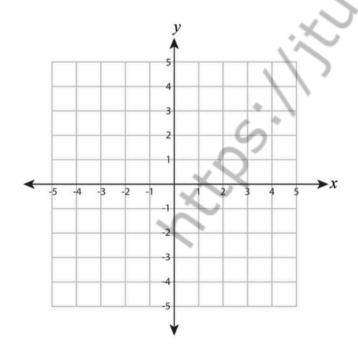
A) Write the point that is located at each ordered pair.

- 1) (-1,-4) _____ 2) (-3,3) _____
- 3) (2,5)
- 4) (5,1)
- 5) (0,-5)
- 6) (-5,-5)

B) Write the ordered pair for each point.

- 7) L(___,__)
- 8) K(____, ___)
- 9) V(___,__) 10) T(___,__)
- 11) C(___,__) 12) S(___,__)





C) Plot each point on the coordinate grid.

- 13) H(-5,-3)
- 14) Z(0,1)
- 15) D(4,-4) 16) P(-4,2)
- 17) Y(3,5)
- 18) M(-3,-1)

D) Draw each shape on the coordinate grid.

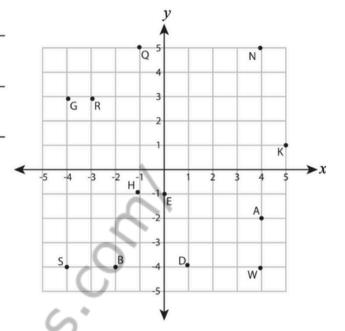
- 19) Draw () at (-1,-4)
- 20) Draw △ at (-2, 5)
- 21) Draw 🖒 at (5,-5)

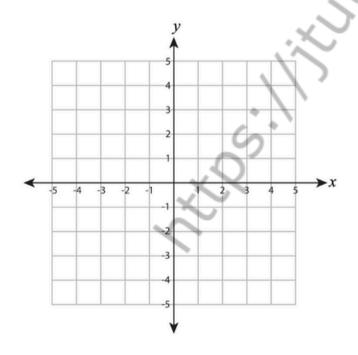
A) Write the point that is located at each ordered pair.

- 1) (4,5) _____ 2) (-1,5) _____
- 3) (4,-4)
- 4) (5,1)
- 5) (1,-4) _____ 6) (-2,-4) _____



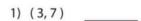
- 7) Q(___,__)
- 8) E(___, ___)
- 9) H(___,__)
- 10) R(____,___)
- 11) W(___,__)
- 12) A(___,__)

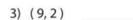




- C) Plot each point on the coordinate grid.
- 13) U(3,-3)
- 14) S(-2,5)
- 15) F(0,-1)
- 16) X(3,2)
- 17) T(-1,-1)
- 18) K(4,-2)
- D) Draw each shape on the coordinate grid.
- 19) Label A at (3, 3)
- 20) Label B at (-1,-5)
- 21) Label C at (4,-1)

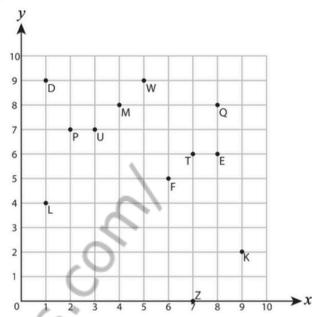
A) Write the point that is located at each ordered pair.

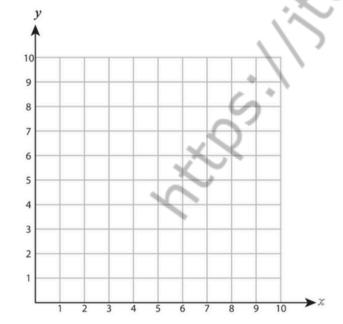




B) Write the ordered pair for each point.







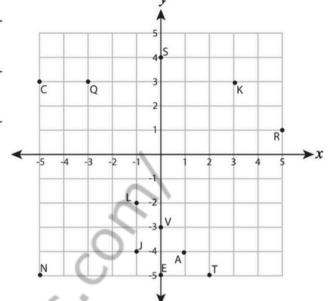
C) Plot each point on the coordinate grid.

D) Draw each shape on the coordinate grid.

A) Write the point that is located at each ordered pair.

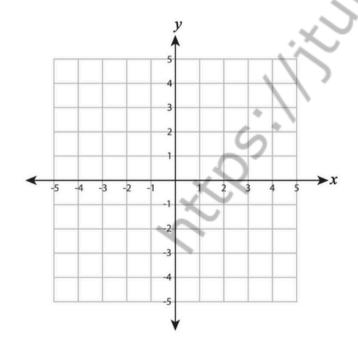
- 1) (1,-4) _____ 2) (3,3)
- 3) (-5, 3) 4) (5, 1)

- 5) (0,-5) _____ 6) (-5,-5) ____



B) Write the ordered pair for each point.

- 7) L(___,__)
- 8) K(____, ___)
- 9) V(___,__)
- 10) T(____,___)
- 11) C(___,__)
- 12) S(___,__)



C) Plot each point on the coordinate grid.

- 13) H(-5,-3)
- 14) Z(0,1)
- 15) D(4,-4)
- 16) P(-4, 2)
- 17) Y(3,5)
- 18) M(-3,-1)

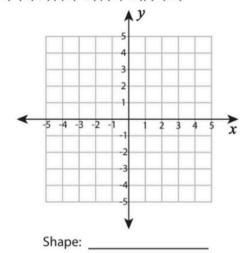
D) Draw each shape on the coordinate grid.

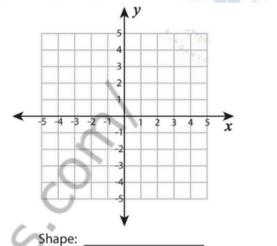
- 19) Label A at (0, 3)
- 20) Label B at (2,-5)
- 21) Label C at (0,-1)

PLOTTING POINTS - SHAPES

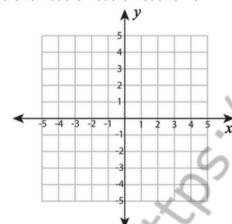
Plot and join the points in the given order. Complete the figure by joining the end points. Identify the shape.

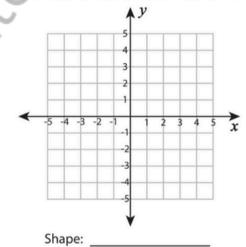
1) (5,3),(5,-3),(2,-3),(2,3)



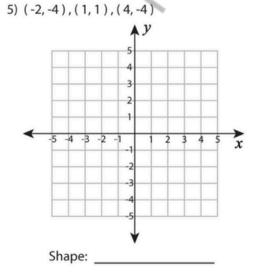


3) (-2,-1),(1,-1),(1,-4),(-2,-4)

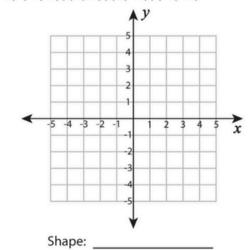




Shape:



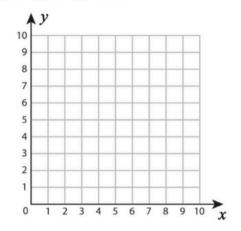
6) (-1,2),(2,5),(2,-5),(-1,-2)



PLOTTING POINTS - SHAPES

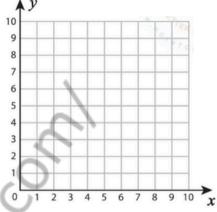
Plot and join the points in the given order. Complete the figure by joining the end points. Identify the shape.

1) (5,3), (5,7), (10,3)

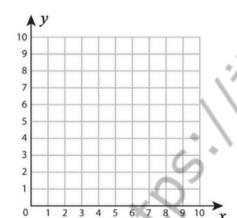




2) (3,4), (7,4), (8,2), (4,2)

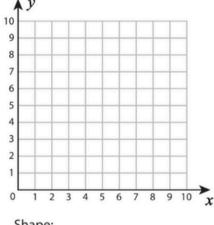


3) (5,9), (7,7), (6,4), (4,4), (3,7)



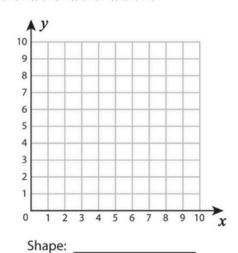
Shape:

(3,2),(5,4),(7,4),(9,2)

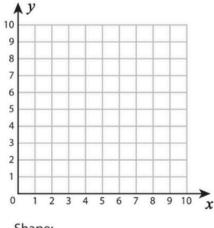


Shape:

5) (3,5), (6,5), (6,2), (3,2)



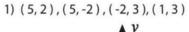
6) (2,7),(9,7),(9,3),(2,3)

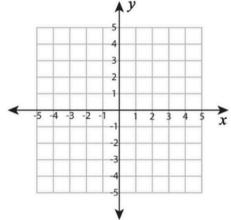


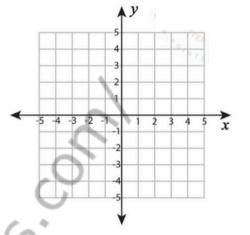
Shape: _

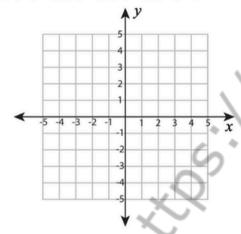
PLOTTING POINTS - SHAPES

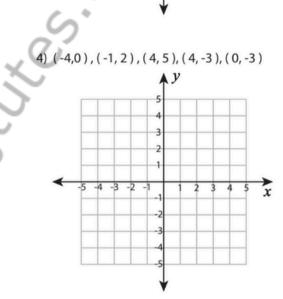
Plot and join the points in the given order. Complete the figure by joining the end points. Identify the shape.

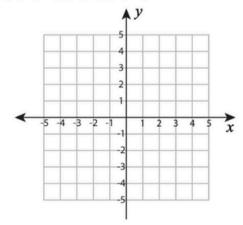


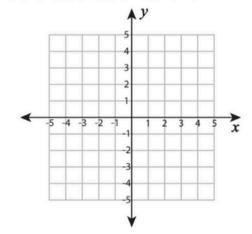








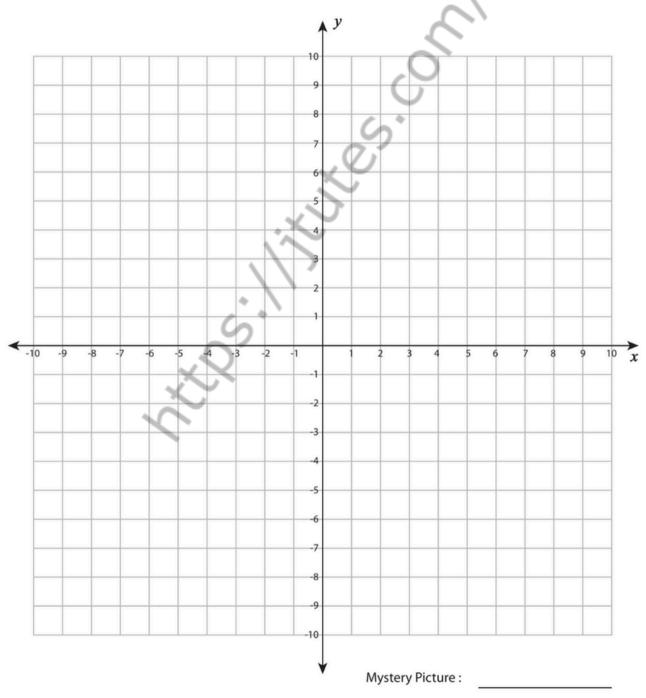




MYSTERY PICTURE

Plot and join the points in the given order. Identify the mystery picture.

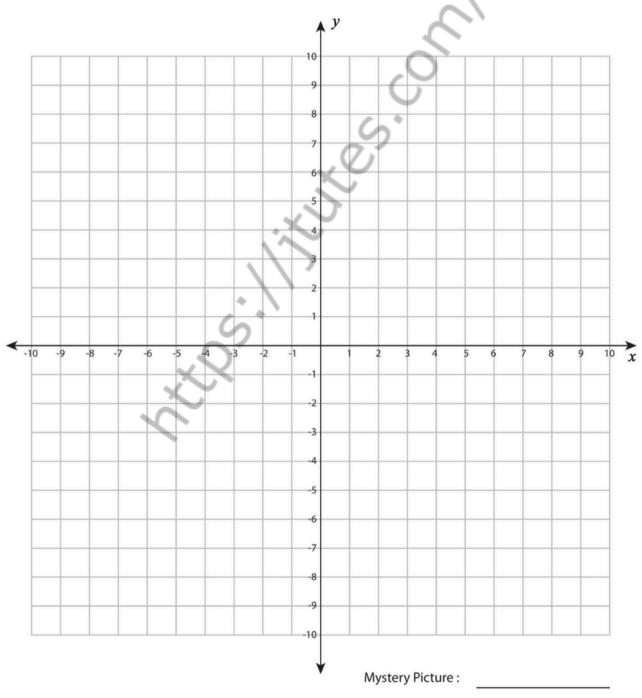
Start (-3, 3), (-1, 3), (-1, 1), (2, 1), (2, 3), (4, 3), (8, -2), (6, -7), (-5, -7), (-7, -2), End (-3, 3)



MYSTERY PICTURE

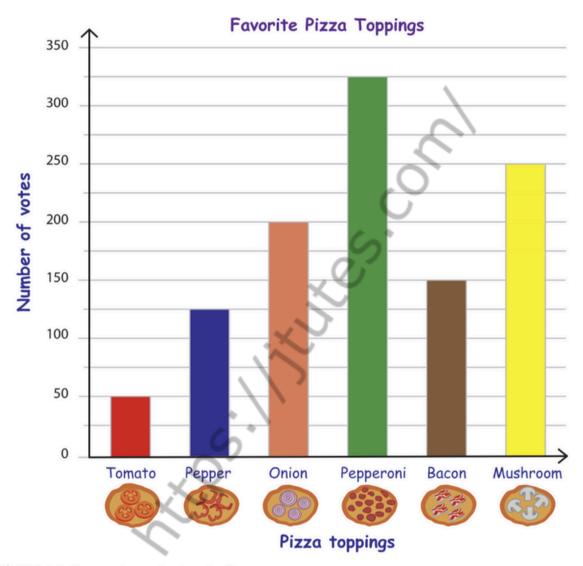
Plot and join the points in the given order. Complete the picture by joining the end points. Identify the mystery picture.

(-8, 1), (-8, 2), (-6, 2), (-7, 5), (-6, 5), (-4, 2), (1, 1), (2, 5), (3, 4), (3, 1), (8, -1), (9, -3), (7, -4), (4, -3), (1, -2), (-4, -4), (-5, -3), (-1, -1), (-3, 0), (-5, 1)



BAR GRAPH - PIZZA TOPPINGS

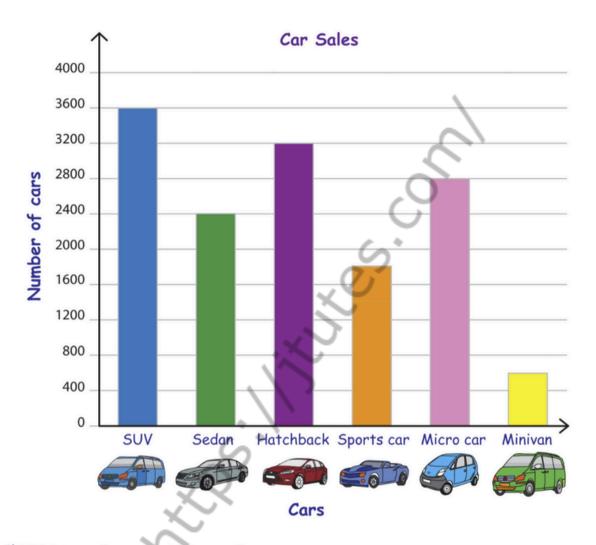
Good Time Pizza Makers are best in making pizzas with six different toppings. They took a survey about customers' favorite toppings and recorded the results in a bar graph. Use the bar graph to answer the questions.



- 1) Which is the most popular topping?
- 2) How many customers have chosen either tomato or pepper toppings?
- 3) If 75 more customers prefer bacon, which one will top the chart, bacon or onion?
- 4) Which topping has 250 votes?
- 5) List the toppings in order from most popular to least popular.

<u>CHAPTER 2 - READING GRAPHS (BAR GRAPHS)</u> BAR GRAPH - CAR SALES

A survey is conducted on the number of cars sold by Mathew's Cars in 2013. The information is recorded in a bar graph. Use the graph to answer the questions.



1) Which type of car was sold the most?

2) How many fewer sports cars were sold than hatchbacks?

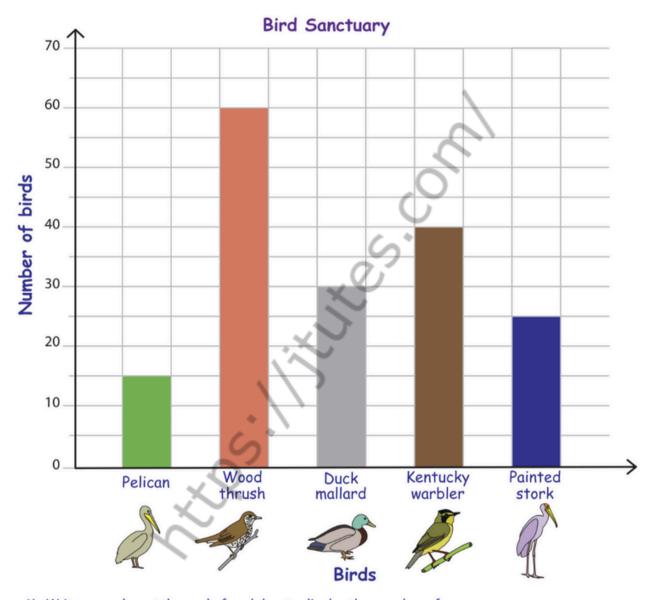
3) How many more SUV cars were sold than Sedans?

4) The sales of sports cars and minivans putting together equals the sales of

5) Find the number of cars sold in all.

BAR GRAPH - BIRD SANCTUARY

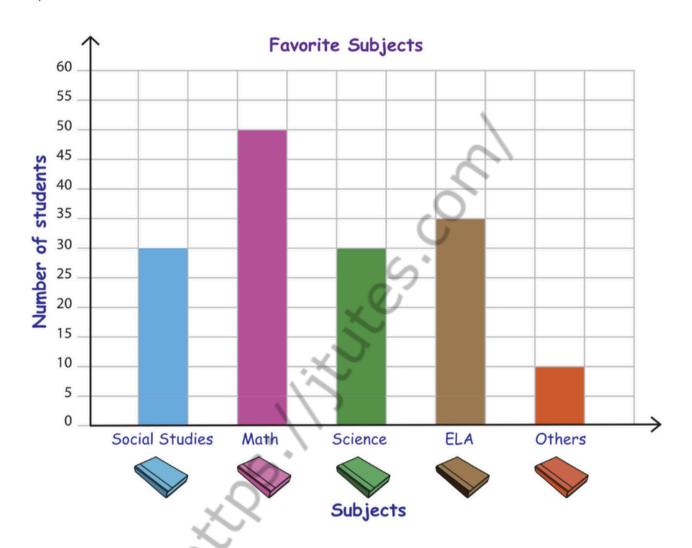
Mr. Brandon, a staff of Exotic Bird Sanctuary, tracks the number of birds migrating to the sanctuary during Spring. He records the information in a bar graph. Use the graph to answer the questions.



- 1) Write a number at the end of each bar to display the number of birds of each kind.
- 2) What is represented along the x-axis of the graph?
- 3) Which bird counts between 10 and 20?
- 4) Which is more, Wood thrush or Kentucky warbler?
- 5) If six Painted stork flew away, how many Painted stork would have left?_____

BAR GRAPH - FAVOURITE SUBJECTS

Miss. Sarah, a teacher of Edwards Elementary School, recorded the favorite subjects of her students in a bar graph. Use the graph to answer the questions.



1)	among the students?	
2)	Which subject is the second most popular?	

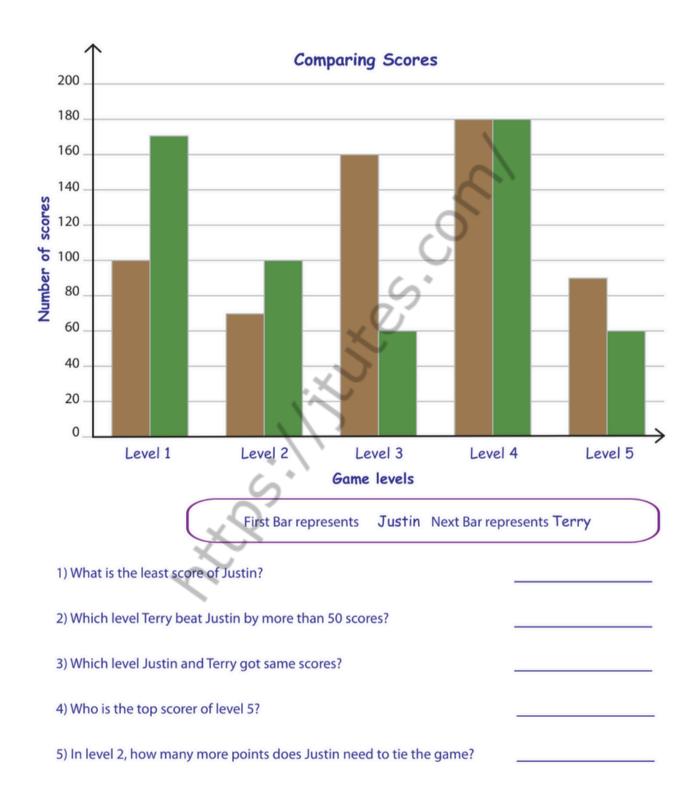
3) Which subject is less popular, science or ELA?

4) Which subject is favorite for 50 students?

5) Which subjects have the same number of votes?

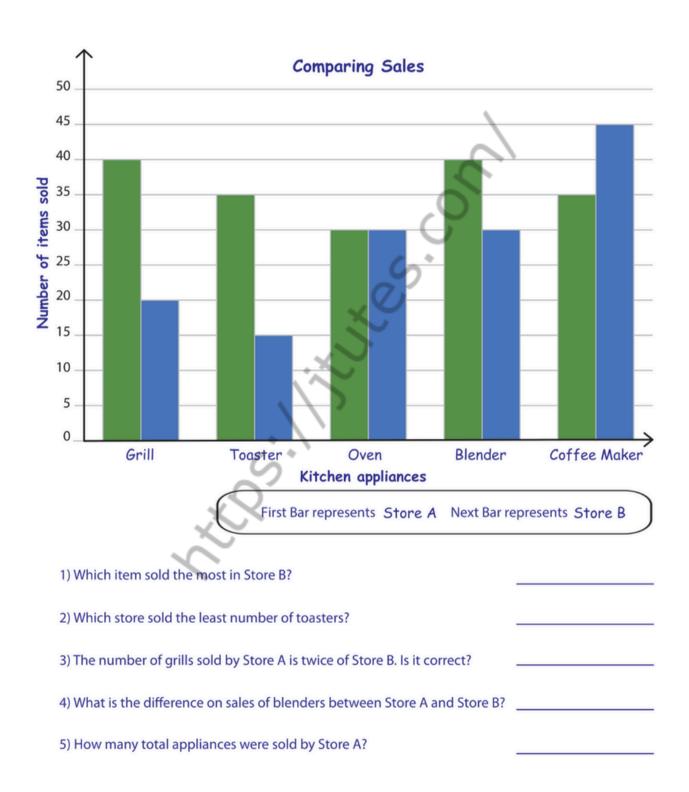
BAR GRAPH - GAME SCORES

Justin and Terry played video games. They recorded their scores in a bar graph. Use the bar graph to answer the questions.



CHAPTER 2 - READING GRAPHS (BAR GRAPHS) BAR GRAPH - COMPARING SALES

Mr. Peter owns two kitchen appliance stores. He compares the sales of two stores and recorded the information in a bar graph. Use the bar graph to answer the questions.



BAR GRAPH - GONE FISHING

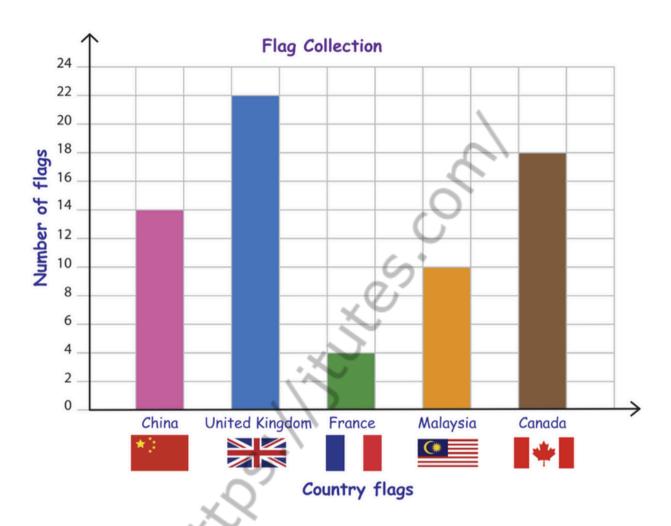
In a camp activity, a group of girls and boys go fishing everyday from Monday through Friday.

They made a bar graph to show the number of fish they caught each day. Use the bar graph to answer the questions.



BAR GRAPH - FLAG COLLECTION

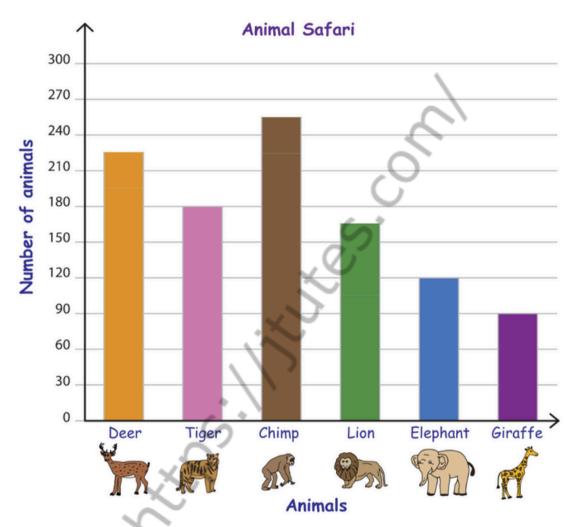
John has a hobby of collecting flags of different countries. The bar graph displays the number of flags collected by him. Use the graph to answer the questions.



- How many fewer China flags does John have than United Kingdom flags?
- 2) Which country flag does John have fewer than 5?
- 3) How many more Malaysian flags should John need to have the same count as Canadian flags?
- 4) How many flags does John have altogether?
- 5) Write the countries in order from fewest flags to most flags.

BAR GRAPH - ANIMAL SAFARI

Henry Ford Zoo, a drive-through safari invites visitors to spend the day with six types of animals, including various activities like feeding, bathing and more. The graph shows the number of animals in each kind. Use the graph to answer the questions.



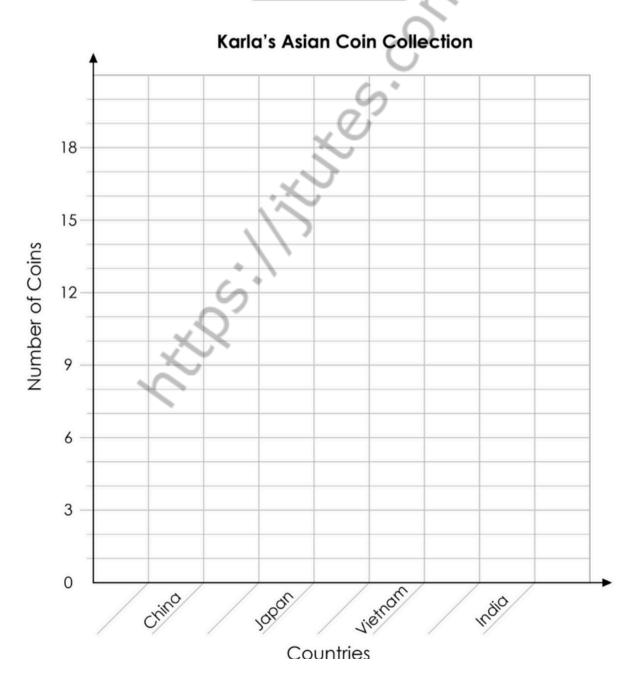
- 1) Write a number at the end of each bar to display the number of animals of each kind.
- 2) Are there more Chimps or Deer?
- 3) Which animal is double the count of Giraffe?
- 4) How many more elephants are required to have an equal number of elephants and lions?
- 5) Henry Ford's zoo made an exchange deal with Saint Peter's zoo. They exchanged 10 tigers, 5 lions and 15 chimps for 9 elephants, 15 deer and 5 giraffes. What would be the new count of animals in each kind?

Deer:	; Tiger:	; Chimp:	; Lion:	; Elephant:	; Giraffe:	
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BAR GRAPH OF COINS

Karla collects coins from Asian countries. The table below shows how many coins she has collected from four different countries. Use the information in the table to complete the graph.

13
15
4
10



BAR GRAPH OF COINS

Use the bar graph you made to answer the questions.

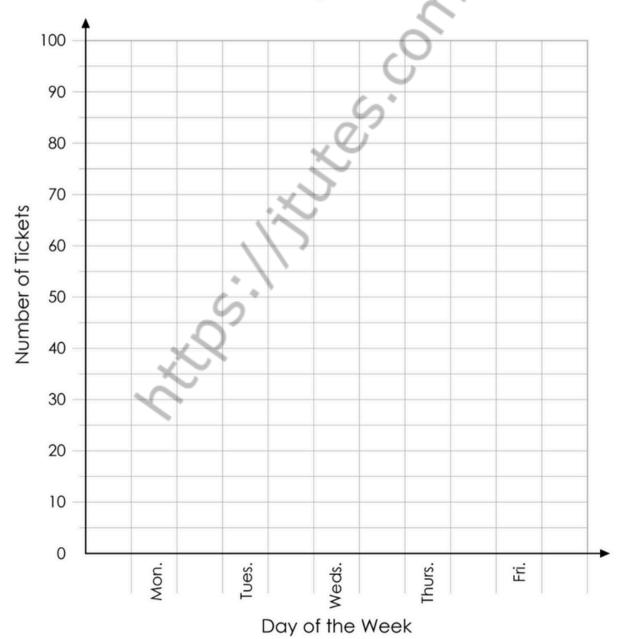
1.	How many more coins does Karla have from China than 1.	
	Vietnam?	
2.	How many fewer coins does Karla have from India than 2. Japan?	
3.	How many total coins does Karla have from these four countries?	
4.	What is on the x-axis of this graph? 4.	
5.	What is on the y-axis of this graph? 5.	
6.	Karla's grandmother sends her seven more coins from China. How many Chinese coins does she have now?	
7.	Karla's older sister sent her 23 more coins from Vietnam. 7. How many Vietnamese coins does she have now?	
8.	Karla traded coins with her friend Patty. She gave Patty three of her Indian coins and Patty gave Karla two more Japanese coins.	
	How many Indian coins does Karla have now?	
	How many Japanese coins does Karla have now?	,

BAR GRAPH OF TICKET SALES

Esther's school sold raffle tickets last week. The table below shows the number of tickets sold each day. Use the information in the table to complete the graph.

٨	Лon.	Tues.	Weds.	Thurs.	Fri.
	55	40	25	35	80

Esther's Daily Raffle Ticket Sales



BAR GRAPH OF TICKET SALES

Use the bar graph you made to answer the questions.

1.	How many tickets were sold on Monday?	1
2.	How many tickets were sold on Thursday?	2
3.	On which day were the most tickets sold?	3.
4.	On which day were the fewest tickets sold?	4
5.	What is on the y-axis of this graph? 5.	
6.	What is on the x-axis of this graph? 6	
7.	How many tickets were sold after Tuesday?	7
8.	How many tickets were sold before Thursday?	8
9.	During which two day period were 115 tickets sold?	9
10.	How many fewer tickets were sold on Wednesday than Thursday?	10

CHAPTER 3 - READING GRAPHS (BAR & PIE GRAPH) POPCORN SALES PICTOGRAPH

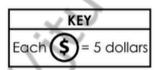
Four Boy Scouts sold popcorn for one month. The list below shows how much money was collected by each Boy Scout.

Logan - \$30

Andrew - \$45

Use the information from the list to complete the pictograph below and answer the questions.

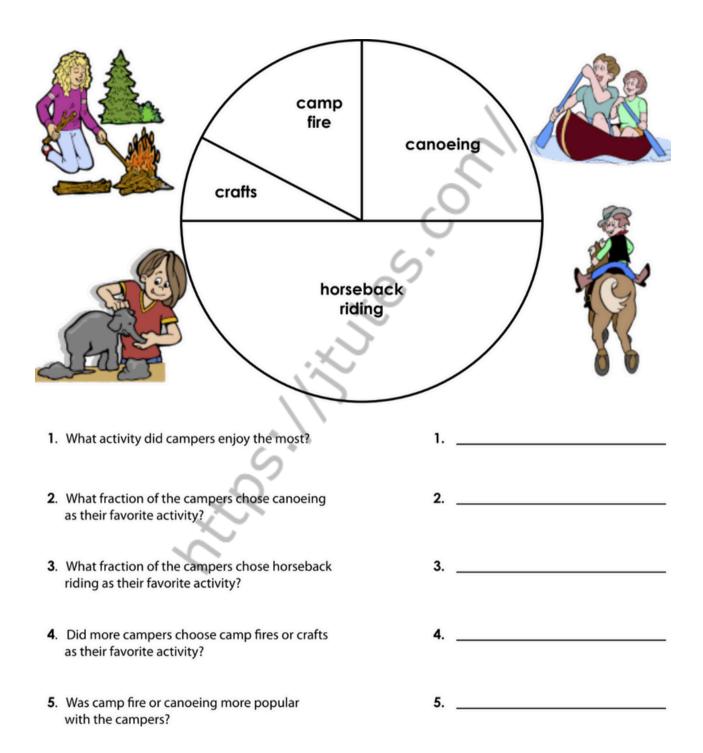
Name	Money Collected
John	
Carter	
Logan	S
Andrew	2



- 1. How much money did the boys collect in all?
- 1. _____
- 2. How much more money did Carter collect than Andrew?
- 2. _____
- 3. Which two boys sold a total of \$120 of popcorn?
- 3. _____
- 4. Who sold more popcorn than Logan, but less than Carter?
- 4. _____

SUMMER CAMP ACTIVITES

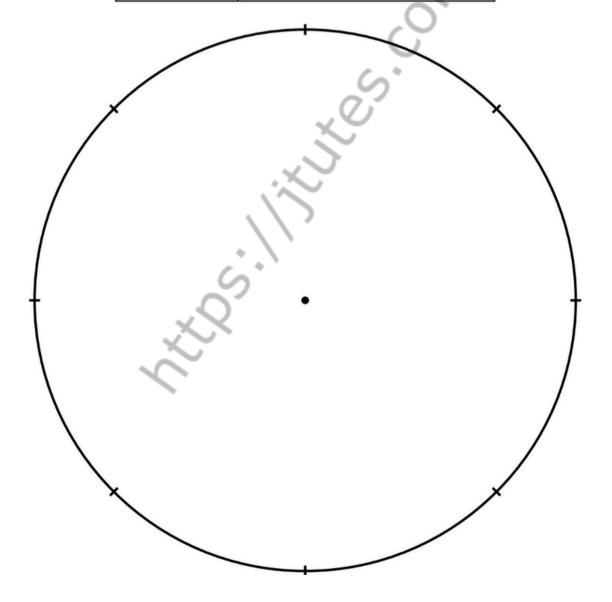
A group of kids spent a week at Big Tree Summer Camp. At the end of the week, the counselors asked campers what their favorite part of camp was. The pie graph shows their responses.



FAVORITE SPORTS GRAPH

Patty surveyed her friends to find out their favorite sports. The table shows the results. Make a circle graph using the information in the table.

football	##	##		
baseball	\iiint			
tennis	IJ			
basketball	##	##	##	##
hockey	##		4	Ç.,



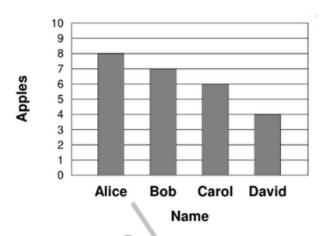
FAVORITE SPORTS GRAPH

Use the circle graph you made to answer the questions.

1.	What fraction of Patty's friends said football		
	was their favorite sport?		
_			
2.	What fraction said hockey was their favorite	-	
	sport?		
		0,	
3.	How many more people chose basketball	\sim	
	than tennis?		
	5		
	(7)		
4.	About one half of Patty's friends chose which sport?	l	
	sporte		
	× ×		
5.	About one quarter of Patty's friends chose which	i	
	sport?		
	* \		
	(0*		
,	What fraction of Dath is fire as above based all		
٥.	What fraction of Patty's friends chose baseball or tennis?)	
	OI TOTTI IIST		
7.	What fraction of Patty's friends chose football	'	
	or basketball?		

GRAPHS

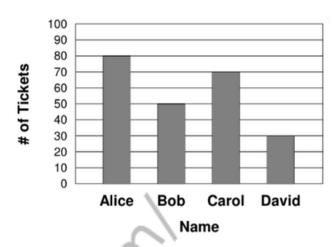
The graph to the right shows the number of apples picked by students visiting a farm.



- How many fewer apples were picked by Bob than Alice?
- How many fewer apples were picked by David than Bob?
- 3) How many apples were picked by Carol and Alice combined?
- How many more apples were picked by Bob than Carol?
- 5) How many apples were picked by David and Carol combined?
- How many apples were picked by Carol and David combined?
- 7) How many fewer apples were picked by Carol than Alice?
- How many apples were picked by Bob and Alice combined?

GRAPHS

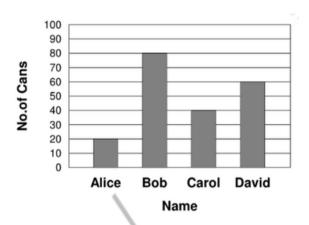
The graph to the right shows the number of tickets sold by students in the drama club.



- How many tickets were sold by David and Bob combined?
- 2) How many more tickets were sold by Bob than David?
- How many fewer tickets were sold by Bob than Alice?
- How many more tickets were sold by Carol than Bob?
- How many tickets were sold by Bob and David combined?
- How many fewer tickets were sold by David than Bob?
- How many fewer tickets were sold by David than Carol?
- How many fewer tickets were sold by Carol than Alice?

GRAPHS

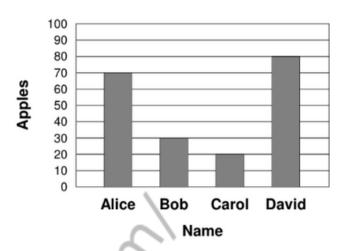
The graph to the right shows the number of cans collected by children for a recycling project.



- How many fewer cans were collected by Alice than David?
- 2)
 How many fewer cans were collected by Alice than Bob?
- How many cans were collected by Alice and Bob combined?
- How many more cans were collected by David than Carol?
- How many cans were collected by David and Alice combined?
- How many more cans were collected by David than Alice?
- 7) How many more cans were collected by Bob than Alice?
- How many fewer cans were collected by Carol than David?

GRAPHS

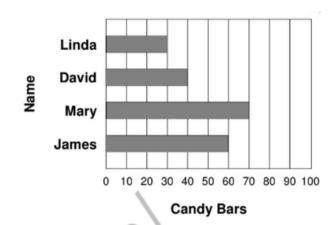
The graph to the right shows the number of apples picked by students visiting a farm.



- How many apples were picked by David and Bob combined?
- 2) How many apples were picked by Carol and Alice combined?
- 3) How many fewer apples were picked by Alice than David?
- How many more apples were picked by Bob than Carol?
- How many fewer apples were picked by Carol than David?
- How many fewer apples were picked by Bob than David?
- How many fewer apples were picked by Bob than Alice?
- How many more apples were picked by David than Carol?

GRAPHS

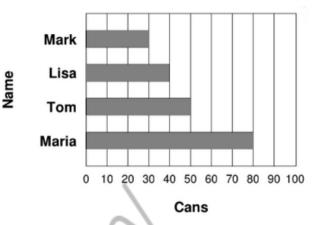
The graph to the right shows the number of candy bars sold for a fundraiser.



- How many more candy bars were sold by Mary than David?
- How many candy bars were sold by David and James combined?
- How many fewer candy bars were sold by James than Mary?
- How many candy bars were sold by James and David combined?
- How many fewer candy bars were sold by Linda than David?
- How many candy bars were sold by Mary and David combined?
- How many fewer candy bars were sold by Linda than Mary?
- How many more candy bars were sold by David than Linda?

GRAPHS

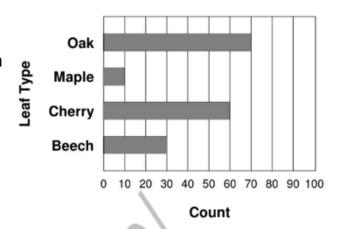
The graph to the right shows the number of cans of food collected for a fund-raiser.



- How many fewer cans of food were collected by Lisa than Maria?
- How many fewer cans of food were collected by Lisa than Tom?
- How many cans of food were collected by Lisa and Mark combined?
- How many more cans of food were collected by Lisa than Mark?
- How many cans of food were collected by Maria and Mark combined?
- How many cans of food were collected by Tom and Lisa combined?
- 7) How many cans of food were collected by Mark and Tom combined?
- How many fewer cans of food were collected by Mark than Maria?

GRAPHS

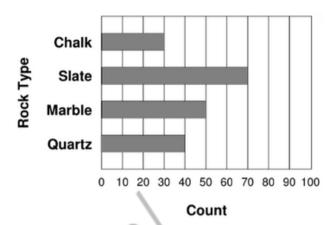
The graph to the right lists different kinds of leaves collected by students in Mrs. Smith's class.



- How many maple and beech leaves were collected in all?
- How many fewer beech leaves were collected than cherry leaves?
- How many cherry and beech leaves were collected in all?
- How many beech and maple leaves were collected in all?
- How many more cherry leaves were collected than maple leaves?
- How many fewer maple leaves were collected than cherry leaves?
- How many cherry and maple leaves were collected in all?
- How many more cherry leaves were collected than beech leaves?

GRAPHS

The graph to the right lists different kinds of rocks collected for a class rock collection.



- How many fewer quartz rocks were collected than marble rocks?
- How many fewer chalk rocks were collected than marble rocks?

- How many chalk and slate rocks were collected in all?
- How many more marble rocks were collected than quartz rocks?

- How many quartz and slate rocks were collected in all?
- How many more marble rocks were collected than chalk rocks?

- How many slate and chalk rocks were collected in all?
- How many more slate rocks were collected than marble rocks?

CHAPTER 5 - NAPLAN

MATERIAL FOR THIS WEEK WILL BE PROVIDED BY YOUR TUTOR IN CLASS

BIRDWATCHING PICTOGRAPH

Pat, Jim, Linda, and Paul went on a bird watching walk. The pictograph below shows how many birds each person saw.

Birdwatching Trip

Name	Number of Birds Seen
Pat	
Jim	2221
Linda	
Paul	

Each prepresents 2 birds

1. How many birds did Pat see?	1
2. How many birds did Jim see?	2
3. How many birds did Paul see?	3
4. How many more birds did Paul see than Linda?	4
5. How many birds did Jim and Pat see together?	5
6. Did Jim see an odd or even number of birds?	6
7. Who saw eleven birds?	7
8. If Jim had seen three more birds, how many symbols	
would be next to his name on the pictograph?	8
9. Who saw fewer birds: Jim or Paul?	9
10. Did Linda see more or less than a dozen birds?	10
11. Tell how you would show 4 birds on the pictograph?	11

12. What is the total number of birds seen by the 4 people? 12. ____

THE CUPCAKE BAKERY

The Cupcake Bakery makes cupcakes and ships them off to supermarkets across the country. The pictograph below shows how many cupcakes they bake each day. Use the information from the graph to answer the questions.

Number of Cupcakes Baked

Monday	
Tuesday	
Wednesday	
Thursday	
Friday	
	4 400

How many	cup calvac wara	hakad an Mandayi) 1
. HOW HIGHY	LUDCAKES WELE	baked on Monday?	·
			· · · ——

- 2. Were more cupcakes baked on Monday or Friday? 2. ______
- 3. On which day were the fewest cupcakes baked?

 3. ______
- 4. How many cupcakes were baked on Tuesday andWednesday combined?4. ______
- 5. How many more cupcakes were baked on Tuesday thanThursday?5. ______
- 6. How many more cupcakes were baked on Friday than

 Wednesday?

 6. ______
- 7. The Cupcake Bakery only makes two kinds of cupcakes: chocolate and white. On Friday, they baked 200 white cupcakes. How many chocolate cupcakes did they bake?
- 8. On Wednesday, the bakery made 100 chocolate cupcakes. How many white cupcakes did they make?

8.			

FISHING TRIP PICTOGRAPH

Michael, Emily, Jose, Jennifer, and Kevin went on a fishing trip. The pictograph below shows how many fish each caught. Use the pictograph to answer the questions.

Number of Fish Caught

Michael	The stand the stand
Emily	the time the time the
Jose	The state of the s
Jennifer	time time time time time
Kevin	and and an

= 6 fish

1. How many fish did Michael catch?	1
2. How many fish did Emily catch?	2
3. How many fish did Kevin catch?	3
4. How many more fish did Emily catch than Jose?	4
5. How many fish did the girls catch?	5
6. How many fish did boys catch?	6
7. How many more fish did the girls catch than the boys?	7
8. How many fish did Jose and Kevin catch?	8
9. Find the sum of the fish caught by all five people?	9
10. Who caught fewer fish, Jennifer or Emily?	10
11. Did Jennifer catch an odd or even number of fish?	11
12 Jose said "Leguaht a dezen fish!" Is he correct? Evolain	12

<u>CHAPTER 6 - PICTO-GRAPH (PROBABILITY)</u> LEMONADE STAND PICTURE GRAPH

Doreen was having a lemonade stand in her front yard. The picture graph below shows how much she earned.

Lemonade Stand Profits

Day	Money Earned							
Friday	\$ \$	\$	\$	\$				
Saturday	\$ \$	\$	\$	\$	\$	\$		
Sunday	\$ \$	\$				7	//	
Monday	\$ \$					/	,	

\$ = five dollars

1. How much money did Doreen earn on Friday?	1
2. How much did she earn on Sunday?	2
3. How much money did she earn on Saturday and Sunday?	3
4. How much more did Doreen earn on Saturday than Friday?	
5. On which day did Doreen earn the least money?	5.
6. Which day did Doreen earn the most money?	6.
7 How much more did Doreen earn on Saturday than Monday	

THE PUMPKIN CARVING CONTEST

Monica, Wayne, Kiersten, and Derrick were in a pumpkin carving contest. There was a prize for the person who carved the most pumpkins.

Number of Pumpkins Carved

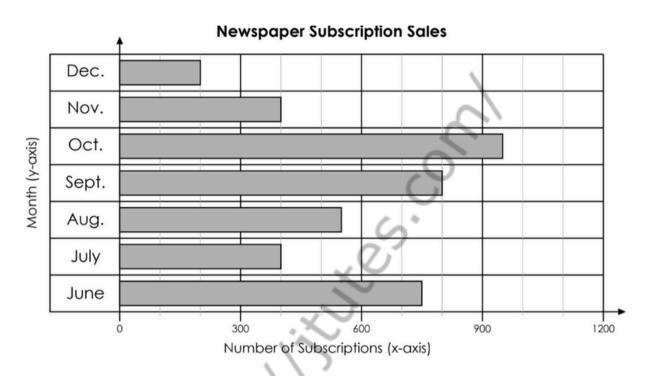
Monica							
Wayne				Ø			
Kiersten							
Derrick					B	/	

(a) = 4 pumpkins	3
1. How many pumpkins did Monica carve?	1
2. How many pumpkins did Monica carve?	2
3. How many pumpkins did Kiersten carve?	3
4. How many pumpkins did Derrick carve?	4
5. How many more pumpkins did Derrick carve than Kiersten?	5
6. How many pumpkins did Monica and Wayne carve in all?	6
7. Which person carved the greatest number of pumpkins?	7
8. Which person carved the least number of pumpkins?	8
9. If Kiersten carved 4 more pumpkins, how many pumpkins would she have carved in all?	9
10. If Monica had carved 6 fewer pumpkins, how many would she have carved?	10
11. How many more pumpkins did Wayne carve than Monica?	11
12. How many pumpkins did the 4 contestants carve altogether?	12

NEWSPAPER BAR GRAPH

The local newspaper keeps track of how many subscriptions are sold each month.

Use the graph below to answer the questions.



- 1. How many newspaper subscriptions were sold in October?
- 1.
- How many more newspaper subscriptions were sold in November than December? (Show your work in the space below.)
- 2. _____
- 3. Were more newspaper subscriptions sold in October, November, and December, or in July, August, and September?

 (Show your work in the space below.)
- 3. _____

- 4. In April, the newspaper sold 100 fewer subscriptions than they did in June. How many supscriptions did they sell in April?
- 4. _____

BEAN PLANT BAR GRAPH

The students in Mr. Suess' class planted lima bean seeds. After two weeks, the students measured the height of their bean plants and graphed the results.



- 1. Write the height of each student's plant at the end of each bar.
- 2. How much taller did Thomas' plant grow than Dora's?
- 2. _____

3. How much shorter is Thomas' plant than Steve's?

- 3.
- 4. If Steve's plant had only grown half as tall, what would its height be?
- 4. _____
- 5. Thomas said to Dora, "My plant is twice as tall as yours." Is he correct? 5. _______ Explain.

Example 11 Describing chance

Classify each of the following statements as either true or false.

- a It is likely that children will go to school next year.
- b It is an even chance for a fair coin to display tails.

d An event that will never occur is called _

- c Rolling a 3 on a 6-sided die and getting heads on a coin are equally likely.
- d It is certain that two randomly chosen odd numbers will add to an even number.

SOLUTION	EXP	LANA'	LION
----------	-----	-------	------

а	true	Although there is perhaps a small chance that the laws might change, it is (very) likely that children will go to school next year.
b	true	There is a 50-50, or an even chance, of a fair coin displaying tails. It will happen, on average, half of the time.
С	false	These events are not equally likely. It is more likely to flip heads on a coin than to roll a 3 on a 6-sided die.
d	true	No matter what odd numbers are chosen, they will always add to an even number.

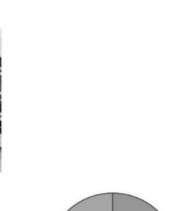
Exercise 8G 1,2 1 —

_					
1	Match each of the events a to d with a description of how likely they are to occur (A to D).				
	a A tossed coin landing heads up.	A unlikely			
	b Selecting an ace first try from a fair deck	A unlikely B likely			
	of 52 playing cards.				
	c Obtaining a number other than 6 if a fair	C impossible			
	6-sided die is rolled.				
	d Obtaining a number greater than 8 if a fair	D even chance			
	6-sided die is rolled.				
2	Fill in the blanks, using the appropriate termine	pology.			
~					
	a If an event is guaranteed to occur, we say it	t is			
	b An event that is equally likely to occur or n	not occur has an			
	c A rare event is considered				

- 3 Consider a fair 6-sided die with the numbers 1 to 6 on it. Answer true or false to each of the following.
 - a Rolling a 3 is unlikely.
 - b Rolling a 5 is likely.
 - c Rolling a 4 and rolling a 5 are equally likely events.
 - d Rolling an even number is likely.
 - e There is an even chance of rolling an odd number.
 - f There is an even chance of rolling a multiple of 3.
- 4 Match up each of the events a to d with an equally likely event A to D.
 - a Rolling a 2 on a 6-sided die
 - b Selecting a heart card from a fair deck of 52 playing cards
 - c Flipping a coin and tails landing face up
 - d Rolling a 1 or a 5 on a 6-sided die
 - A Selecting a black card from a fair deck of 52 playing cards
 - B Rolling a number bigger than 4 on a 6-sided die
 - C Selecting a diamond card from a fair deck of 52 playing cards
 - D Rolling a 6 on a 6-sided die



- 5 Consider the spinner shown, which is spun and could land with the arrow pointing to any of the three colours. (If it lands on a boundary, it is re-spun until it lands on a colour.)
 - a State whether each of the following is true or false.
 - i There is an even chance that the spinner will point to green.
 - ii It is likely that the spinner will point to red.
 - iii It is certain that the spinner will point to purple.
 - iv It is equally likely that the spinner will point to red or blue.
 - V Green is twice as likely to occur as blue.
 - b Use the spinner to give an example of:
 - i an impossible event
 - ii a likely event
 - iii a certain event
 - iv two events that are equally likely



green

blue

red



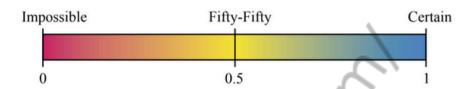
- Discuss the meaning of probability terminology (for example probability, sample space, favourable outcomes, trial, chance events and experiments).
- Construct sample spaces for single-step experiments with equally likely outcomes
- Express probabilities in common and decimal fractional and percentage forms.
- Understand the advantages and limitations of calculating theoretical probabilities.

PROBABILITY

Probability is the chance of something happening.

So many things involve probability.

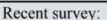
- · Insurance is about probability.
- · Weather prediction is about probability.
- · Gambling is about probability.
- · Even atomic theory is about probability.
- etc., etc., etc.



- 1 Copy the above probability scale and add each of the following to the scale.
 - a) The day after Monday will be Tuesday.
 - b) Next year will have 390 days.
 - c) We will have a new Maths teacher next week.
 - d) I will watch TV tonight.
 - e) I will become the Prime Minister.
 - f) I will drink some milk today.
 - g) It will rain tomorrow.
 - h) I will get my driver's licence before I am 21.
 - i) When a coin is thrown it will land tails up.
 - j) I will send a text message today.
 - k) The next movie I watch will be an action movie.
 - 1) The next person to walk through the door will be a girl.
- 2 Brainstorm each of the following:
 - a) List 3 events in your everyday life that will be certain.
 - b) List 3 events in your everyday life that will be impossible.
 - c) List 3 events in your everyday life that will be approximately fifty-fifty.
 - d) The probability of tossing a coin and getting a head is fifty-fifty, or 0.5 or ½. If a coin is tossed 100 times, will the number of heads be 50?
 - e) The probability of rolling a die and getting a 6 is one-sixth, or 0.17, or ¹/6. If a die is rolled 60 times, will the number of 6s be 10?
 - f) Almost every gambling game involving money is unfair.
 - g) We have Buckley's chance of winning the match.

Next time you get a chance, find out about Buckley's chance.





1 out of 2 people make up 50% of the population.



SAMPLE SPACE

A Sample Space is a complete list of all possible outcomes.

Tossing a coin:

There are two possibilities: head or Tail. The Sample Space is: $S = \{H, T\}$

a) Write the Sample Space for spinning the spinner.



S = {Green, Blue, Red, Yellow}

b) Calculate the probability of getting blue.

Probability of Blue =
$$\frac{1}{4}$$
 = 0.25

c) Spin the spinner 40 times. What fraction of the spins are blue?

G	В	R	Y
13	8	9	10

Fraction Blue =
$$\frac{8}{40}$$
 = 0.20

d) Is your answer to b) and c) different? Which answer is more reliable?

The answers are different. The Sample Space gives the theoretical answer. The spinner is experimental - the more spins, the more likely the answer will be 0.25.

1 a) Write the Sample Space for tossing a coin.



A

- b) Calculate the probability of getting a tail.
- 2 a) Write the Sample Space for throwing a die.
 - b) Calculate the probability of getting a 6.



THEORETICAL PROBABILITY

The probability of an event is the number of favourable outcomes divided by the number of possible outcomes.

Number of favourable outcomes Theoretical Probability = Total number of outcomes

The Sample Space is the complete list of all possible outcomes.

Four balls are numbered 1 to 4. What is the probability of selecting a ball that shows:

- a) 2?
- **b)** even?
- c) >1?

Sample space = $\{1,2,3,4\}$

- a) $P(2) = \frac{1}{4} = 0.25$ {there is one 2}
- **b)** P(even) = $\frac{2}{4}$ = 0.5 {2,4 are even} **c)** P(>1) = $\frac{3}{4}$ = 0.75 {2,3,4 are >1}

A standard 6-sided die is thrown. What is the probability of each of the following happening?

- **b**) odd **c**)

Sample space = $\{1,2,3,4,5,6\}$

- **a)** $P(3) = \frac{1}{6} = 0.17$ {there is one 3} **b)** $P(\text{odd}) = \frac{3}{6} = 0.5$ {1,3,5 are odd} **c)** $P(<4) = \frac{3}{6} = 0.5$ {1,2,3 are <4}
- 1 Four balls are numbered 1 to 4. What is the probability of selecting a ball that shows:



c) >2?

- **b)** odd?
- d) <2?



Five balls are numbered 1 to 5. What is the probability of selecting a ball 2 that shows:

a) 4?

b) even?

c) >3?

3 A six-sided die is thrown. What is the probability of each of the following:

a) 3?

b) even? 5? c) odd? d)

e) <3?

f) >4?

g) >6?

h) a number divisible by 3?

THEORETICAL PROBABILITY

- 4 The numbers 1 to 4 are each written on a piece of paper and placed in a bag. If a piece of paper is drawn from the bag, what is the probability that the number on the paper is:
 - a) 3?

b) even?

c) >3?

d) 5?

- A class raffle is conducted by writing the numbers from 1 to 26 on a piece of paper and placed in a bag. What is the probability that the drawn number is:
 - a) 7?
 - c) odd?
 - e) >20?
 - g) divisible by 3?
 - i) divisible by 5?

- **b)** 20?
- d) even?
- <15?
- h) divisible by 4?
- j) divisible by 6?
- 6 A letter is randomly chosen from the word CHANCE.

What is the probability that the letter is:

- a) a vowel?
- **b)** a consonant?
- c) the letter A?

Vowels are a, e, i, o, u.

A vowel is a sound made with little restriction of the oral cavity.

- 7 A letter is randomly chosen from the word PROBABILITY. What is the probability that the letter is:
 - a) a vowel?
 - b) a consonant?
 - c) the letter A?

Consonants are non-vowels.

A consonant is a sound made with complete or partial closure of the oral cavity.

THEORETICAL PROBABILITY

- 8 A six-sided die is thrown. What is the probability of each of the following?
 - a) 3

b) even

e) odd

d) 5

e) <3

 $\hat{\mathbf{f}}$ >3

 $\mathbf{g}) > 7$

h) a number divisible by 2

- 9 A class raffle is conducted by writing the numbers from 1 to 20 on a piece of paper and placed in a bag. What is the probability that the drawn number is:
 - a) 18?

- b) 2?
- c) odd?
- d) even?
- e) >15?
- **f)** <10?
- g) divisible by 3?
- h) divisible by 4?
- i) divisible by 5?
- j) divisible by 6?

- 10 A letter is randomly chosen from the word LIKELY. What is the probability that the letter is:
 - what is the probability that
 - a) a vowel?
 - b) a consonant?
 - c) the letter L?

THEORETICAL PROBABILITY

- 11 A six-sided die is thrown. What is the probability of each of the following?
 - a) 6

b) even

c) odd

d) 4

e) <4

f) >4

 \mathbf{g}) <1

h) a number divisible by 3

- 12 A class raffle is conducted by writing the numbers from 1 to 30 on a piece of paper and placed in a bag. What is the probability that the drawn number is:
 - a) 28?

- **b)** 2?
- c) odd?
- d) even?
- e) >25?
- f) <10?
- g) divisible by 3?
- h) divisible by 4?
- i) divisible by 5?
- j) divisible by 6?

13 A letter is randomly chosen from the word SPINNER.

What is the probability that the letter is:

- a) a vowel?
- b) a consonant?
- c) the letter S?

EXPERIMENTAL PROBABILITY

If the experiment is fair then with a large number of trials, the experimental probability and the theoretical probability should be similar. $Experimental \ probability = \frac{Number \ of \ successful \ trials}{Total \ number \ of \ trials}$

Experimental probability changes from trial to trial.

- 1 Investigate the experimental probability of heads (and tails) by tossing a coin 50 times. Use a procedure similar to the above example.
- 2 Increase the number of trials from 50 to 500, using a table similar to this table:



	50 throws	500 throws
P(head)	$=\frac{1}{50}=0.$	$=\frac{1}{500}=0.$
P(tail)	$=\frac{1}{50}=0.$	$=\frac{1}{500}=0.$

3 Combine your results with other members of your class. As the number of trials increase, does the experimental probability get closer to the theoretical probability? Theoretical probability of tossing a coin. $S = \{\text{head, tail}\}$ $P(\text{head}) = \frac{\text{Number of favourable outcomes}}{\text{Total number of outcomes}}$ $P(\text{head}) = \frac{1}{2} = 0.5$

EXPERIMENTAL PROBABILITY

A die was tossed 30 times:

| A die was tossed 30 times: | No. of 1s = 4 |
| No. of 2s = 6 |
| No. of 3s = 4 |
| No. of 4s = 4 |
| No. of 5s = 5 |
| No. of 6s = 7 |
| TOTAL = 30 |
| P(1) =
$$\frac{No \text{ of 1s}}{Total \text{ tosses}}$$
 | P(2) = $\frac{No \text{ of 2s}}{Total \text{ tosses}}$ | P(3) = $\frac{No \text{ of 3s}}{Total \text{ tosses}}$ | = $\frac{4}{30} = 0.13$ | P(5) = $\frac{No \text{ of 5s}}{Total \text{ tosses}}$ | P(6) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(7) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(9) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(9) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(1) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(1) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(1) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(2) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(3) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(4) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(5) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(6) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(7) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$ | P(8) = $\frac{No \text{ of 6s}}{Total \text{ tosses}}$

4 Investigate the experimental probability of tossing a die.

Toss a die 60 times. Use a procedure similar to the above example.

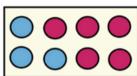
NAPLAN QUESTIONS

1 If the spinner is spun, on which number is the arrow least likely to stop?

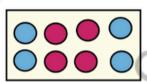


2 From which box does Lin have a 75% chance of selecting a red ball?

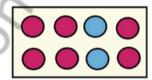
a)



b)



c)

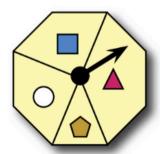


3 The two spinners show a total of 9. If the spinners are spun again, in how many different ways can a total of 7 be obtained?

1 2



- 4 A traffic light is amber and red for 30 seconds. The traffic light is green for 20 seconds. What is the probability that the traffic light is green?
- 5 There are 50 Australian stamps and 30 New Zealand stamps. What is the probability of choosing an Australian stamp?
- 6 A jar of jelly beans contains jelly beans with the following colours: 30 black, 25 white, 25 red and 20 green. What is the chance of picking a white jelly bean.
- A bag contains 50 marbles of which 20 are red, the others are yellow. What is the chance of picking a red marble from the bag?
- **8** Jo spins the arrow 100 times. Which is the most likely table of results?



a)

Shape	Number
	25
	30
	25
0	20

b)

Shape	Number
	25
	35
	15
0	25

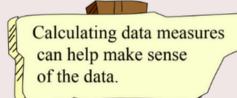
CHAPTER 7 - PROBABILITY NAPLAN QUESTIONS



CHAPTER 8 - STATISTICS
RANGE
MEDIAN
MEAN
MODE
DOT PLOT

- Calculate mean, median, mode and range for sets of data.
- Use ordered stem-and-leaf plots to record and display numerical data.
- Use mean and median to compare data sets and explain how outliers may affect the comparison.
- Locate mean, median and range on graphs and connect them to real life.

DATA MEASURES



The Range

describes the spread of the data.

Range = largest - smallest

Exercise 14.1

Find the range of each of the following set of scores

Range = largest - smallest

Range = 4 - 1

Range = 3

 $\begin{array}{c|cccc} & & & & & \\ \hline & 1 & 2 & 3 & 4 \\ \hline & & Range = 3 & \longrightarrow \end{array}$

- **1** 4, 7, 15, 23, 31, 43
- **3** 2, 7, 2, 6, 3, 2, 6, 7
- 5 232, 235, 236, 232, 231

- **2** 4, 15, 32, 83, 112, 145, 231
- 4 1, 3, 3, 5, 1, 2, 7, 4
- **6** 425, 424, 421, 423, 424, 427

The Mode

describes the middle of the data.

The mode is the score that occurs most often.

Exercise 14.2

Find the mode of each of the following set of scores:

5,	3.	3.	4.	3.	5.	3
-,	-,	-,	٠,	-,	-,	-

Mode = 3 {Occurs 4 times}

2, 5, 8, 5, 4, 2, 1, 3

Mode = 2 and 5 {Twice each}

This set of scores is bimodal

- 1 4, 6, 6, 3, 2, 3, 6
- **3** 2, 5, 2, 1, 6, 1, 1, 5
- **5** 5, 5, 5, 3, 4, 3, 3, 5

- **2** 4, 5, 2, 3, 4, 2, 4, 5
- 4 1, 4, 3, 3, 4, 5, 6, 2
- 6 1, 2, 3, 2, 1, 2, 4, 1

CHAPTER 8 - STATISTICS DATA MEASURES



DATA MEASURES

The Median

describes the middle of the data.

The median is in the middle

Exercise 14.3

Find the median of each of the following set of scores:

Put the scores in ascending order 3, 3, 3, 4, 5, 5, 7

Median = 4

{4 is in the middle }

Put the scores in ascending order 1, 2, 2, 3, 4, 5, 5, 7

Median = 3.5

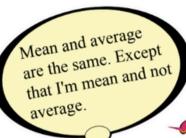
{Average of 3 & 4}

DATA MEASURES

The Mean

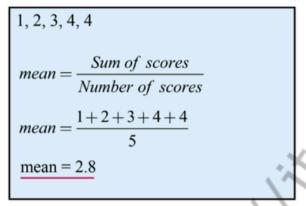
describes the middle of the data.

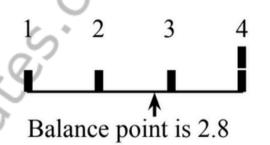
 $mean = \frac{Sum \ of \ scores}{Number \ of \ scores}$



Exercise 14.4

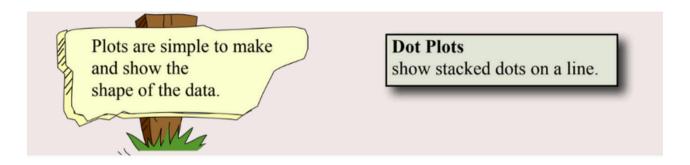
Find the mean of each of the following set of scores:





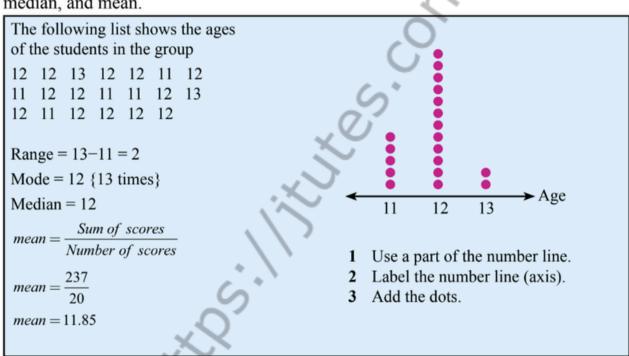
- 1 1, 2, 3, 4, 4, 4
- **3** 1, 1, 2, 2, 3, 4, 4, 4, 4, 4
- 5 31, 36, 36, 32, 32, 33
- **2** 1, 2, 3, 4, 4, 80
- 4 1, 6, 6, 2, 2, 3
- **6** 81, 86, 86, 82, 82, 83

DOT PLOTS



Exercise 14.5

Use a Dot Plot to show the shape of the following data. Also find the range, mode, median, and mean.



DOT PLOTS

1 The ages of students in the group: 12, 13, 13, 12, 13

13, 12, 14, 13, 13

13, 13

2 The test marks (out of 20): 16, 16, 18, 19, 16

17, 18, 19, 18, 17,

16, 18, 18, 17,

3 Each person was asked how many brothers and sisters they have at this school:

0, 0, 2, 1, 3,

1, 0, 1, 2, 1,

0, 1, 0, 1, 2,

1, 0, 0, 1, 0,

0, 1, 0



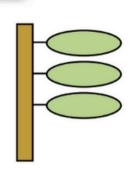
4 The minimum temperature each day for the last fortnight:

$$2, -3, -4, 1, -3, 0, -2, -1, -3, 0, 2, 0, -2, 1$$

STEM AND LEAF PLOTS

Stem and Leaf Plots

show the shape of the data.



	itle
Stem	Leaf Key 3 4 means 34
2	4 6
3	024558
4	1 7
	This number is 25
	This number is 35

Exercise 14.6

Use a stem and leaf plot to represent the following data. Also find the range, mean, mode, and median.

Use a stem and leaf plot to represent the ages of 23 employees of a shire council. Also find the range, mode, median, and mean of the ages.

19 27 34 37 32 49 42 34 25 28 35 56 43 39 23 51 28 32 49 36 34 42 34

First, put the ages in order:

19 23 25 27 28 28 32 32 34 34 34 34 35 36 37 39 42 43 43 49 49 51 56

Then, use the first digit as the ste and the trailing digit as the leaf:

Range =
$$56 - 19 = 37$$

Mode = 34 {34 occurs 4 times}
Median = 34 {the middle number is 34}

$$Mean = \frac{Sum}{Number} = \frac{830}{23}$$
Mean = 36.09

STEM AND LEAF PLOTS

- 1 Scores on the test (maximum of 20): 14, 16, 16, 13, 12, 13, 16
- 2 Number of birds visiting the feeder each day: 34, 35, 42, 43, 34, 32, 44, 35
- 3 Ages of people at the birthday party: 12, 35, 22, 21, 16, 21, 21, 34
- 4 The weights (kg) of the forward pack: 121, 132, 103, 124, 131, 122, 134, 123
- 5 The weekly holiday rents (\$): 519, 522, 517, 516, 522, 522, 518, 522, 528
- 6 The weekly house rents (\$): 348, 349, 352, 349, 351, 352, 350, 351, 349, 351, 348, 350, 356, 345, 349
- 7 The daily solar cell voltage readings: 5.2, 6.1, 5.8, 7.2, 4.6, 4.9, 5.8, 7.3, 5.9, 6.8, 6.2, 5.3, 5.2, 5.2

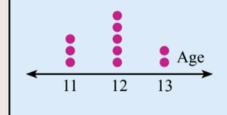
DATA MEASURES FROM A PLOT

Outliers are unusual values.

- · Are they a mistake?
- · Should you delete them?

Exercise 14.8

Given the following plots, find the range, mode, median and mean.



Range =
$$largest - smallest$$

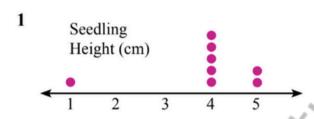
= $13 - 11$

$$= 13$$
 $= 2$

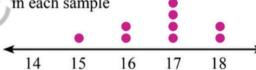
$$= \underline{12}_{sum}$$

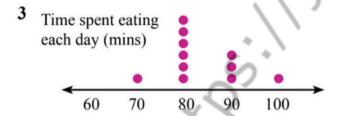
Mean
$$= \frac{sum}{number}$$
$$= \frac{3 \times 11 + 5 \times 12 + 2 \times 13}{10}$$

$$=\frac{119}{10}$$

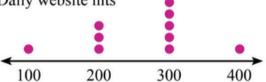


Number of fishlings in each sample





Daily website hits



DATA MEASURES FROM A PLOT

Range = largest - smallest
$$= 100 - 63$$
 $= 100 - 63$ $=$

5	Arm span (14 8 means 148 cm)		6 No. of situps (1 7 means 17)	
	13	1 4	0	6
	14	0 2 2 2 5 8	1	01227
	15	3 7	ن کا کا کا	467778
	16	00	7, 3	3 3 6
	17		4	8
	18	5		

NAPLAN QUESTIONS

Exercise 14.12

- 1 What is the average of 3 and 7?
- 2 What is halfway between $1\frac{1}{2}$ and $2\frac{1}{2}$?
- 3 Find the mean (average) exercise time:

Monday	Tuesday	Thursday	Saturday	Sunday
30 minutes	50 minutes	20 minutes	30 minutes	30 minutes

- **4** Given the scores: 4, 4, 5, 5, 5, 5, 7, 85
 - a) What is the mean, median, and mode?
 - b) What is the mean, median, and mode after 85 is removed?
 - c) Which is affected the most by removing 85, the mean, median, or mode?
- 5 a) Find the mean, median, and mode of the following: 1, 2, 2, 2, 3, 5
 - **b)** Is Mean > Median = Mode true?

After four innings, the average number of runs per innings was 15. After five innings, the average number of runs per innings was 16. How many runs were scored in the fifth innings?

After 4 innings:

$$average = \frac{total}{no innings}$$

$$15 = \frac{\text{total}}{4}$$

Total for 4 innings =
$$15 \times 4$$

= 60

After 5 innings:

$$average = \frac{total}{no innings}$$

$$16 = \frac{\text{total}}{5}$$

Total for 5 innings =
$$16 \times 5$$

$$= 80$$

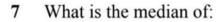
No runs in fifth innings
$$= 80 - 60$$

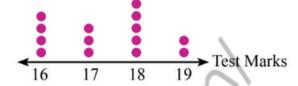
$$= 20$$

NAPLAN QUESTIONS

6 After 4 innings, the average number of runs was 20. After 5 innings, the average number of runs was 25. How many runs were scored in the fifth innings?







- 8 The basketball team of fifteen players need to score at least 75 points to be competitive. What is the average score per player needed to be competitive?
- 9 The basketball team has twelve players with an average player score of 4.5. What total would the team be expected to score?
- 10 Given the scores: 6, 6, 6, 7, 7, 7, 50. Which central measure is affected the most by removing the 50: the mean, median, or mode?

CHAPTER 8 - STATISTICS NAPLAN QUESTIONS



RATIO & RATE

- Use percentages to solve problems, including those involving mark-ups, discounts, profit and loss and GST. Use ordered stemand-leaf plots to record and display numerical data.
- Express profit and loss as a percentage of cost or selling price, compare the difference.
- Investigate the methods used in retail stores to express discounts.

RATIO WARM UP

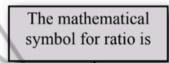
A Ratio is a comparison of two quantities of the same type in the same units.

A ratio can be written as 3: 10, a fraction $\frac{3}{10}$, a decimal 0.3, a percentage 30%

Exercise 11.1

Write the following comparisons as ratios:

18 people passed the test and 5 failed.	
a) What is the ratio of pass to fail?	18:5
b) What is the ratio of fail to pass?	5:18
c) What is the ratio of pass to the total?	18 : 23
d) What is the ratio of fail to the total	5:23





- 1 The Maths class has 9 girls and 14 boys.
 - a) What is the ratio of girls to boys?
 - **b)** What is the ratio of boys to girls?
 - c) What is the ratio of girls to the total number in the class?
 - d) What is the ratio of boys to the total number in the class?

RATIO WARM UP

- 2 Last month there were 24 sunny days and 7 cloudy days.
 - a) What is the ratio of sunny to cloudy days?
 - **b)** What is the ratio of cloudy to sunny days?
 - c) What is the ratio of sunny to the total number of days in the month?
 - d) What is the ratio of cloudy to the total number of days in the month?

RATIO WARM UP

3 Write each of the following ratios as a fraction, a decimal and a percentage:

	fraction	decimal	percentage
1:4	$\frac{1}{4}$	0.25	25%
5:2	<u>5</u> 2	2.5	250%

Make a percentage by multiplying by 100.

- a) 1:2
- **b)** 1:10
- c) 1:4
- d) 3:4h) 4:5

- e) 1:5
- f) 2:5
- g) 2:10

83

RATIO WARM UP

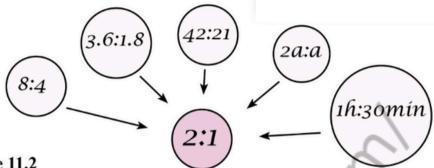
- 4 Write each of the following fractions as a ratio, a decimal and a percentage:
 - **a)** $\frac{1}{2}$
- **b)** $\frac{3}{10}$

c) $\frac{4}{5}$

d) $\frac{1}{4}$

RATIO

When ratios are large or awkward it sometimes helps to simplify them.



Exercise 11.2

Simplify the following ratios:

15:9
$$= \frac{15}{9}$$

$$= \frac{3x \cdot 5}{3x \cdot 3}$$

$$= \frac{5}{3}$$

$$= \frac{9}{11}$$
4.5:5.5
$$= \frac{4.5 \times 10}{5.5 \times 10}$$

$$= \frac{8b}{4b}$$

$$= \frac{8b}{4b}$$

$$= \frac{8b}{4}$$

$$= \frac{8}{4}$$

$$= \frac{2}{1}$$

$$= \frac{2}{1}$$
A calculator is good at simplifying ratios (see

- 1 8:4
- 4 3:9
- 7 2.5:1.5
- 2 3:12
- 5 6:9
- 8 2.4:1.8
- **3** 12:16

Technology 11.1).

- 6 15:5
- 9 5:1.5

RATIO

The rose food is mixed with water in the ratio of 1: 4. How much rose food is needed to make a total mixture of 4 L?

Rose food is 1/5 of the mixture $= 1/5 \times 4$ L = 0.8 L or 800 mL

1 The rose food is mixed with water in the ratio of 1:4. How much rose food is needed to make a mixture of 2 L?

2 The fruit juice is made by mixing juice concentrate and water in the ratio of 1:3. How much juice concentrate is needed to make 2 L of fruit juice?

RATIO

3 The lunch bill for the 7 guests came to \$154. If Amelia paid for 3 of the guests and Jack paid for the other 4 guests, how much did each pay?

4 Sophie paid \$7 towards the Lottery ticket and Noah paid \$3. If the Lottery ticket returned \$30, how much should each receive?

RATIO

5 The concrete is to be made of cement, sand, and gravel in the ratio of 1 : 2 : 3. If the mixer takes 30 shovelfulls, how many shovelfulls of cement is needed?

6 A line 20 cm long is to be divided in the ratio of 1.2 : 1.8, where should the line be divided?

PERCENTAGES

Percentages are used hundreds of thousands of times every day for comparison and analysis.

Calculations often involve finding a percentage of an amount.

1 Write each of the following percentages as a fraction and as a decimal:

$$30\% = \frac{30}{100} = \frac{3}{10}$$
 $= 0.3$
 $112\% = \frac{112}{100}$
 $= 1.12$
 $4.25\% = \frac{4.25}{100}$
 $= 0.0425$

- a) 10%
- **b)** 20%
- c) 30%
- d) 40%

- e) 50%
- f) 60%
- g) 70%
- h) 80%

- i) 90%
- j) 100%
- k) 3%
- I) 5%

PERCENTAGES

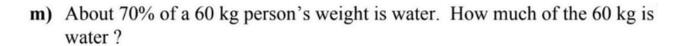
2 Calculate each of the following:

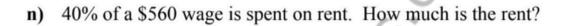
Find 20% of 80	Find 37% of 176	Find $13\frac{1}{5}\%$ of 65
= 0.2 x 80	= 0.37 x 176	= 0.132 x 65
= 16	= 65.12	= 8.58

- a) 25% of 60
- **b)** 10% of 65
- c) 75% of 24
- d) 30% of 70

- e) 50% of 80
- **f)** 40% of 30
- g) 60% of 250
- h) 80% of 25

PERCENTAGES





o) If 27% of a sale is profit, how much profit in a sale of \$4650?

<u>CHAPTER 9 - PROPORTIONS</u> PERCENTAGES

p) Lenny pays 37% tax on an income of \$68 500 pa. How much tax does Lenny pay?

q) The management fund returned 11.5% on an investment of \$74 500. How much was returned?

Add GST (10%) to an item priced at \$37	A discount of 15% is offered on a sub-woofer priced at \$230. What is the new price?
= 37 + 10% of 37	= 230 - 15% of 230
$= 37 + 0.1 \times 37$	$= 230 - 0.15 \times 230$
= \$40.70	= \$195.50

- 1 Add GST (10%) to the price of each of the following items:
 - a) A sandwich @ \$2.40
 - c) A watch @ \$50
 - e) A hotel room @ \$145
 - g) A telephone bill @ \$125
- b) Cable subscription @ \$55
- d) A filing cabinet @ \$240
- f) Haircut @ \$33
- h) Electricity account @ \$171

PERCENTAGES

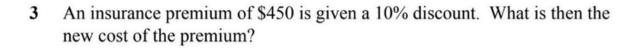
The GST is a tax of 10% on most supplies of goods and services in Australia from 1 July 2000.



- 2 Discount each of the following prices by 25%
 - a) A DVD player @ \$224
 - c) A running shoe @ \$105
 - e) A bedside clock @ \$23
 - g) A calculator @ \$18

- b) A coffee table @ \$119
- d) An MP3 player @ \$275
- f) A ball gown @ \$859
- h) A DVD @ \$27

PERCENTAGES



4 A health insurance fee of \$160 per month is supported by a Federal Government rebate of 30%. What is the fee after the 30% rebate?

5 A car insurance discount of 7.5% is given to drivers 55 and over. What would a 56 year-old actually pay for a car insurance premium of \$350?

CHAPTER 10 - PERCENTAGES PERCENTAGES

6 A fortnightly wage of \$970 is increased by 3.8%. What is the new wage?

7 A fixed deposit of \$5430 is increased by an interest payment of 4.2%. How much money is now in the fixed deposit?

PERCENTAGES

Express profit and loss as a percentage of cost price or selling price.

Mia bought a block of land for \$120 000 and because of financial difficulty, quickly sold the block of land for \$100 000.

Find the loss = 120 000 - 100 000 = \$20 000 = \$20 000 $= 20000 \times 100$ $= 20000 \times 100$ = 16.67%Find the loss as a percentage of the selling price. $= 20000 \times 100$ $= 20000 \times 100$ $= 20000 \times 100$ $= 20000 \times 100$

- 1 Ethan bought a Year 7 maths textbook for \$65 and a year later sold it on ebay for \$23 (after deducting ebay commission and postage costs).
 - a) Find the loss.
 - b) Find the loss as a percentage of the buying price.
 - c) Find the loss as a percentage of the selling price.
 - d) Which percentage loss sounds better as far as Ethan is concerned?

- 2 Ella bought a 2 bedroom unit 12 years ago for \$95 000 and recently sold it for \$280 000 (after deducting selling costs).
 - a) Find the profit.
 - b) Find the profit as a percentage of the buying price.
 - c) Find the profit as a percentage of the selling price.
 - d) Which percentage profit sounds better as far as Ella is concerned?

- 3 A cattle buyer bought a pen of steers from a farmer for \$12 500 and sold them to a feedlot for \$15 000.
 - a) Find the profit.
 - b) Find the profit as a percentage of the buying price.
 - c) Find the profit as a percentage of the selling price.
 - d) Which percentage profit would the buyer mention to the farmer?
 - e) Which percentage profit would the buyer mention to their employer?

- 4 A phone has a retail price of \$85 and a recommended retail price of \$105.
 - a) What is the new price after a discount of 20% off \$85?
 - b) What is the new price after a discount of 30% off \$105?
 - c) Which sounds more impressive? Which is the better deal?

- 5 Find the discounted price of a CD:
 - a) A discount of 20% on the marked price of \$26.
 - b) A discount of 30% on the recommended retail price of \$32.
 - c) Which sounds more impressive? Which is the better deal?

- **6** Find the discounted price of a phone:
 - a) A discount of 15% on the marked price of \$89.
 - b) A discount of 30% on the recommended retail price of \$112.
 - c) Which sounds more impressive? Which is the better deal?



MATERIAL FOR THIS WEEK WILL BE PROVIDED BY YOUR TUTOR IN CLASS