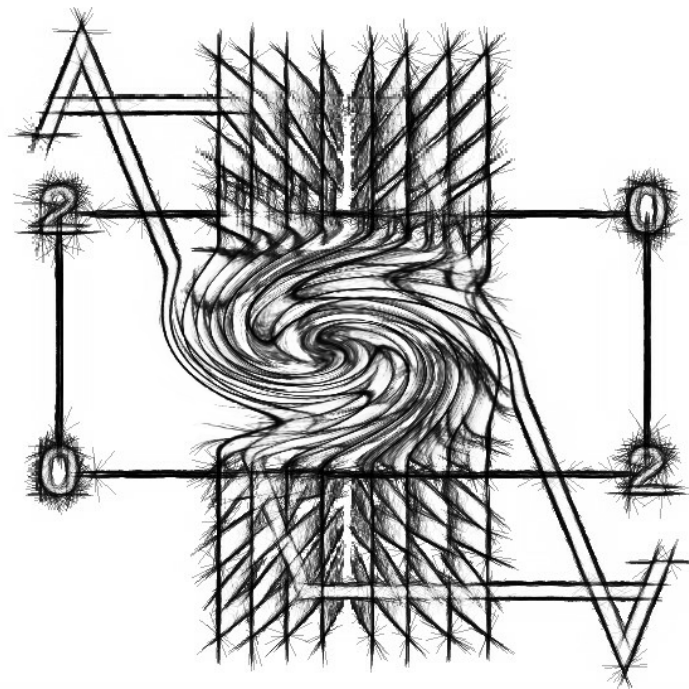
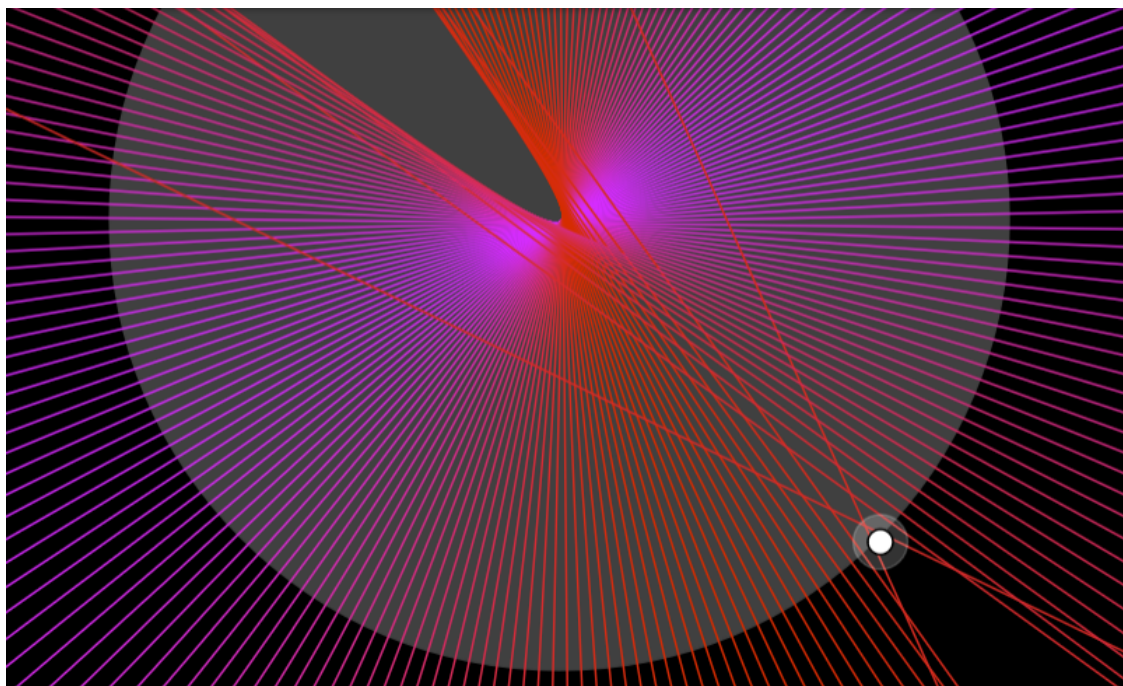
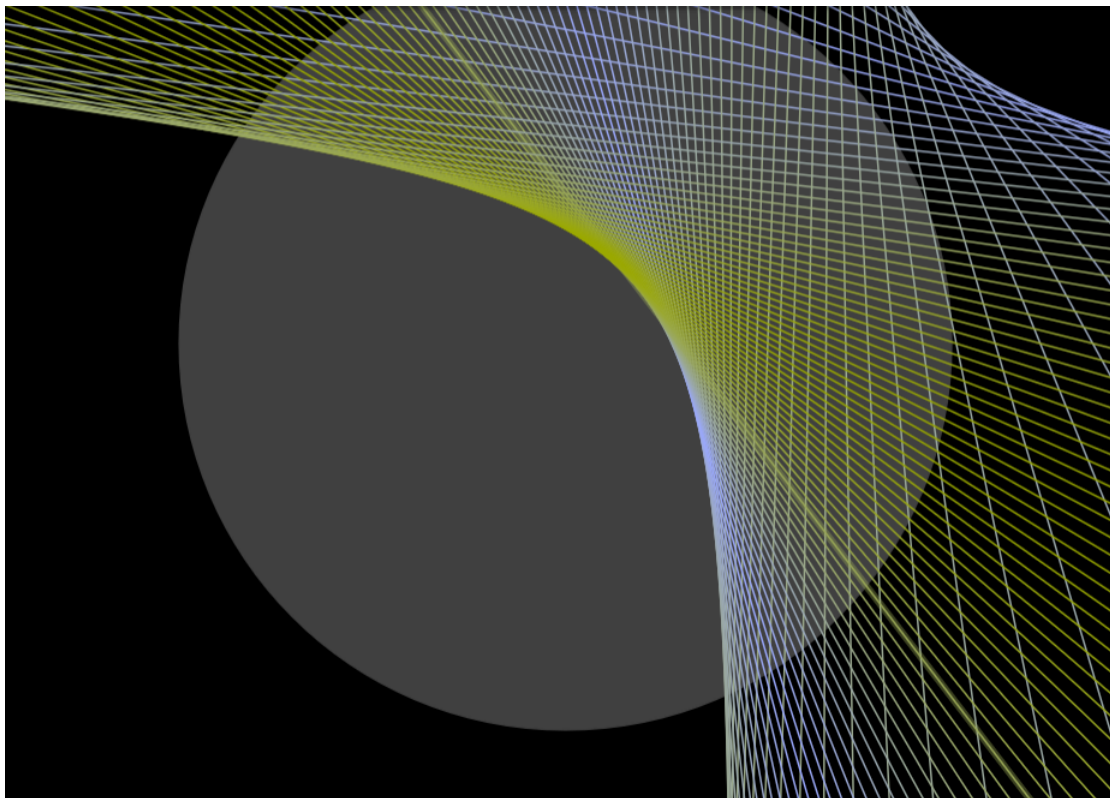

MATHEMATICAL THINKING
AN INVOLUTION FOR ARCHITECTS

ELIAS ZAFIRIS





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In these days the angel of topology and the devil of abstract algebra fight for the soul of every individual discipline of mathematics.

H. WEYL

Historically, architecture was part of mathematics, and in many periods of the past, the two disciplines were indistinguishable. In the ancient world, mathematicians were architects, whose constructions - the pyramids, ziggurats, temples, stadia, and irrigation projects - we marvel at today.

N. A. SALINGAROS