

Mark Scheme

1. Kerjain semua nomor, pasti bisa trigonometry

(a)	$\frac{1}{2} \times 16 \times 5.4 \times \sin 62$ oe 38.14...	M1 A1
(b)	95.6 or 95.64 to 95.65	4 M2 for $\frac{6.7 \times \sin 48}{8.4}$ or M1 for implicit form and M1dep for $180 - 48 - \text{their } 36.4$
(c)	286 or 285.7 to 285.8	5 B1 for [Angle $APB=$] 83° M2 for $180^2 + 245^2 - 2 \times 180 \times 245 \times \cos \text{their } 83$ or M1 for implicit form and A1 for [$AB^2 =$] 81676[.1...] After 0 scored, SC2 for ans 406.87 to 406.88 or 406.9 or 407 if 146° used in cos rule Or SC1 for $180^2 + 245^2 - 2 \times 180 \times 245 \times \cos 146$
2.	130 or 130.0 to 130.1	2 M1 for $\frac{1}{2} \times 22.3 \times 27.6 \times \sin 25$
3.	111.2 or 111.1 to 111.2	4 M2 for [cos =] $\frac{2.8^2 + 3.6^2 - 5.3^2}{2 \times 2.8 \times 3.6}$ or M1 for implicit form A1 for [cos =] -0.362 to -0.361
4.	[0]47	2 B1 for 133 or 47 seen or M1 for $227 - 180$ oe
5.	(a) (i) 275 (ii) 095 (b) 464.66 to 464.67 [= 464.7] (c) 44.9 or 44.86 to 44.87...	2 M1 for $360 - 40 - 45$ oe 2FT FT <i>their</i> (a) $- 180$ M1 for <i>their</i> (a) $- 180$ oe or $180 - 40 - 45$ 4 M2 for $510^2 + 720^2 - 2 \times 510 \times 720 \cos 40$ or M1 for correct implicit equation A1 for 215 900 to 215 920 3 M2 for $\frac{510 \sin(40)}{464.7}$ or M1 for correct implicit equation

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6.

(a) 20.1 or 20.07 to 20.08

(b) 5.86 or 5.858.....

2 **M1** for $\frac{1}{2} \times 7 \times 10 \times \sin 35$ oe

4 **M2** for $7^2 + 10^2 - 2 \times 7 \times 10 \times \cos 35$
A1 for 34.3 ..

or

M1 for $\cos 35 = \frac{7^2 + 10^2 - AC^2}{2 \times 7 \times 10}$

7.

(a) 126 or 126.4 to 126.5

(b) 99.9 or 99.86 to 99.87

(c) 92.6 or 92.58 to 92.59

(d) 115.1 or 115.0 to 115.1

(e) 19700 or 19708 to 19720

3 **M2** for $\sqrt{220^2 - 180^2}$ oe
or **M1** for $BC^2 + 180^2 = 220^2$ oe

4 **M2** for $180^2 + 170^2 - 2 \times 180 \times 170 \cos 33$
or **M1** for $\cos 33 = \frac{180^2 + 170^2 - CD^2}{2 \times 180 \times 170}$

A1 for 9970 or 9973 to 9974

2 **M1** for $\frac{\text{dist}}{170} = \sin 33$ oe

3 **M1** for $\cos = \frac{180}{220}$ oe

M1dep for $47 + 33 + \text{their angle } BAC$

3 **M1** for $0.5 \times 180 \times 170 \times \sin 33$ oe
or $0.5 \times 180 \times \text{their (c)}$ oe
M1 for $0.5 \times 180 \times \text{their (a)}$ oe
or $0.5 \times 180 \times 220 \times \sin(\text{their } BAC)$ oe

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8.

(a)	$\frac{240 \sin 85}{\sin 50}$ <p>312 or 312.1</p>	<p>M2</p> <p>B1</p>	<p>or M1 for $\frac{\sin 50}{240} = \frac{\sin 85}{AB}$ oe</p>
(b)	$\frac{1}{2} \times 180 \times 240 \times \sin A = 12000$ <p>33.748 to 33.749</p>	<p>M1</p> <p>A2</p>	<p>A1 for $\sin = \frac{24000}{43200}$ or better or 0.555 or 0.556 or 0.5 or 0.5555 to 0.5556</p>
(c)	<p>328 or 328.3 to 328.5</p>	<p>5</p> <p>M2</p>	<p>B1 for [angle $A =$] 78.75 seen</p> <p>$180^2 + (\text{their } AB)^2 - 2 \times 180 \times \text{their } AB \times \cos 78.75$ or M1 for $\cos 78.75 = \frac{180^2 + (\text{their } AB)^2 - x^2}{2 \times 180 \times (\text{their } AB)}$ A1 for 107 800 to 107 900</p>
(d) (i)	<p>108.75 or 108.7 or 108.8</p>	<p>1</p>	
(ii)	<p>288.75 or 288.7 or 288.8</p>	<p>2FT</p>	<p>FT 180 + <i>their</i> (d)(i) M1 for 180 + <i>their</i> (d)(i) or 360 – (180 – <i>their</i>(d)(i))</p>

9.

(a)	<p>[cos$ABL =$] $\frac{40^2 + 61.1^2 - 92.1^2}{2 \times 40 \times 61.1}$</p> <p>130.11...</p>	<p>M2</p> <p>A2</p>	<p>M1 for correct implicit version</p> <p>A1 for [cos$ABL =$] -0.644... or $-\frac{7873}{12220}$ or $-\frac{3149.2}{4888}$</p>
(b)	<p>[0]59.5 or 59.50 to 59.511</p>	<p>4</p> <p>M2</p> <p>M1</p> <p>and</p> <p>A1</p>	<p>or $\frac{40 \sin 130.1}{92.1}$ or $\frac{61.1 \sin 130.1}{92.1}$ or $\frac{\sin A}{40} = \frac{\sin 130.1}{92.1}$ or $\frac{\sin L}{61.1} = \frac{\sin 130.1}{92.1}$ or 19.39 to 19.4... or 30.48 to 30.49...</p>

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(c)	1h 50min	<p>5 M2 for $[BC =] 2 \times 40 \times \cos(180 - 130.1)$ oe or M1 for $\frac{x}{40} = \cos(180 - 130.1)$ oe</p> <p>OR M2 for $[BC =] \sqrt{40^2 + 40^2 - 2 \times 40 \times 40 \cos(\text{their } 80.2)}$ or M1 for correct implicit version</p> <p>OR M2 for $[BC =] \frac{40 \sin(\text{their } 80.2)}{\sin 49.9}$ or M1 for correct implicit version</p> <p>and M1 for $\frac{\text{their } BC}{28}$ A1 for 1.84[0...] to 1.841</p>
10.		
(a)(i)	290	2 M1 for $180 + 110$ oe
(a)(ii)	156.8 or 156.7[9..]	<p>5 B1FT for $CBA = 10^\circ$ (<i>their (a)</i> – 280) and B3 for [angle $ACB =$]13.2° or M2 for $[\sin C] = \frac{50 \sin(\text{their } 10)}{38}$ or M1 for $\frac{50}{\sin C} = \frac{38}{\sin(\text{their } 10)}$ oe</p>

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(a)(iii)	8.68 or 8.677 to 8.684	3	M2 for $[x =]50\sin(\text{their}10)$ oe or M1 for $\sin(\text{their}10) = \frac{x}{50}$ oe or M1 for a correct right-angled triangle drawn with 50 as hypotenuse
3(b)(i)	$x(x - 25) = 2200$	1	and no errors seen
3(b)(ii)	$\frac{-(-25) \pm \sqrt{(-25)^2 - 4(1)(-2200)}}{2(1)}$ or better	B2	B1 for $\sqrt{(-25)^2 - 4(1)(-2200)}$ or better or for $\left(x - \frac{25}{2}\right)^2$ oe or B1 for $\frac{-(-25) + \sqrt{q}}{2(1)}$ or $\frac{-(-25) - \sqrt{q}}{2(1)}$ or both or for $\frac{25}{2} + \text{or} - \sqrt{\left(\frac{25}{2}\right)^2 + 2200}$
	-36.04 and 61.04 final answer	B1,B1	If B0B0, SC1 for values in ranges -36.042 to -36.041 and 61.041 to 61.042 seen or for answers -36[.0] or -36.042 to -36.041 and 61[.0] or 61.041 to 61.042 or -36.04 and 61.04 seen in working or for -61.04 and 36.04 as final ans

11.

(a)	1120 or 1121.	4	M2 for $[AC^2 =]$ $525^2 + 872^2 - 2 \times 525 \times 872 \times \cos 104$ or M1 for implicit version A1 for 1257000 to 1258000
(b)	$[QB \text{ or } x =] 872 \times \tan 1$ seen	M2	M1 for $\tan 1 = \frac{QB}{872}$
	$\tan = \text{their } QB \div 525$	M1	
	1.7 or 1.660 to 1.661 nfw	A1	dep on M3
3(c)(i)	222000 or 222100. or 222101	2	M1 for $\frac{1}{2} \times 525 \times 872 \times \sin 104$
3(c)(ii)	5.55 or 5.550 to 5.553 nfw	2FT	FT <i>their</i> (c)(i) $\times 100^2 \div 20000^2$ M1 for <i>their</i> (c)(i) $\times 100^2 \div 20000^2$ or restart

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12.

73.6 or 73.63 to 73.64

4 **B3** for 27.4 or 27.36...
OR
M2 for $\frac{5.9 \sin 79}{12.6}$ oe
or **M1** for $\frac{\sin[C]}{5.9} = \frac{\sin 79}{12.6}$ oe
and **M1dep** for $180 - 79 - \text{their } C$ (dep on at least **M1** earned)

13.

(a)	$12.5^2 = x^2 + 8.5^2 - 2 \times x \times 8.5 \cos 60$ oe isw	M2	M1 for $\cos 60 = \frac{x^2 + 8.5^2 - 12.5^2}{2 \times x \times 8.5}$
	$156.25 = x^2 + 72.25 - 8.5x$	A1	or better
	$2x^2 - 17x - 168 = 0$	A1	with no errors or omissions
(b)	$\frac{[- -]17 \pm \sqrt{([- -]17)^2 - 4(2)(-168)}}{2 \times 2}$	2	B1 for $\sqrt{([- -]17)^2 - 4(2)(-168)}$ or better seen and if in form $\frac{p + or - \sqrt{q}}{r}$ B1 for $p = [- -] 17$ and $r = 2 \times 2$
	14.35, -5.85 final answers	1, 1	SC1 for 14.352 to 14.353 and -5.853 to -5.852 seen or 14.3 or 14.4 and -5.8 or -5.9 as final answers or -14.35 and 5.85 as final answers or 14.35 and -5.85 seen in working
(c)	12.2 or 12.17... nfw	3	M2 for $\frac{\text{their } 14.35 \times \sin 46}{\sin 58}$ or M1 for $\frac{\sin 46}{CD} = \frac{\sin 58}{\text{their } 14.35}$
(d)	138 or 137.5 to 137.8 nfw	3	M1 for $0.5 \times \text{their } 14.35 \times 8.5 \sin 60$ M1 for $0.5 \times \text{their } 14.35 \times \text{their } 12.2 \times \sin 76$

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14.

(a)	7040 or 7035. ...	3	<p>M1 for $\frac{1}{2} \times 100 \times 70$ oe</p> <p>M1 for $\frac{1}{2} \times 100 \times 110 \times \sin 40$ oe</p>
(b)	374 or 375 or 374.4 to 374.5....	5	<p>M2 for $110^2 + 100^2 - 2 \times 110 \times 100 \times \cos 40$ oe or M1 for implicit form A1 for 5250 or 5247. ... (or 72.4 or 72.43 to 72.44) M1 for $70^2 + 100^2$</p>
(c)	64.3 or 64.27 to 64.28 nfw	2	<p>M1 for $\sin 40 = \frac{\text{distance}}{100}$ oe</p>
(d)	235	3	<p>B2 for [angle $ACB =$] 34.99 to 35 or [angle $ABC =$] 55[.0...] or M1 for $\tan[ACB] = \frac{70}{100}$ or $\tan[ABC] = \frac{100}{70}$ or equivalent trig ratio</p>

15.

(a)	370 or 370.2 to 370.3	2	<p>M1 for $864 \div \text{their time}$</p>
(b)	991 or 990.5 ...	4	<p>M2 for $864^2 + 928^2 - 2 \times 864 \times 928 \cos 67$ or M1 for correct implicit version A1 for 981100 to 981110</p>
(i)	313	2	<p>M1 for $180 + 133$ or $360 - 47$</p>
(ii)	[0]79.5 to [0]79.6 ...	4	<p>M2 for $\frac{928 \times \sin 67}{\text{their } 991}$ or $\frac{864 \times \sin 67}{\text{their } 991}$ oe or M1 for implicit form of either</p> <p>A1 for [angle $HGB =$] 59.5 to 59.6 ... or [angle $HBG =$] 53.4 or 53.37 to 53.42</p> <p>M1 dep for <i>their</i> angle $HGB + 20$ leading to answer or for $133 - \text{their angle } HBG$ leading to answer</p>

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16.

(a)	52[.0] or 52.02...	4	<p>M2 for $[\cos =] \frac{13^2 + 4^2 - 11^2}{2 \times 13 \times 4}$ or M1 for $11^2 = 13^2 + 4^2 - 2 \times 13 \times 4 \cos(\dots)$ A1 for $[\cos^{-1} =] \frac{64}{104}$ oe or 0.615 or 0.6153 to 0.6154</p>
(b)	62.7 or 62.69 to 62.70	4	<p>M3 for $180 - \sin^{-1}\left(\frac{8 \sin 80}{13}\right) - 80$ oe or M2 for $\sin A = \frac{8 \sin 80}{13}$ or M1 for $\frac{13}{\sin 80} = \frac{8}{\sin A}$ oe A1 for 37.3 or 37.30... If 0 scored, M1 for $180 - 80 - \text{their } A$</p>
(c)	66.7 or 66.68 to 66.71	3	<p>M1 for $0.5 \times 13 \times 4 \times \sin(\text{their } ACB)$ oe M1 for $0.5 \times 8 \times 13 \times \sin(\text{their } ACD)$ oe</p>

17.

19.3 or 19.26 to 19.27 nfw	3	<p>M2 for $[\sin =] 5.9 \times \frac{\sin 84.6}{17.8}$ or M1 for $\frac{5.9}{\sin B} = \frac{17.8}{\sin 84.6}$ oe</p>
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18.

(a)(i)	116.6 or 116.56 to 116.57	4	<p>M1 for $\sin[EAD] = \frac{6}{12}$ oe M1 for $\tan[BAC] = \frac{6}{12}$ oe B1 for $[\text{angle } DAC] = 60$</p>
a)(ii)	13.4 or 13.41 to 13.42	2	<p>M1 for $12^2 + 6^2$</p>
a)(iii)	10.4 or 10.39...	3	<p>M2 for $\sqrt{12^2 - 6^2}$ or M1 for $AE^2 + 6^2 = 12^2$</p>
a)(iv)	130 or 129.5... to 129.6	4	<p>M1 for $0.5 \times 6 \times \text{their } AE$ oe M1 for $0.5 \times 12 \times 12 \times \sin 60$ oe M1 for $0.5 \times 6 \times 12$ oe</p>

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19.

3(a)	356 or 356.2 to 356.3	4	B1 for [Angle LPM] = 74 soi M2 for $\frac{248 \times \sin \text{their } 74}{\sin 42}$ oe or M1 for implicit statement
b)(i)	320 or 319.9 to 320.2...	3	B1 for angle PLM = 64 soi or for angle between LM and perpendicular from M = 26 soi or [PM =] 333.[1...] M1 for <i>their</i> $356 \times \sin \text{their } 64$ oe or <i>their</i> $356 \times \cos \text{their } 26$ oe
b)(ii)	02 57 or 2 57 am	3	B2 for 6 hours 12 mins or 372 mins seen or M1 for $248 \div 40$ oe If 0 scored, SC1 for <i>their</i> time in hours converted to hours and minutes

20.

(a)	4.29 or 4.285 to 4.286	3	M2 for $\frac{150}{\frac{450}{3.6} - \frac{120}{4} - \frac{180}{3}}$ or M1 for [time =] $120 \div 4$ or $180 \div 3$ or $450 \div 3.6$ or $3.6 = \frac{150 + 180 + 120}{\text{total time}}$
(b)	82.8 or 82.81 to 82.82 using cosine rule	4	M2 for $\frac{150^2 + 120^2 - 180^2}{2 \times 150 \times 120}$ or M1 for $180^2 = 120^2 + 150^2 - 2 \times 120 \times 150 \cos(\dots)$ A1 for $\frac{4500}{36000}$ oe
c)(i)	127.2 or 127.1 to 127.2 or 127	1	FT 210 – <i>their</i> (b)
c)(ii)	307.2 or 307.1 to 307.2 or 307	2	FT 180 + <i>their</i> (c)(i) M1 for $180 + \text{their (c)(i)}$
(d)	15 or 14.99 to 15.04	2	M1 for $\cos(\text{their (b)}) = \frac{\text{dist}}{120}$ oe

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21.

(a)(i)	13.9[0...] from cosine rule	4	M2 for $8^2 + 13^2 - 2 \times 8 \times 13 \cos 79$ or M1 for $\cos 79 = \frac{13^2 + 8^2 - BC^2}{2 \times 8 \times 13}$ A1 for 193
(a)(ii)	66.6 or 66.60... to 66.65 from sine rule	3	M2 for $[\sin ACB =] \frac{13 \times \sin 79}{\text{their}(a)(i)}$ or M1 for $\frac{\sin ACB}{13} = \frac{\sin 79}{\text{their}(a)(i)}$ oe
(b)(i)	$\frac{1}{2}(x+4)(4x-5)\sin 30 = 70$	M1	
	$4x^2 + 16x - 5x - 20 = 280$	M2	Dep on M1 B1 for $4x^2 + 16x - 5x - 20$ or better
	Leading to $4x^2 + 11x - 300 = 0$	A1	with no errors or omissions seen
(b)(ii)	$\frac{-11 \pm \sqrt{11^2 - 4 \times 4 \times -300}}{2 \times 4}$	B2	B1 for $\sqrt{11^2 - 4(4)(-300)}$ or better or for $\frac{-11 + \sqrt{q}}{2 \times 4}$ or $\frac{-11 - \sqrt{q}}{2 \times 4}$
	-10.14 and 7.39	B2	B1 for each or SC1 for final answers -10.1 or -10.144 to -10.143 and 7.4 or 7.393 to 7.394 or -10.14 and 7.39 seen in working or for -7.39 and 10.14 as final answer
(b)(iii)	11.4 or 11.39...	1	FT <i>their</i> positive root + 4

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22.

(a)	36.8 or 36.84...	2	M1 for $\frac{h}{107} = \tan 19$ or $\frac{h}{\sin 19} = \frac{107}{\sin 71}$ oe or better
(b)	42.1 or 42.12... from cosine rule	4	M2 for $[\cos BAC =] \frac{158^2 + 132^2 - 107^2}{2 \times 158 \times 132}$ or M1 for implicit version A1 for $[\cos BAC =] \frac{30939}{41712}$ or 0.7417...
(c)	35.8 or 35.84... from sine rule	3	M2 for $\frac{86 \times \sin 116}{132} [= 0.58557...]$ or M1 for $\frac{\sin CAD}{86} = \frac{\sin 116}{132}$ oe
(d)	9670 or 9669 to 9676	3	M2 for $\frac{1}{2} \times 158 \times 132 \times \sin(\text{their (b)})$ oe and $\frac{1}{2} \times 86 \times 132 \times \sin(64 - \text{their (c)})$ oe or M1 for either area
(e)	214.2 or 214.1... or 214	2	M1 for $[180 +]70 - \text{their (c)}$ oe

23.

(a)(i)	$180 - 60 - 39 [= 81]$	1	
(a)(ii)	147 or 147.1...	3	M2 for $\frac{129 \sin(81)}{\sin 60}$ oe or M1 for $\frac{\sin(81)}{CD} = \frac{\sin 60}{129}$ oe
(a)(iii)	$[\cos =] \frac{85^2 + 129^2 - 72^2}{2 \times 85 \times 129}$	M2	M1 for $72^2 = 85^2 + 129^2 - 2 \times 85 \times 129 \cos ABD$
	31.58...	A2	A1 for 0.851 to 0.852 or $\frac{9341}{10965}$ or equivalent fraction
(a)(iv)	44.5 or 44.51 to 44.54	3	M2 for implicit correct method e.g. $\frac{d}{85} = \sin 31.6$ oe or M1 for recognition that the line from <i>A</i> is perpendicular to <i>BD</i>
(a)(v)	247 or 247.4...	2	M1 for $180 + (180 - 81 - 31.6)$ oe or for $\angle NBC = 180 - 81 - 31.6$ oe or for $\angle NCB = 81 + 31.6$ oe