

$\sqrt{ch, k}$

✓ Rainbow

## ● 計數機玩法：[Prog A2] Quadratic Functions 二次函數

Program A2. [4合] Quadratic Functions 二次函數 (95 bytes)	
MODE : 2 (CMPLX)	
ClrMemory : ? → A : ? → B : ? → M : B <sup>2</sup> - 4AM → D ▲ -B ∙ ( 2A → C ▲ -D ∙ ( 4A ▲ AC <sup>2</sup> M ∙ : C +	46
$\sqrt{(-M - A \rightarrow X \blacktriangle 2C - X \rightarrow Y \blacktriangle MM : C \blacktriangle \pi : Sci 8 : While Ans \neq Rnd(Ans M + : \sqrt{(D - M : 95$	83
WhileEnd : Norm 1 : Ans ∙ (2A ▲ M	

輸入

顯示

$$\Delta = \boxed{\quad}$$

Vertex 頂點 = ( $\boxed{\quad}$ ,  $\boxed{\quad}$ )

$$\boxed{\quad}x^2 + \boxed{\quad}x + \boxed{\quad} = 0 \quad \downarrow \quad x = \boxed{\quad} \text{ or 或 } \boxed{\quad}$$

$$x = \boxed{\quad} \pm \boxed{\quad} \sqrt{\boxed{\quad}}$$

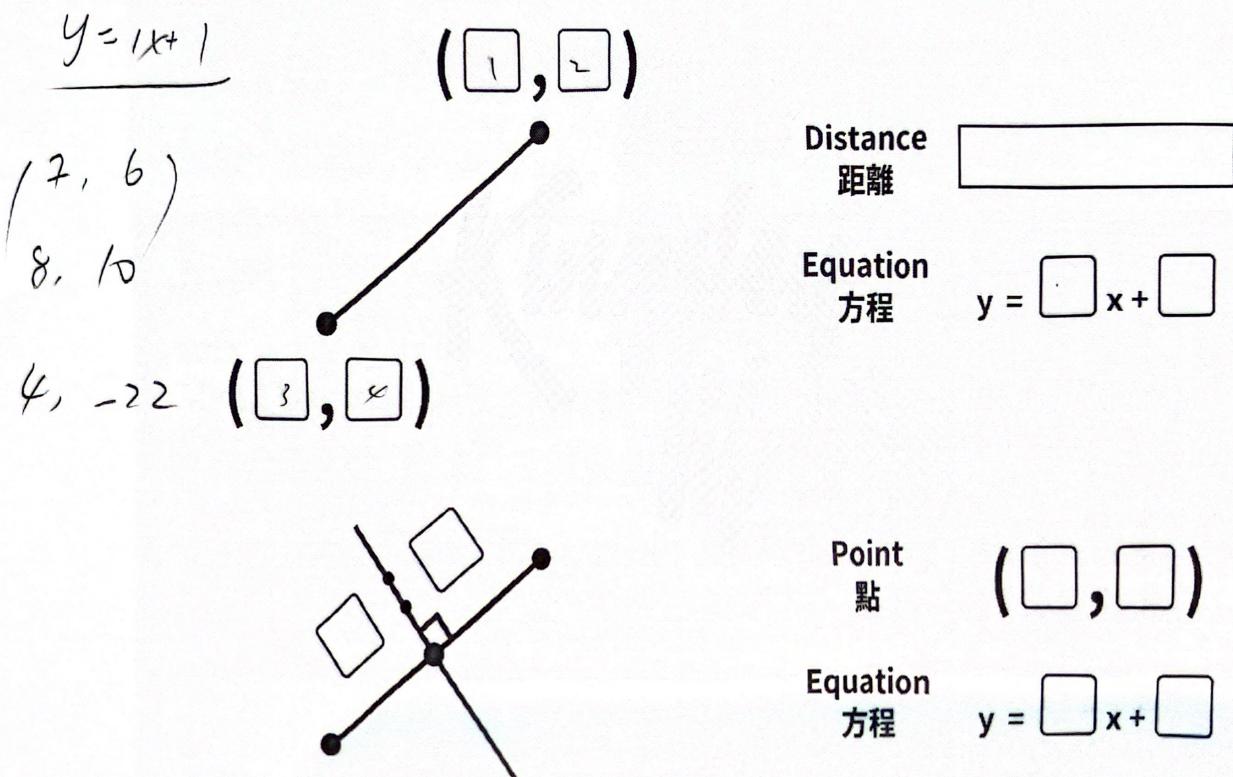
ChunMan X


● 計數機玩法：【Prog B1】Equations of Straight Lines 直線方程

Program B1. 【7合1】 Equations of Straight Lines 直線方程 (105 bytes)	
MODE : 1 (COMP)	
ClrMemory : ? → A : ? → B : ? → C : ? → D : Pol( A - C, B - D ▲ (B - D) - (A - C → M ▲ B - Ans	43
A ▲ ? → X : ? → Y : (AY + CX) - (X + Y → X ▲ Ans M + B - AM → Y ▲ -1 - M ▲ Y - Ans X ▲	88

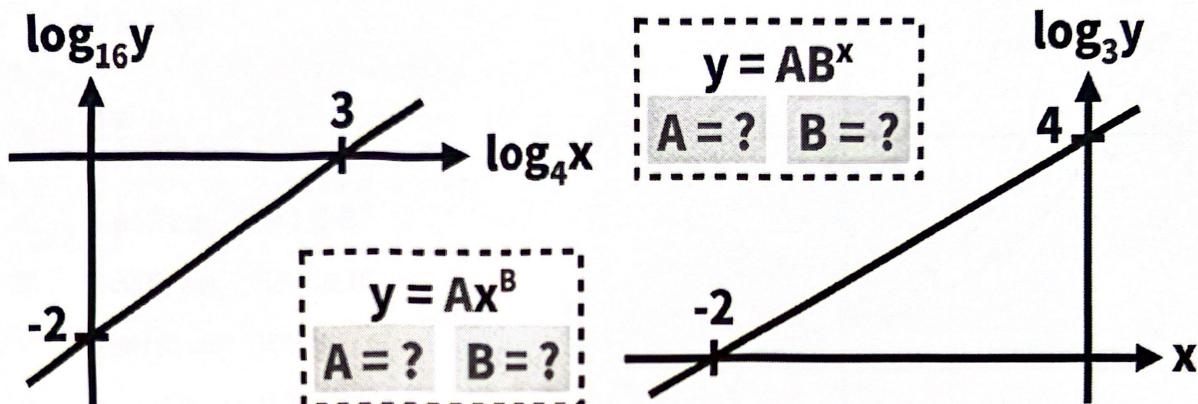
輸入

顯示



### 計數機玩法：【Prog C1】Log Transformation 對數變換

Program C1. Logarithmic Transformation 對數變換 (77 bytes)	
MODE : 1 (COMP)	
ClrMemory : ? → X : ? → Y : ? → A : ? → B : ? → C : ? → D : (B - D) ← (A - C → M : If X = 0 : Then	45
Y ^ (B - AM) ▲ Y ^ (M ▲ Else X ^ ((B - AM) ← log(Y, X ▲ M ← log(Y, X	77



☛ Kingsley方法：神級計數機程式

x底 y底 點 點  
  (, ) (, )

<b>A</b>	<b>B</b>

☛ Kingsley方法：神級計數機程式

x底 y底 點 點  
  (, ) (, )

<b>A</b>	<b>B</b>

Prog A4(A)

## ● 計數機玩法：【Prog A4】ASGS 等差等比數列

Program A4. 【12合1】ASGS 等差等比數列 (306 bytes)	
MODE : 1(COMP)	
ClrMemory : ? → A : ? → B : ? → X : ? → C : ? → Y : ? → M : If A = 1 : Then (X - Y) ← (B - C → D)	44
▲ X - BD + D → A ▲ A + DM - D ▲ AM + DM(M-1) ← 2 ▲ D ▲ A - D ▲ D ← 2 ▲ A - D ← 2 ▲	90
IfEnd : If A = 2 : Then (X ← Y) ^((B - C)^-1 → D : IfEnd : If sin(90(B - C)) = 0 : Then Goto 9 : Else	133
② Goto 8 : Lbl 8 : D ▲ X ← (D ^((B - 1) → A ▲ AD ^((M - 1 ▲ A(1 - D ^((M)) ← (1 - D ▲ IfEnd : If	178
③ Abs(D) ≥ 1 : Then 0^-1 : Else A ← (1 - D ▲ Lbl 9 : D ▲ -D ▲ X ← (D ^((B - 1 → A ▲ X ← ((-D) ^((B -	225
④ 1 → B ▲ AD ^((M - 1 ▲ B(-D) ^((M - 1 ▲ A(1 - D ^((M)) ← (1 - D ▲ B(1 - (-D) ^((M)) ← (1 + D	278
⑤ ▲ If Abs(D) ≥ 1 : Then 0^-1 : Else A ← (1 - D ▲ B ← (1 + D ▲ IfEnd	306

輸入

顯示

Step 0.

選擇功能

1. AS 等差數列 : 1

2. GS 等比數列 : 2

common

d =

 $a_1 =$  $a_1 = \boxed{-1}$  $a_x =$  $a_2 = \boxed{5}$  $S_x =$  $a_x = ?$  $n_{term} \leftarrow a_n = \boxed{2} n + \boxed{19}$  $\text{sum of } n_{term} \leftarrow S_n = \boxed{1} n^2 + \boxed{18} n$

● 計數機玩法：【Prog A4】ASGS 等差等比數列

輸入

顯示

選擇功能

1. AS 等差數列：1  
2. GS 等比數列：2

 $r =$  $a_1 =$  $a_{\square} = \square$  $S_{\square} =$  $S_{\infty} =$  $a_{\square} = \square$  $a_{\square} = \square$  $a_{\square} = ?$ 

輸入

顯示

選擇功能

1. AS 等差數列：1  
2. GS 等比數列：2

可能性 1

可能性 2

 $r =$  $a_1 =$  $a_{\square} = \square$  $S_{\square} =$  $S_{\infty} =$  $a_{\square} = \square$  $a_{\square} = \square$  $a_{\square} = ?$

## ● 計數機玩法：[Prog B2] Equations of Circles 圓方程

```

Program B2. [3合1] Equations of Circles 圓方程 (199 bytes)

MODE : 2 (CMPLX)

ClrMemory: ? → A: ? → Y: ? → C: ? → M: ? → If A = i: Then -2Y ▶ -2C ▶ C² + Y² - M² ▶ IfEnd : 43
If A = π: Then arg( C - M ) - arg( C - M - (1 - j) ) < Ans x( C - Y ) / j ▶ sin( Ans ) ▶ Abs( Y - Ans ) 84
IfEnd: If A = e: Then ? → X: ? → B: BCY + 2YM - XC² → X: ? → A: M² + AC² + BCM → A: 132
( √( X² - 4AC² - 4AY² ) + X ) → ( 2C² + 2Y² → A ▶ ( M - Ans Y ) → C → B ▶ X - A → X 186
( M - Ans Y ) → C → Y ▶ IfEnd 199

```

功能 1：直出 Dx+Ey+F

輸入 顯示

選擇功能

1. 直出 Dx+Ey+F : 1

2. 圓線交點 : e

3. 三點求圓 : π

→  $x^2 + y^2 + \underline{\square} x + \underline{\square} y + \underline{\square} = 0$

Centre 圓心 = ( $\underline{\square}$ ,  $\underline{\square}$ )  
Radius 半徑 =  $\underline{\square}$

### 功能 2：圓線交點

**輸入**

**顯示**

#### 選擇功能

1. 直出  $Dx+Ey+F = 0$  : i

2. 圓線交點 : e

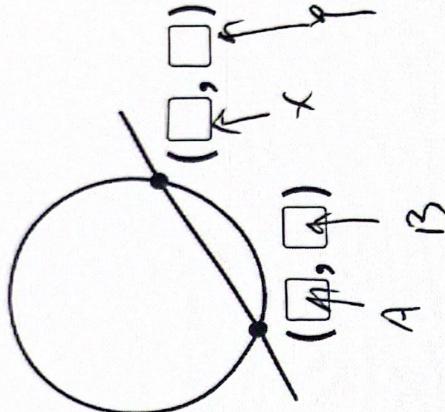
3. 三點求圓 : π

直線 :

$$\square x + \square y = \square$$

圓 :

$$x^2 + y^2 + \square x + \square y + \square = 0$$



### 功能 3：三點求圓

**輸入**

**顯示**

#### 選擇功能

1. 直出  $Dx+Ey+F = 0$  : i

2. 圓線交點 : e

3. 三點求圓 : π

$$(x - \square)^2 + (y - \square)^2 = \square^2$$

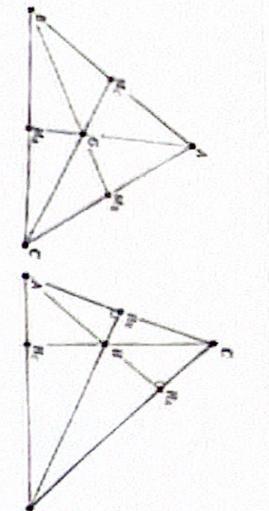


第一點 :  $\square + \square i$

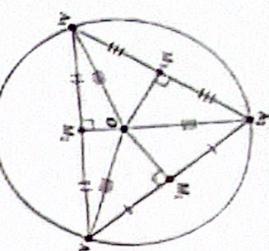
第二點 :  $\square + \square i$

第三點 :  $\square + \square i$

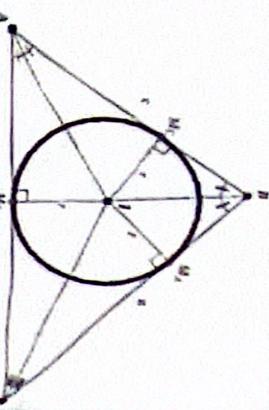
■ 課本 / 參考書 / 一般補習筆記：



**Centroid** is the point of intersection of three medians of a triangle. It divides the median internally in ratio 2 : 1.  
**形心為三角形的三條中線的交點。它將中線以2:1的比內分。**



**Orthocentre** is the point of intersection of three altitudes of a triangle.  
**垂心為三角形的三條高線的交點。**



**Circumcentre** is the point of intersection of three perpendicular bisectors of a triangle. It is equidistant from the three vertices of the triangle. It is also the centre of the circumcircle of the triangle.  
**外心為三角形的三條垂直平分線的交點。它與三角形的三個頂點等距。它亦為三角形的外接圓的圓心。**

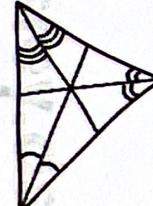
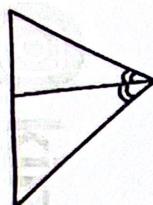
**In-centre** is the point of intersection of three angle bisectors of a triangle. It is equidistant from the three sides of the triangle. It is also the centre of the inscribed circle of the triangle.  
**內心為三角形的三條角平分線的交點。它與三角形的三邊等距。它亦為三角形的內切圓的圓心。**

- ◎ 將大量複雜內容塞入一幅圖，極簡消化  
 ◎ 沒有100%覆蓋DSE所有考點

## 〔考點一〕四心の基本概念

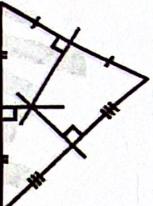
### In-centre (内心)

Angle Bisectors (角平分線) x3



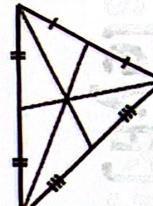
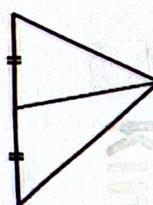
### Circumcentre (外心)

Perpendicular Bisectors (垂直平分線) x3



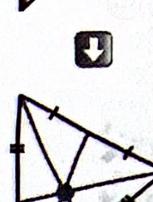
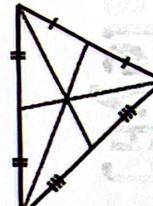
### Orthocentre (垂心)

Altitudes (高線) x3



### Centroid (形心)

Medians (中線) x3





# 速記方法 (英文版)

<b>Orthocentre</b> <b>Altitudes (x3)</b> “痾” “痾”	<b>In-centre</b> <b>Angle Bisectors (x3)</b> an in-centre	<b>Centroid</b> <b>Medians (x3)</b> send me
<b>Circumcentre</b> <b>Perpendicular Bisectors (x3)</b> 最長字 最長字		



# 速記方法 (中文版)

<b>形心</b> <b>中線 (x3)</b> 	<b>內心</b> <b>角平分線 (x3)</b> 	<b>垂心</b> <b>高線 (x3)</b> 	<b>外心</b> <b>垂直平分線 (x3)</b> 

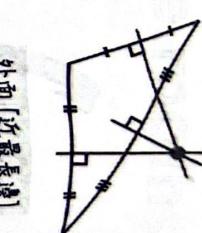
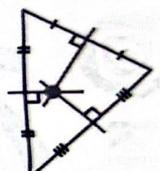
英 中

內 閣 , 誰 高

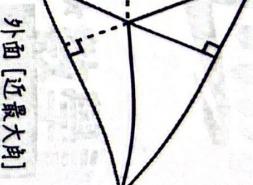
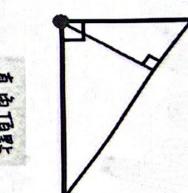
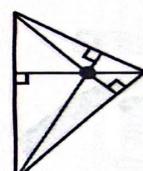
愛 誰

## ② [考點二] 四心の位置

Circumcentre (外心)  
Perpendicular Bisectors  
(垂直平分線) x3

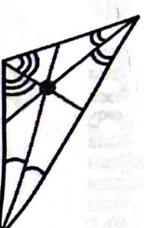
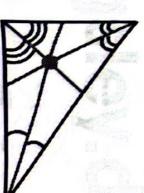
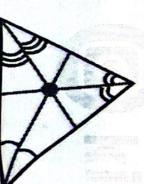


Orthocentre (垂心)  
Altitudes (高線) x3

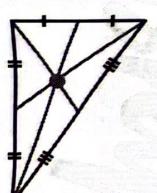
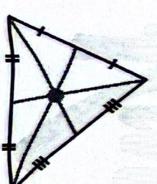


In-centre (内心)  
Angle Bisectors (角平分線) x3

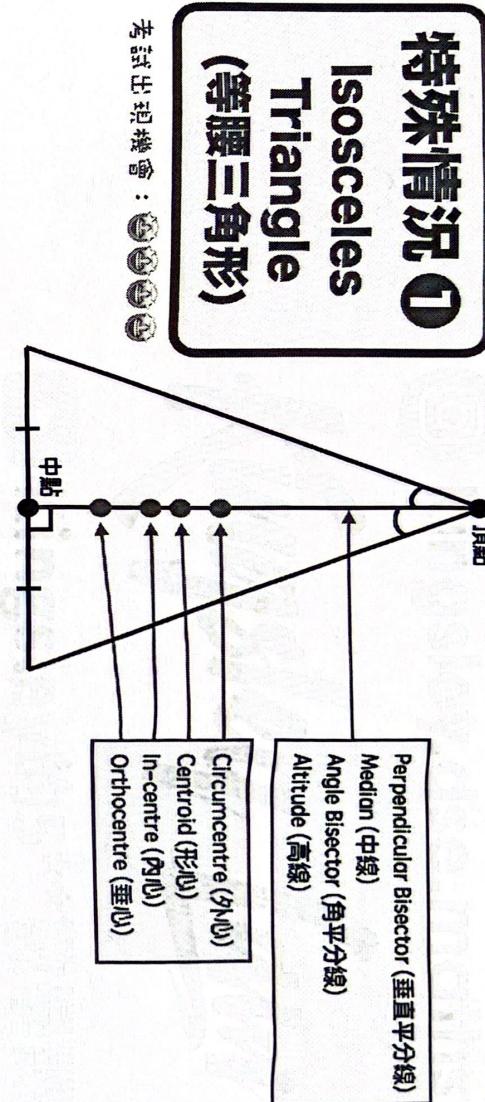
Acute-angled Triangle  
(锐角三角形)  
Right-angled Triangle  
(直角三角形)  
Obtuse-angled Triangle  
(钝角三角形)



Centroid (形心)  
Medians (中線) x3

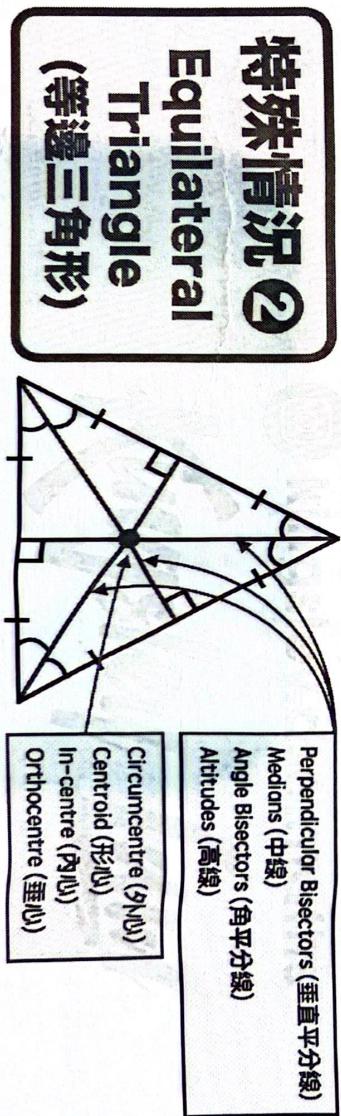


### 【考點三】四心の特殊情況



### 四心連成一線 / \*Collinear (共線)\*

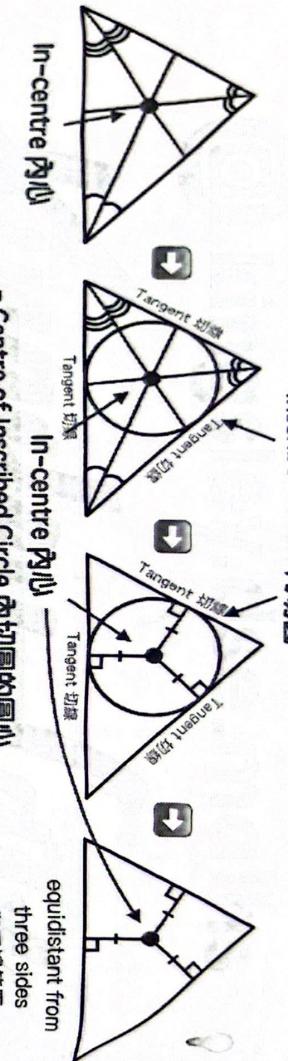
#### 【考點三】四心の特殊情況



考試出現機會：

# 四心在同一位置

## ♥ [考點四] In-centre (内心) の性質



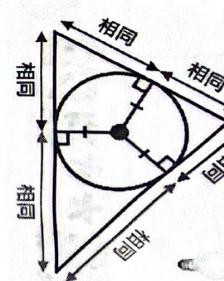
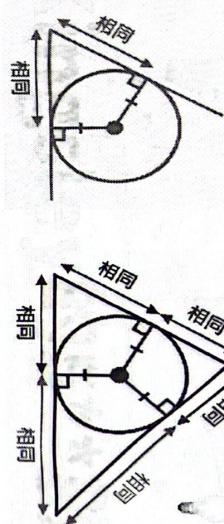
In-centre 内心

= Centre of Inscribed Circle 内切圓的圓心

equidistant from  
three sides  
與三邊等距

### 記憶召喚

Tangent Properties  
切線性質



## ♥ [考點五] Circumcentre (外心) の性質

Circumcircle 外接圓



$$OA = OB = OC$$

equidistant from three vertices  
與三個頂點等距

### ● 計數機玩法：[Prog B4] Four Centres 四心

Program B4, Four Centres 四心 (93 bytes)	
MODE : 2 (CMPLX)	
ClrMemory : ? → A : ? → B : ? → C : A + B + C → M : B - C → X : A - B → Y : M ↴ 3 ▲ X ↴ (A - C	44
→ D : C - i Y tan( arg( iD M - ▲ M ↴ 2 ▲ Abs(X) + Abs(A - C) - Abs(Y : Ans - i Ans tan(.5 arg(	82
D : C + Ans( .5 ↴ arg( X	93

輸入

$$\boxed{\phantom{0}} + \boxed{\phantom{0}}i$$

顯示

$$\boxed{\phantom{0}} + \boxed{\phantom{0}}i$$

$$\boxed{\phantom{0}} + \boxed{\phantom{0}}i$$

顯示

$$\text{Centroid 形心} = \boxed{\phantom{0}} + \boxed{\phantom{0}}i$$

SHIFT EXE

EXE

SHIFT EXE

$$\text{Orthocentre 垂心} = \boxed{\phantom{0}} + \boxed{\phantom{0}}i$$

EXE

SHIFT EXE

$$\text{Circumcentre 外心} = \boxed{\phantom{0}} + \boxed{\phantom{0}}i$$

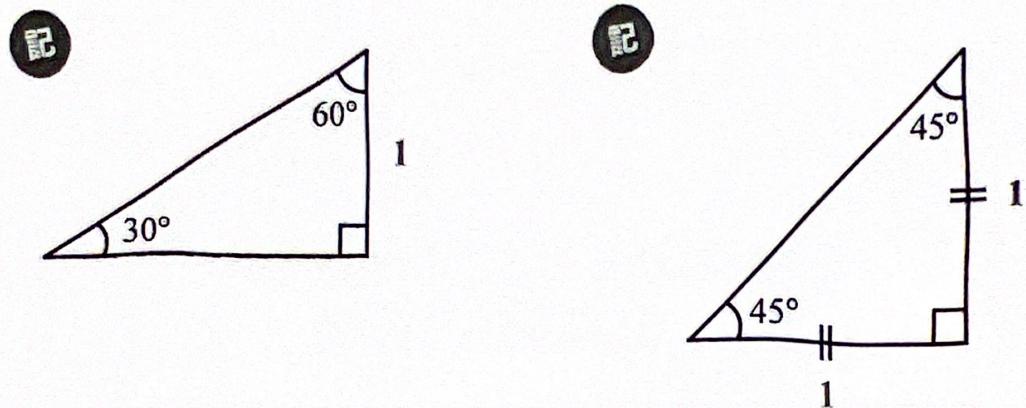
SHIFT EXE

$$\text{In-centre 內心} = \boxed{\phantom{0}} + \boxed{\phantom{0}}i$$

EXE

● 隱藏關鍵：最特別的直角三角形

👍 用途：一眼睇穿邊長比例 !!!



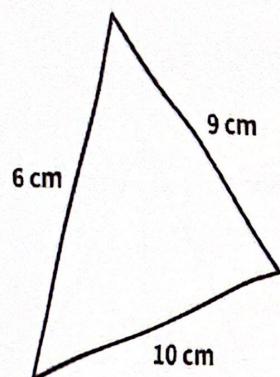
● 計數機玩法：【Prog B3】Trigonometry 三角

Program B3. 【5合1】 Trigonometry 三角 (200 bytes)	
MODE : 1 (COMP)	
ClrMemory : While 1 : ? → A : ? → B : ? → C : AB < 0 ⇒ Goto 0 : B → X : - sin( C ) ← sin( A → B : A < 0 ⇒ cos⁻¹( ( A² + X² - C² ) ) ← ( 2AX → B : X → C : Lbl 0 : C < 0 → D : Abs( A ▲ Abs( B ▲ A < 0 ⇒ Break : D ⇒ 180 - A - sin⁻¹( BC⁻¹ sin( A → C : C ▲ Pol( B tan( 90 - A - C , -B ) sin( A ▲ Y ▲ X sin( C ▲ -.5B Ans sin( A ▲ DY - A → C : Ans > 0 ⇒ Goto 0 : WhileEnd : cos⁻¹( D ⇒ A sin( B + C ) ← sin( C → C : -C ▲ Pol( Ans + A cos( B , -A sin( B : Y ▲ X ▲ 180 - B - Y ▲ .5AC sin( B	39
A < 0 ⇒ cos⁻¹( ( A² + X² - C² ) ) ← ( 2AX → B : X → C : Lbl 0 : C < 0 → D : Abs( A ▲ Abs( B ▲ A < 0 ⇒ Break : D ⇒ 180 - A - sin⁻¹( BC⁻¹ sin( A → C : C ▲ Pol( B tan( 90 - A - C , -B ) sin( A ▲ Y ▲ X sin( C ▲ -.5B Ans sin( A ▲ DY - A → C : Ans > 0 ⇒ Goto 0 : WhileEnd : cos⁻¹( D ⇒ A sin( B + C ) ← sin( C → C : -C ▲ Pol( Ans + A cos( B , -A sin( B : Y ▲ X ▲ 180 - B - Y ▲ .5AC sin( B	85
Break : D ⇒ 180 - A - sin⁻¹( BC⁻¹ sin( A → C : C ▲ Pol( B tan( 90 - A - C , -B ) sin( A ▲ Y ▲ X sin( C ▲ -.5B Ans sin( A ▲ DY - A → C : Ans > 0 ⇒ Goto 0 : WhileEnd : cos⁻¹( D ⇒ A sin( B + C ) ← sin( C → C : -C ▲ Pol( Ans + A cos( B , -A sin( B : Y ▲ X ▲ 180 - B - Y ▲ .5AC sin( B	126
C ▲ -.5B Ans sin( A ▲ DY - A → C : Ans > 0 ⇒ Goto 0 : WhileEnd : cos⁻¹( D ⇒ A sin( B + C ) ← sin( C → C : -C ▲ Pol( Ans + A cos( B , -A sin( B : Y ▲ X ▲ 180 - B - Y ▲ .5AC sin( B	163
C → C : -C ▲ Pol( Ans + A cos( B , -A sin( B : Y ▲ X ▲ 180 - B - Y ▲ .5AC sin( B	200

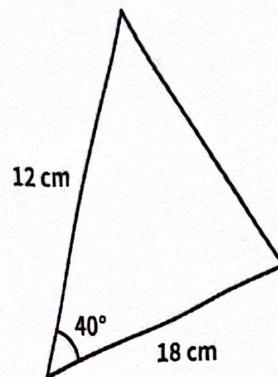
計數機玩法：【Prog B3】Trigonometry 三角

3 大原則

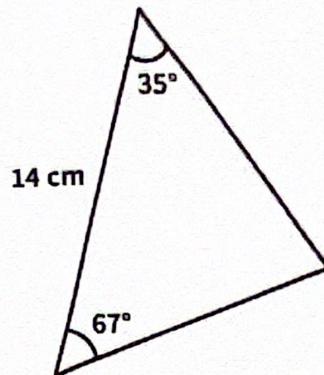
1 最短路線    2 先近后遠    3 邊長 = 負數



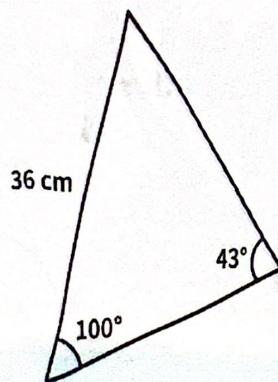
Area 面積 = \_\_\_\_\_



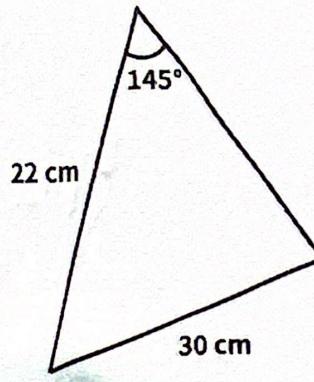
Area 面積 = \_\_\_\_\_



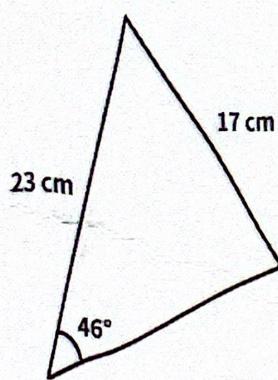
Area 面積 = \_\_\_\_\_



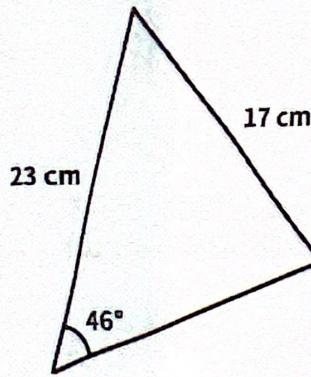
Area 面積 = \_\_\_\_\_



Area 面積 = \_\_\_\_\_



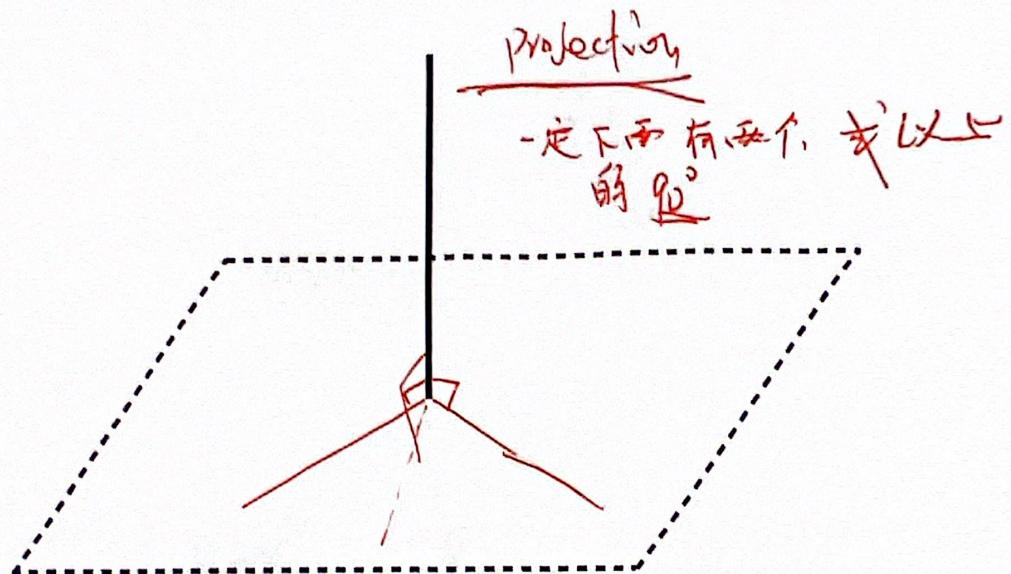
Area 面積 = \_\_\_\_\_



Area 面積 = \_\_\_\_\_

● 必讀考點：

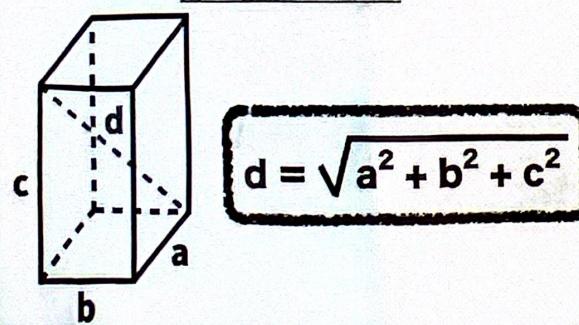
Vertical (鉛垂) / Perpendicular to Plane (垂直於平面) / Height (高)



● 5\*\*招式：立體畢氏定理

立體畢氏定理

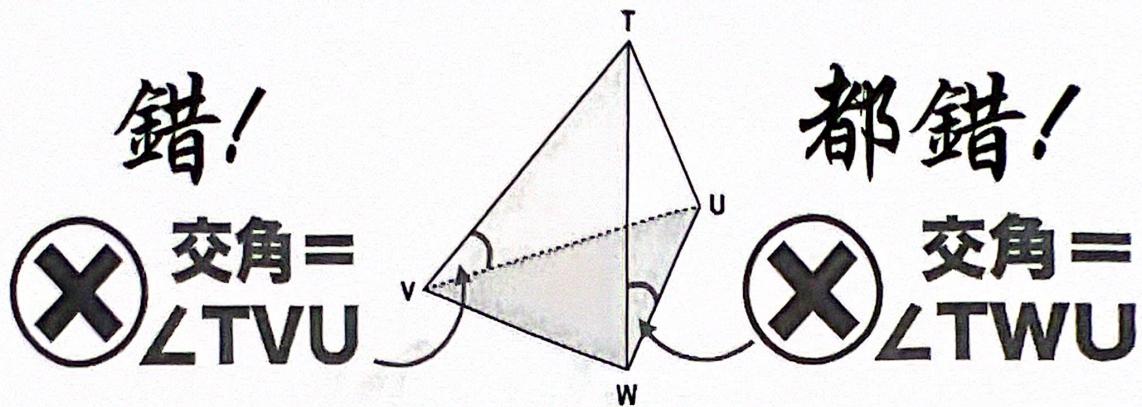
來源：[https://www.mathsisfun.com/geometry/  
pythagoras-3d.html](https://www.mathsisfun.com/geometry/pythagoras-3d.html)



## Angle between Two Planes

### 兩平面的交角【兩面交角】

In the figure,  $\Delta TVW \cong \Delta UVW$ . Find the angle between the plane  $TVW$  and the plane  $UVW$ .  
 圖中,  $\Delta TVW \cong \Delta UVW$ 。求平面  $TVW$  與平面  $UVW$  間的交角。

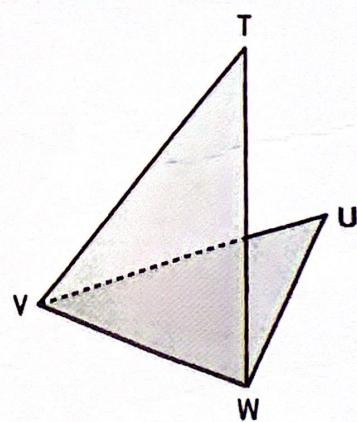


### ♥ 入腦秘笈：爬山故事【兩面交角】

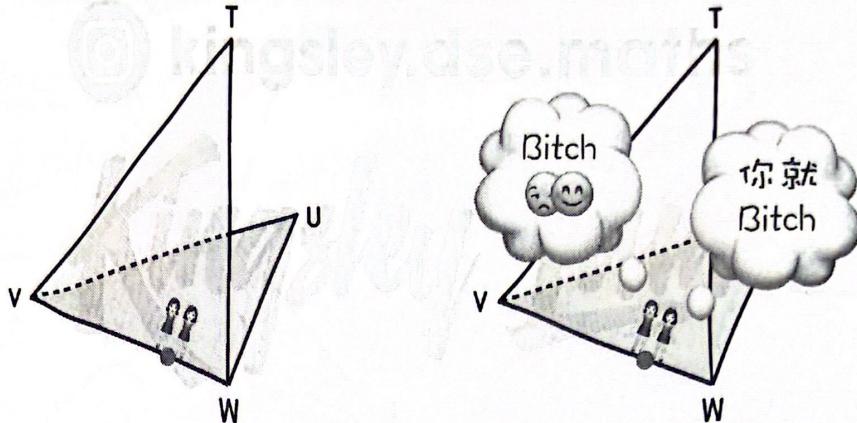
(In the figure,  $\Delta TVW \cong \Delta UVW$ .) Find the angle between the plane  $TVW$  and the plane  $UVW$ .  
 (圖中,  $\Delta TVW \cong \Delta UVW$ 。) 求平面  $TVW$  與平面  $UVW$  間的交角。

- ▲ 平面  $TVW$  = 山
- ▲ 平面  $UVW$  = 山
- \*相交線  $VW$  = 山腳

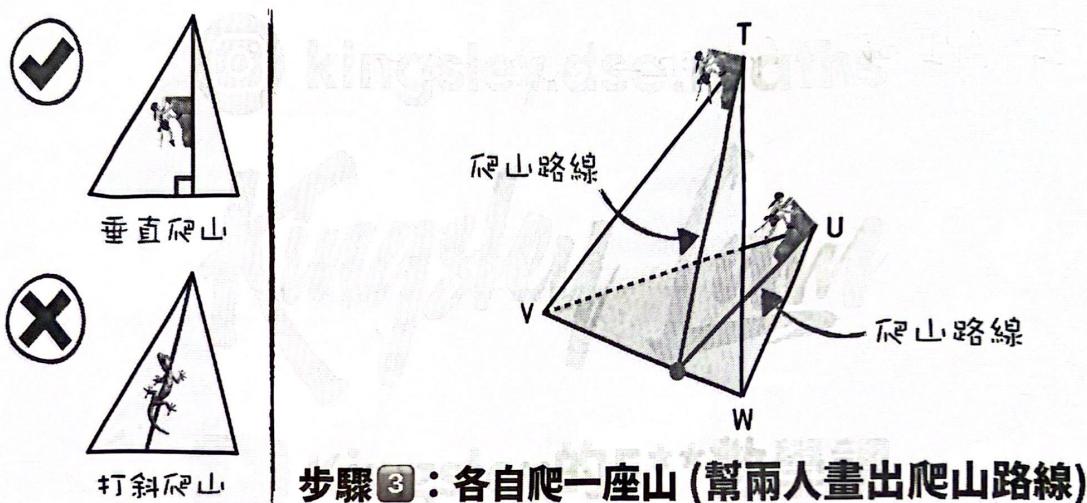
步驟①：找出山、山、山腳



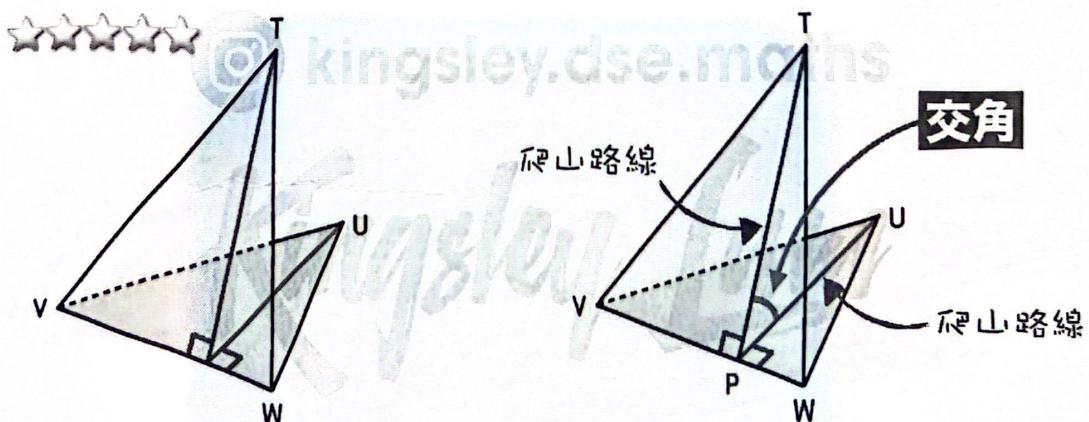
(In the figure,  $\triangle TVW \cong \triangle UVW$ .) Find the angle between the plane  $TVW$  and the plane  $UVW$ .  
 (圖中,  $\triangle TVW \cong \triangle UVW$ 。) 求平面  $TVW$  與平面  $UVW$  間的交角。



### 步驟②：兩人在山腳相遇 → 忽然吵架 → 決定分開爬山



### 步驟③：各自爬一座山 (幫兩人畫出爬山路線)

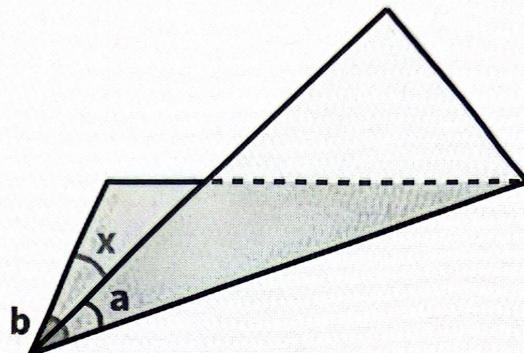


### 步驟④：畫直角(x2)      步驟⑤：爬山路線之間 = 交角

## 交角定理

Dihedral Angle Formula  
二面角公式

来源：[https://en.wikipedia.org/wiki/Dihedral\\_angle#Geometry](https://en.wikipedia.org/wiki/Dihedral_angle#Geometry)



Let (設) 交角 =  $\theta$

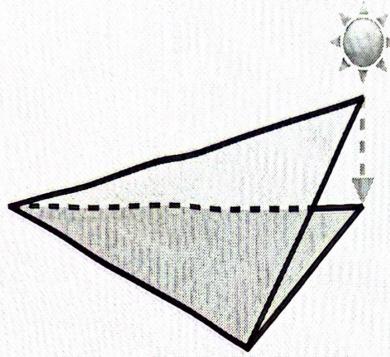
$$\cos \theta = \frac{\cos x - \cos a \cdot \cos b}{\sin a \cdot \sin b}$$

## ● 5\*\*招式：影の定理

### 影の定理

Area Projection Theorem  
面積投影定理

來源：HKCEE A.Maths 2003 – Q18

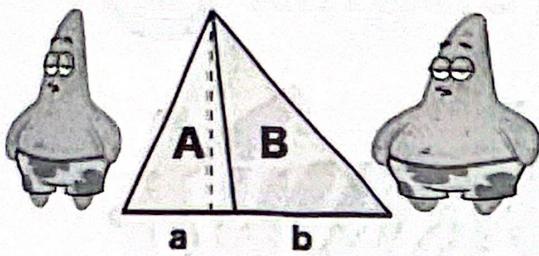


Let (設) 交角 =  $\theta$

$$\cos \theta = \frac{\text{影子面積}}{\text{斜面面積}}$$

● 隱藏關鍵：Ratio of Area (面積比)

钥匙 隱藏關鍵 (一)

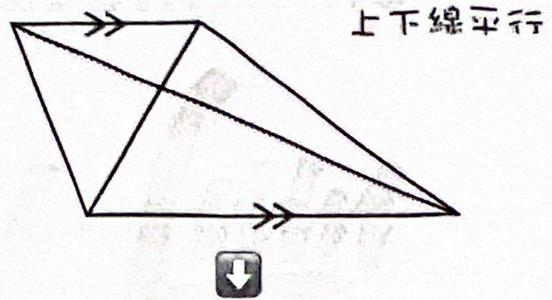


same height (同高)

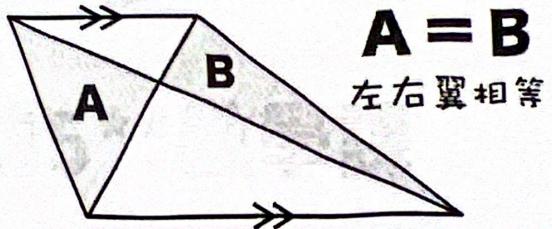
Ratio of base (底比) = Ratio of AREA (面積比)  
 $a : b = A : B$

底比  $\frac{a}{b} = \frac{A}{B}$  面積比

钥匙 隱藏關鍵 (二)



上下線平行



**A = B**

左右翼相等